# **Centripetal Motion**

Unit: Kinematics (Motion) in Multiple Dimensions

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP<sup>®</sup> Physics 1 Learning Objectives/Essential Knowledge (2024): 2.9.A, 2.9.A.1,

2.9.A.1.i, 2.9.A.1.ii, 2.9.A.2, 2.9.A.2.i, 2.9.A.3, 2.9.A.4, 2.9.A.5, 2.9.A.5.i, 2.9.A.5.ii, 2.9.A.5.iii

Mastery Objective(s): (Students will be able to ... )

• Calculate the tangential and angular velocity and acceleration of an object moving in a circle.

#### Success Criteria:

- Correct quantities are chosen in each dimension (r,  $\omega$ ,  $\omega_o$ ,  $\alpha$ , a and/or  $\theta$ ).
- Algebra is correct and rounding to appropriate number of significant figures is reasonable.

Language Objectives:

- Explain why an object moving in a circle must be accelerating toward the center.
- Correctly identify quantities with respect to type of quantity and direction in word problems.
- Assign variables correctly in word problems.

Tier 2 Vocabulary: centripetal, centrifugal

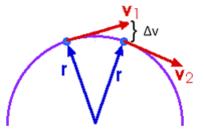
#### Labs, Activities & Demonstrations:

- Have students swing an object and let it go at the right time to try to hit something. (Be sure to observe the trajectory.)
- Swing a bucket of water in a circle.

### Notes:

If an object is moving at a constant speed around a circle, its speed is constant, its direction keeps changing as it goes around. Because <u>velocity</u> is a vector (speed and direction), this means its velocity is constantly changing. (To be precise, the magnitude is staying the same, but the direction is changing.)

Because a change in velocity over time is acceleration, this means the object is constantly accelerating. This continuous change in velocity is toward the center of the circle, which means there is continuous acceleration toward the center of the circle.



Use this space for summary and/or additional notes:

|           |   | Centripetal Motion   | Page: 249                           |  |  |
|-----------|---|--|-------------------------------------|--|--|
| Big Ideas | Details   | Unit: Kinematics (Motion) ir   | ۱ Multiple Dimensions               |  |  |
|           |   | ration ( <i>a<sub>c</sub></i> ): the constant acceleration of an ol tion that keeps it rotating around the center a  | •                                   |  |  |
|           | The equation <sup>*</sup> for centripetal acceleration ( $a_c$ ) is:            |  |                                     |  |  |
|           |   | $a_c = \frac{v^2}{r} = \frac{(r\omega)^2}{r} = r\omega^2$  |                                     |  |  |
|           | (The derivation of this equation requires calculus, so it will not be presented |  |                                     |  |  |
|           | Sample Problem:   |  |                                     |  |  |
|           | rotation of 10<br>weight? How   | ung from the end of a string that is 0.65 m lo<br>revolutions in 6.5 s. What is the centripetal a<br>many "g's" is that? ( <i>I.e.,</i> how many times the<br>centripetal acceleration?) | acceleration of the                 |  |  |
|           | A: There are two  | ways to solve this problem.  |                                     |  |  |
|           | Without using   | angular velocity:  |                                     |  |  |
|           | In each rev   | volution, the object travels a distance of $2\pi r$ :  |                                     |  |  |
|           |   | $s_{rev} = 2\pi r = (2)(3.14)(0.65) = 4.08 \mathrm{m}$   | ı                                   |  |  |
|           | The total o   | distance for 10 revolutions is therefore: s = 0  | (4.08)(10) = 40.8 m                 |  |  |
|           | The veloci  | ty is the distance divided by the time: $v = \frac{d}{t}$  | $=\frac{40.8}{6.5}=6.28\frac{m}{s}$ |  |  |
|           | Finally, $a_c$  | $=\frac{v^2}{r}=\frac{(6.28)^2}{0.65}=60.7\frac{m}{s^2}$   |                                     |  |  |
|           | This is $\frac{60}{10}$   | $\frac{7}{0}$ = 6.07 times the acceleration due to gravit  | ÿ.                                  |  |  |
| AP®       | Using angular   | velocity:  |                                     |  |  |
|           | The angula  | ar velocity is:  |                                     |  |  |
|           | $\left(\frac{10 \text{ rev}}{6.5 \text{ s}}\right)$                             | $\left(\frac{2\pi \text{ rad}}{1 \text{ rev}}\right) = \frac{20\pi}{6.5} = 9.67 \frac{\text{rad}}{\text{s}}$   |                                     |  |  |
|           | The centri  | petal acceleration is therefore:   |                                     |  |  |
|           | $a_{c} = r\omega^{2}$   |  |                                     |  |  |
|           | e   | $(9.67)^2 = (0.65)(93.44) = 60.7 \frac{m}{s^2}$  |                                     |  |  |
|           |   | $\frac{7}{0}$ = 6.07 times the acceleration due to gravit  | y.                                  |  |  |
|           |   |  |                                     |  |  |
|           | honors courses). Eq   | elates to angular motion (which is studied in AP® Physic<br>uations or portions of equations with angular velocity (<br>ly only to the AP® course.                                       |                                     |  |  |

Use this space for summary and/or additional notes:

## Centrinetal Motion

|           |                                 | Centripetal N                                      | /lotion  | Page: 250            |
|-----------|---------------------------------|--|--|----------------------|
| Big Ideas | Details                         | Uni  | t: Kinematics (Motion) in Mul                    | tiple Dimensions     |
|           | Centripetal motio               | n is a form of simple                              | harmonic motion (repetitive i                    | motion) and can      |
|           | be described usir               | g time period ( <i>T</i> ) and                     | frequency ( <i>f</i> ).                          |                      |
|           | (time) period (T,               | unit = s): The amount                              | of time that it takes for an ol                  | oject to             |
|           |                                 |  | riodic (repetitive) motion. In                   |                      |
|           | -                               | otion, the period is th<br>nplete revolution.      | e amount of time it takes for                    | the object to        |
|           | frequency (f, unit              | = Hz = $\frac{1}{s}$ ): The num                    | ber of cycles of repetitive mo                   | tion per unit of     |
|           | time. Freque                    | ncy and period are re                              | ciprocals of each other, <i>i.e.,</i>            | $f=rac{1}{T}$ and   |
|           | $T = \frac{1}{f}$               |  |  |                      |
|           | Because $v_{avg} = \frac{d}{t}$ | and the distance arou                              | nd the circle is the circumfer                   | ence, $C = 2\pi r$ , |
|           |                                 | eriod is equal to $T = \frac{2\pi}{N}$             |  |                      |
|           |                                 | ese quantities and relation unit, starting on page | ationships further in the <i>Intro</i><br>e 497. | duction: Simple      |
|           |                                 |  |  |                      |
|           |                                 |  |  |                      |
|           |                                 |  |  |                      |
|           |                                 |  |  |                      |
|           |                                 |  |  |                      |
|           |                                 |  |  |                      |
|           |                                 |  |  |                      |
|           |                                 |  |  |                      |
|           |                                 |  |  |                      |
|           |                                 |  |  |                      |
|           |                                 |  |  |                      |
|           |                                 |  |  |                      |
|           |                                 |  |  |                      |

Use this space for summary and/or additional notes:

| Big Ideas | Details          | Unit: Kinematics (Motion) in Multiple Dimensions  |  |
|-----------|------------------|---|--|
|           | Homework Problem |   |  |
|           | 1.               | One of the demonstrations we saw in class was swinging a bucket of water<br>in a vertical circle without spilling any of the water. |  |
|           |                  | a. (M) Explain why the water stayed in the bucket.  |  |
|           |                  |   |  |
|           |                  |   |  |
|           |                  |   |  |
|           |                  |   |  |
|           |                  |   |  |
|           |                  |   |  |
|           |                  | b. <b>(M)</b> If the combined length of your arm and the bucket is 0.90 m, what   |  |
|           |                  | is the minimum tangential velocity that the bucket must have in order to not spill any water?                                       |  |
|           |                  |   |  |
|           |                  |   |  |
|           |                  |   |  |
|           |                  |   |  |
|           |                  |   |  |
|           |                  |   |  |
|           |                  | Answer: 3.0 <sup>m</sup> / <sub>s</sub>   |  |
|           |                  | $\frac{1}{s}$   |  |

Use this space for summary and/or additional notes: