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| Big Ideas | Details Unit: Kinematics (Motion) in Multiple Dimensions |
| | Projectile Motion |
| | Unit: Kinematics (Motion) in Multiple Dimensions |
| | NGSS Standards/MA Curriculum Frameworks (2016): N/A |
| | AP [®] Physics 1 Learning Objectives/Essential Knowledge (2024): 1.5.A, 1.5.A.1, 1.5.A.2, 1.5.A.3 |
| | Mastery Objective(s): (Students will be able to) |
| | Solve problems that involve motion in two dimensions. |
| | Success Criteria: |
| | Correct quantities are chosen in each dimension (x & y). |
| | Positive direction is chosen for each dimension and vector quantities in each dimension have the appropriate sign (+ or –). |
| | Time (scalar) is correct, positive, and the same in both dimensions. |
| | Algebra is correct and rounding to appropriate number of significant figures is reasonable. |
| | Language Objectives: |
| | Correctly identify quantities with respect to type of quantity and direction in word problems. |
| | Assign variables correctly in word problems. |
| | Tier 2 Vocabulary: projectile, dimension |
| | Labs, Activities & Demonstrations: |
| | • Play "catch." |
| | Drop one ball and punch the other at the same time. |
| | "Shoot the monkey." |
| | Notes: |
| | projectile: an object that is propelled (thrown, shot, <i>etc</i> .) horizontally and also falls due to gravity. |
| | Because perpendicular vectors do not affect each other, the vertical and horizontal motion of the projectile are independent and can be considered separately, using a separate set of equations for each. |
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| | Assuming we can neglect friction and air resistance (which is usually the cas year physics problems), we make the following important assumptions: | e in first- |
| | Horizontal Motion | |
| | The horizontal motion of a projectile is not affected by anything except for a resistance. If air resistance is negligible, we can assume that there is no hor acceleration, and therefore the horizontal velocity of the projectile, \vec{v}_x , is can be described by the equilation of a projectile can be described by the equilation. | air izontal onstant. uation: |
| | $\vec{d}_x = \vec{v}_x t$ | |
| | The projectile is always moving in the same horizontal direction, so we make positive (horizontal, or " x ") direction for the vector quantities of velocity and displacement. | e this the d |
| | Vertical Motion | |
| | Gravity affects projectiles the same way regardless of whether or not the pris also moving horizontally. All projectiles therefore have a constant downwacceleration of $\vec{g} = 10 \frac{m}{s^2}$ (in the vertical or "y" direction), due to gravity. | ojectile /ard |
| | Therefore, the vertical motion of the particle can be described by the equat | ions: |
| | $ec{m{v}}_{y}-ec{m{v}}_{o,y}=ec{m{g}}t$ | |
| | $\vec{\boldsymbol{d}}_{y} = \vec{\boldsymbol{v}}_{o,y}t + \frac{1}{2}gt^{2}$ | |
| | $\vec{\boldsymbol{v}}_{y}^{2} - \vec{\boldsymbol{v}}_{o,y}^{2} = 2\vec{\boldsymbol{g}}\vec{\boldsymbol{d}}$ | |
| | (Notice that we have <i>two</i> subscripts for initial velocity, because it is <i>both</i> the velocity v_0 <i>and also</i> the vertical velocity v_y .) | e initial |
| | If the projectile is always moving downwards (<i>i.e.,</i> it is launched horizontally falls), we make down the positive vertical direction and all vector quantities (velocity, displacement and acceleration) in the <i>y</i> -direction are positive. | and it |
| | If the projectile is launched upwards, reaches a maximum height, and then for velocity and displacement are sometimes upwards and sometimes downwards this case, we need to choose a direction to be positive. Usually, upward is compositive direction, which makes $\vec{v}_{o,y}$ positive, and makes \vec{v}_{y} and \vec{g} be negative. (In fact, $\vec{g} = -10 \frac{m}{s^2}$.) | ^a lls, the rds. In hosen to oth |
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| | Time | |
| | The time projectile equation horizonta | that the projectile spends falling must be the same as the time that the e spends moving horizontally. This means time (t) is the same in both is, which means time is the variable that links the vertical problem to the al problem. |
| | The cons | equences of these assumptions are: |
| | • T t | The <i>time</i> that the object takes to fall is determined by its movement <u>only</u> in the vertical direction. (When it hits the ground, it stops moving in all directions.) |
| | ⊺ ● (| The <i>horizontal distance</i> that the object travels is determined by the time from the vertical equation) and by its velocity in the horizontal direction. |
| | Therefor | e, the general strategy for most projectile problems is: |
| | 1. | Solve the vertical problem first, to get the time. |
| | 2. | Use the time from the vertical problem to solve the horizontal problem. |
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| | Sample problem: |
| | Q: A ball is thrown horizontally at a velocity of $5 \frac{m}{s}$ from a height of 1.5 m. How far does the ball travel (horizontally)? |
| | A: We're looking for the horizontal distance, d_x . We know the vertical distance, $d_y = 1.5 \text{ m}$, and we know that $v_{o,y} = 0$ (there is no initial vertical velocity |
| | because the ball is thrown horizontally), and we know that $a_y = g = 10 \frac{m}{s^2}$. |
| | We need to separate the problem into the horizontal and vertical components. |
| | Horizontal: Vertical: |
| | $d_x = v_x t$ $d_y = v_{o,y} t + \frac{1}{2}gt^2$ |
| | At this point we can't get any $d_y = \frac{1}{2}gt^2$ |
| | farther, so we need to turn to the vertical problem. $\frac{2u_y}{g} = t^2$ |
| | $t = \sqrt{\frac{2d_y}{q}}$ |
| | $t = \sqrt{\frac{(2)(1.5)}{2}} = \sqrt{0.3} = 0.55 \mathrm{s}$ |
| | V 10 |
| | Now that we know the time, we can substitute it back into the horizontal equation, giving: d = (5)(0.55) - 2.74 m |
| | $\sigma_{x} = (3)(0.33) = 2.7411$ |
| | A graph of the vertical vs. horizontal motion of the ball looks like this: |
| | 1.5 |
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| | 0 0.5 1 1.5 2 2.5 3 |
| | horizontal distance (m) |
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| honors & AP® | Sample Problem: |
| | Q: An Angry Bird [*] is launched upward from a slingshot at an angle of 40° with a velocity of $20 \frac{m}{s}$. The bird strikes the pigs' fortress at the same height that it was launched from. How far away is the fortress? |
| | |
| | A: We are looking for the horizontal distance, d_x . |
| | We start with the equation: |
| | $d_x = v_x t$ |
| | We need v_h and t . |
| | We can substitute for v_x using $v_x = v \cos \theta$ to get: |
| | $d_x = (v \cos \theta) t = 20 \cos(40^\circ) t = 15.3 t$ |
| | We can get <i>t</i> from: |
| | $d_{y} = v_{o,y}t + \frac{1}{2}gt^{2} = v(\sin\theta)t + \frac{1}{2}gt^{2} = 20(\sin 40^{\circ})t + \frac{1}{2}(-10)t^{2} = 12.9t - 5t^{2}$ |
| | Because the vertical displacement is zero (the angry bird ends at the same height as it started), $d_v = 0$: |
| | $0 = 12.9t - 5t^2$ |
| | 0 = t(12.9 - 5t) |
| | which has the solutions: |
| | t = 0, 12.9 - 5t = 0 |
| | The first solution ($t = 0$) is when the angry bird is launched. The second solution is the one of interest—when the angry bird lands. Solving for t gives: |
| | 12.9 = 5t |
| | $\frac{12.9}{5} = 2.57 \mathrm{s} = t$ |
| | We can now substitute this expression into the first equation to get: |
| | $d_x = 15.3 t = (15.3)(2.57) = 39.4 m$ |
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| | * Angry Birds was a video game from 2010 in which players used slingshots to shoot birds with the |
| II | necessary version y and angle to destroy a formess and kin the bad guys, who were green pigs. |



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| AP® | For each pair of graphs, the first graph is velocity vs. time. The slope, $rac{\Delta m{v}}{\Delta t}$, is | |
| | acceleration. Because acceleration is constant, the graph has to have a constant. if we choose up to be the positive direction (which is the most commo convention), correct answers would be (A), (B), and (D). If we choose down to be positive, only (C) would be correct. | n ? |
| | The second graph is acceleration vs. time. We know that acceleration is constant, which eliminates choices (A) and (B). We also know that acceleration is not zero, which eliminates choice (C). This leaves choice (D) as the only possible remaining answer. Choice (D) correctly shows a constant negative acceleration, because the slope of the first graph is negative, and the y-value of the second graph is also negative. | |
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| honors & AP® | 3. | (M – honors & AP[®]; A – CP1) A tiger leaps horizontally from a rock with height <i>h</i> at a speed of v_0 . What is the distance, <i>d</i> , from the base of the rock where the tiger lands? |
| | | (If you are not sure how to solve this problem, do #4 below and use the steps to guide your algebra.) |
| | | |
| | | |
| | | Answer: $d = v_{ol} \sqrt{\frac{2h}{2}}$ |
| | | °√ g |
| | 4. | (S – honors & AP[®]; M – CP1) A tiger leaps horizontally from a 7.5 m high rock with a speed of $4.5 \frac{m}{s}$. How far from the base of the rock will he land? |
| | | (You must start with the equations in your Physics Reference Tables and show all of the steps of GUESS. You may only use the answer to question #3 above as a starting point if you have already solved that problem.) |
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| | | Answer: 5.5 m |
| | 5. | (M) The pilot of an airplane traveling $45\frac{m}{s}$ wants to drop supplies to flood victims isolated on a patch of land 160 m below. The supplies should be dropped when the plane is how far from the island? |
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| | | Answer: 255 m |

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| honors & AP® | Problei | ms involving projectiles launched at an angle: | |
| | 6. | (M – honors & AP [®] ; A – CP1) A ball is shot out of a slingshot with of 10.0 ^m / _s at an angle of 40.0° above the horizontal. How far away land? | a velocity does it |
| | 7. | Answer: 9.85 m (S – honors & AP [®] ; A – CP1) The 12 Pounder Napoleon Model 18 primary cannon used during the American Civil War. If the canno muzzle velocity of $439 \frac{m}{s}$ and was fired at a 5.00° angle, what was effective range of the cannon (the distance it could fire)? (Negleor resistance.) | 57 was the n had a t the t air |
| I | | Answer: 3347 m (Note that this is more than 2 miles!) | |

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| honors & AP® | 8. | (M – AP [®] ; S – honors; A – CP1) A physics teacher is designing a ballistics event for a science competition. The ceiling is 3.00 m high, and the maximum velocity of the projectile will be $20.0 \frac{m}{s}$. |
| | | a. What is the maximum that the vertical component of the projectile's initial velocity could have? |
| | | Answer: 7.75 <u>m</u> |
| | | b. At what angle should the projectile be launched in order to achieve this maximum height? |
| | | Answer: 22.8° |
| | | Allswel. 22.0 |
| | | c. What is the maximum horizontal distance that the projectile could travel? |
| | | Answer: 28.6 m |

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