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Unit: Energy, Work & Power

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## **Power**

Unit: Energy, Work & Power

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP Physics 1 Learning Objectives/Essential Knowledge (2024): 3.5.A, 3.5.A.1,

3.5.A.2, 3.5.A.3, 3.5.A.4

Mastery Objective(s): (Students will be able to...)

• Calculate power as a rate of energy consumption.

#### **Success Criteria:**

- Variables are correctly identified and substituted correctly into the appropriate equations.
- Algebra is correct and rounding to appropriate number of significant figures is reasonable.

#### **Language Objectives:**

• Explain the difference between total energy and power.

Tier 2 Vocabulary: power

#### **Notes:**

<u>power</u>: a measure of the rate at which energy is applied or work is done. The average power is calculated by dividing work (or energy) by time.

$$P_{avg} = \frac{\Delta E}{t} = \frac{W}{t} = \frac{\Delta K + \Delta U}{t}$$

Power is a scalar quantity and is measured in Watts (W).

$$1W = 1\frac{J}{s} = 1\frac{N \cdot m}{s} = 1\frac{kg \cdot m^2}{s^3}$$

Note that utility companies measure energy in kilowatt-hours. This is because  $P = \frac{W}{L}$ , which means energy = W = Pt.

Because 1 kW = 1000 W and 1 h = 3600 s, this means 1 kWh = (1000 W)(3600 s) = 3600000 J

Because 
$$W = F_{\parallel}d$$
, this means  $P_{avg} = \frac{F_{\parallel}d}{t} = F_{\parallel}\left(\frac{d}{t}\right) = F_{\parallel}v_{avg}$ 

However, if we use the instantaneous velocity instead of the average velocity, this equation gives us the instantaneous power:

$$P_{inst} = F_{\parallel} v = F v \cos \theta$$

Big Ideas

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### **Power in Rotational Systems**

In a rotational system, the formula for power looks similar to the equation for power in linear systems, with force replaced by torque and linear velocity replaced by angular velocity:

$$P = Fv$$
  $P = \tau \omega$  linear rotational

## **Solving Power Problems**

Many power problems require you to calculate the amount of work done or the change in energy, which you should recall is:

$$W = F_{||} d$$
 if the force is caused by linear displacement 
$$\Delta K_t = \frac{1}{2} m v^2 - \frac{1}{2} m v_o^2$$
 if the change in energy was caused by a change in velocity 
$$\Delta U_g = mgh - mgh_o$$
 if the change in energy was caused by a change in height

# **Solving Rotational Power Problems**

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Power is also applicable to rotating systems:

$$W = \tau \Delta \theta$$
 if the work is produced by a torque 
$$\Delta K_r = \frac{1}{2} I \omega^2 - \frac{1}{2} I \omega_o^2$$
 if the change in energy was caused by a change in angular velocity

Once you have the work or energy, you can plug it in for either W,  $\Delta K$  or  $\Delta U$ , use the appropriate parts of the formula:

$$P = \frac{W}{t} = \frac{\Delta K + \Delta U}{t} = Fv = \tau \omega$$

and solve for the missing variable.

<sup>\*</sup>  $K_t$  is translational kinetic energy. This is the only form of kinetic energy used in CP1 and honors physics. The subscript t is used here to distinguish translational kinetic energy from rotational kinetic energy ( $K_r$ ), because both are used in AP® Physics.

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### **Sample Problems:**

Q: What is the power output of an engine that pulls with a force of 500. N over a distance of 100. m in 25 s?

A: 
$$W = Fd = (500)(100) = 50000 \text{ J}$$
  

$$P = \frac{W}{t} = \frac{50000}{25} = 2000 \text{ W}$$

Q: A 60. W incandescent light bulb is powered by a generator that is powered by a falling 1.0 kg mass on a rope. Assuming the generator is 100% efficient (*i.e.*, no energy is lost when the generator converts its motion to electricity), how far must the mass fall in order to power the bulb at full brightness for 1.0 minute?

A:  

$$P = \frac{\Delta U_g}{t} = \frac{mg \, \Delta h}{t}$$

$$60 = \frac{(1)(10) \, \Delta h}{60}$$

$$3600 = 10 \, \Delta h$$

$$\Delta h = \frac{3600}{10} = 360 \, \text{m}$$

Note that 360 m is approximately the height of the Empire State Building. This is why changing from incandescent light bulbs to more efficient compact fluorescent or LED bulbs can make a significant difference in energy consumption!

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# Homework Problems

1. **(S)** A small snowmobile has a 9000 W (12 hp) engine. It takes a force of 300. N to move a sled load of wood along a pond. How much time will it take to tow the wood across the pond if the distance is measured to be 850 m?

Answer: 28.3 s

2. **(M)** A winch, which is rated at 720 W, is used to pull an all-terrain vehicle (ATV) out of a mud bog for a distance of 2.3 m. If the average force applied by the winch is 1500 N, how long will the job take?

Answer: 4.8 s

3. **(S)** What is your power output if you have a mass of 65 kg and you climb a 5.2 m vertical ladder in 10.4 s?

Answer: 325 W

- 4. **(M)** Jack and Jill went up the hill. (The hill was 23m high.) Jack was carrying a 21 kg pail of water.
  - a. **(M)** Jack has a mass of 75 kg and he carried the pail up the hill in 45 s. How much power did he apply?

Answer: 490.7 W

b. **(M)** Jill has a mass of 55 kg, and she carried the pail up the hill in 35 s. How much power did she apply?

Answer: 499.4 W

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honors & AP®

5. **(M – honors & AP®; A – CP1)** The maximum power output of a particular crane is P. What is the fastest time, t, in which this crane could lift a crate with mass m to a height h?

(If you are not sure how to do this problem, do #6 below and use the steps to guide your algebra.)

Answer: 
$$t = \frac{mgh}{P}$$

6. **(S – honors & AP®; M – CP1)** The maximum power output of a particular crane is 12 kW. What is the fastest time in which this crane could lift a 3 500 kg crate to a height of 6.0 m?

(<u>You must start with the equations in your Physics Reference Tables and show all of the steps of GUESS.</u> You may only use the answer to question #5 above as a starting point if you have already solved that problem.)

Hint: Remember to convert kilowatts to watts.

Answer: 17.5 s

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7. **(M – AP®; A – honors & CP1)** A 30 cm diameter solid cylindrical flywheel with a mass of 2 500 kg was accelerated from rest to an angular velocity of 1 800 RPM in 60 s.

a. How much work was done on the flywheel?

Answer: 5.0×10<sup>5</sup> N⋅m

b. How much power was exerted?

Answer: 8.3×10<sup>3</sup> W