Class Notes for **Physics 2:**

Non-Mechanics Topics

(including AP® Physics 2) in Plain English

Jeff Bigler

April 2025



https://www.mrbigler.com/Physics-2/Notes-Physics-2.pdf

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> ISBN-13: 979-8545489268 ISBN-10: 8545489268

This is a set of class notes that can be used for an algebra-based, second-year high school Physics 2 course at the honors or AP[®] level. This hardcopy is provided so that you can fully participate in class discussions without having to worry about writing everything down.

While a significant amount of detail is included in these notes, they are intended as a supplement to textbooks, classroom discussions, experiments and activities. These class notes and any textbook discussion of the same topics are intended to be complementary. In some cases, the notes and the textbook differ in method or presentation, but the physics is the same. There may be errors and/or omissions in any textbook. There are almost certainly errors and omissions in these notes, despite my best efforts to make them clear, correct, and complete.

Topics

The AP[®] curriculum is, of course, set by the College Board. My decision was to have the same units in the honors course and the AP[®] course. However, the honors course has more flexibility with regard to pacing, difficulty, and topics.

Topics that are part of the curriculum for either the honors or AP[®] course but not both are marked in the left margin as follows:



Topics that are not otherwise marked should be assumed to apply to both courses.

The first two units (*Laboratory & Measurement* and *Mathematics*) are repeated from the Physics 1 notes, so these notes can be used without having to refer to them.

About the Homework Problems

The homework problems include a mixture of easy and challenging problems. *The process of making yourself smarter involves challenging yourself, even if you are not sure how to proceed.* By spending at least 10 minutes attempting each problem, you build neural connections between what you have learned and what you are trying to do. Even if you are not able to get the answer, when we go over those problems in class, you will reinforce the neural connections that led in the correct direction.

Answers to most problems are provided so you can check your work and see if you are on the right track. Do not simply write those answers down in order to receive credit for work you did not do. This will give you a false sense of confidence, and will actively prevent you from using the problems to make yourself smarter. *You have been warned.*

Using These Notes

As we discuss topics in class, you will want to add your own notes to these. If you have purchased this copy, you are encouraged to write directly in it, just as you would write in your own notebook. If this copy was issued to you by the school and you intend to return it at the end of the year, you will need to write your supplemental notes on separate paper. If you do this, be sure to write down page numbers in your notes, to make cross-referencing easier.

You should bring these notes to class every day, because lectures and discussions will follow these notes, which will also be projected onto the SMART board.

Features

These notes, and the course they accompany, are designed to follow both the 2016 Massachusetts Curriculum Frameworks, which are based on the Next Generation Science Standards (NGSS), and the AP[®] Physics 2 curriculum (2024 learning objectives). The notes also utilize strategies from the following popular teaching methods:

- Each topic includes Mastery Objectives and Success Criteria. These are based on the *Studying Skillful Teaching* course, from Research for Better Teaching (RBT), and are in "Students will be able to..." language.
- AP[®] topics include Learning Objectives and Essential Knowledge (2024) from the College Board.
- Each topic includes Next-Generation Science Standards (NGSS) and Massachusetts Curriculum Frameworks (2016). The MA Curriculum Frameworks are the same as the NGSS standards with the exception of a few MA-specific frameworks, which include (MA) in the identifier.
- Each topic includes Language Objectives and Tier 2 vocabulary words for English Learners, based on the Massachusetts Rethinking Equity and Teaching for English Language Learners (RETELL) course.
- Notes are organized in Cornell notes format as recommended by Keys To Literacy.
- Problems in problem sets are designated "Must Do" (M), "Should Do" (S) and "Aspire to Do" (A), as recommended by the Modern Classrooms Project (MCP).

Conventions

Some of the conventions in these notes are different from conventions in some physics textbooks. Although some of these are controversial and may incur the ire of other physics teachers, here is an explanation of my reasoning:

- When working sample problems, the units are left out of the algebra until the end. While I agree that there are good reasons for keeping the units to show the dimensional analysis, many students confuse units for variables, *e.g.*, confusing the unit "m" (meters) with the variable "m" (mass).
- Problems are worked using $g = 10 \frac{m}{s^2} = 10 \frac{N}{kg}$. This is because many students are not adept with algebra, and have trouble seeing where a problem is going once they take out their calculators. With simpler numbers, students have an easier time following the physics.
- Vector quantities are denoted with arrows as well as boldface, *e.g.*, \vec{v} , \vec{d} , \vec{F}_g . This is to help students keep track of which quantities are vectors and which are scalars. In some cases, this results in equations that are nonsensical as vector expressions, such as $\vec{v}^2 \vec{v}_o^2 = 2\vec{a}\vec{d}$. (A

vector can't be "squared", and multiplying \vec{a} by \vec{d} would have to be either $\vec{a} \cdot \vec{d}$ or $\vec{a} \times \vec{d}$.) It is good to point this out to students when they encounter these expressions, but in my opinion the benefits of keeping the vector notation even where it results in an incorrect vector expression outweigh the drawbacks.

• Forces are denoted as the variable \vec{F} with a subscript, e.g., \vec{F}_g , \vec{F}_f , \vec{F}_N , \vec{F}_τ , etc. instead of $m\vec{g}$, \vec{f} , \vec{N} , \vec{T} , etc. This is to reinforce the connection between a quantity (force), a single variable (\vec{F}), and a unit.

- Page 5
- Average velocity is denoted $\vec{v}_{ave.}$ instead of \vec{v} . I have found that using the subscript "ave." helps students remember that average velocity is different from initial and final velocity.
- The variable V is used for electric potential. Voltage (potential difference) is denoted by ΔV . Although $\Delta V = IR$ is different from how the equation looks in most physics texts, it is useful to teach circuits starting with electric potential, and it is useful to maintain the distinction between absolute electric potential (V) and potential difference (ΔV). This is also how the College Board represents electric potential vs. voltage on AP[®] Physics exams.
- Equations are typeset on one line when practical. While there are very good reasons for

teaching $\vec{a} = \frac{\vec{F}_{net}}{m}$ rather than $\vec{F}_{net} = m\vec{a}$ and $I = \frac{\Delta V}{R}$ rather than $\Delta V = IR$, students' difficulty in solving for a variable in the denominator often causes more problems than does their lack of understanding of which are the independent and dependent variables.

Learning Progression

There are several categories of understandings and skills that simultaneously build on themselves throughout this course:

Content

The content topics are:

- Thermal Physics (Heat) & Thermodynamics
- Electricity & Magnetism
- Mechanical Waves
- Electromagnetic Waves, Light & Optics
- Quantum, Particle, Atomic & Nuclear Physics

Preliminary "unit zero" topics such as laboratory and mathematical skills are presented in the Physics 1 notes, and are not duplicated here.

Problem-Solving

This course builds on the problem-solving skills from Physics 1. The topics in this course require more high-level thinking to decide what the situation is for each problem, and which equation(s) apply.

Laboratory

This course continues the experimental design lessons learned in Physics 1. Because the topics require more specialized equipment, more time will be spent teaching students to use the equipment and giving them sufficient time to practice with it.

Scientific Discourse

In this course, the causal relationships between quantities are more complex than in Physics 1. Students need to continue to be given opportunities to explain these relationships throughout the course, both orally and in writing. These notes would not have been possible without the assistance of many people. It would be impossible to include everyone, but I would particularly like to thank:

- Every student I have ever taught, for helping me learn how to teach, and how to explain and convey challenging concepts.
- The physics teachers I have worked with over the years who have generously shared their time, expertise, and materials. In particular, Mark Greenman, who has taught multiple courses on teaching physics and who, as the PhysTEC Teacher in Residence at Boston University, organizes a monthly meeting for Boston-area physics teachers to share laboratory activities and demonstrations; Barbara Watson, whose AP® Physics 1 and AP® Physics 2 Summer Institutes I attended, and with whom I have had numerous conversations about the teaching of physics, particularly at the AP® level; and Eva Sacharuk, who met with me weekly during my first year teaching physics to share numerous demonstrations, experiments and activities that she collected over her many decades in the classroom.
- Every teacher I have worked with, for their kind words, sympathetic listening, helpful advice and suggestions, and other contributions great and small that have helped me to enjoy and become competent at the profession of teaching.
- The department heads, principals and curriculum directors I have worked with, for mentoring me, encouraging me, allowing me to develop my own teaching style, and putting up with my experiments, activities and apparatus that place students physically at the center of a physics concept. In particular: Mark Greenman, Marilyn Hurwitz, Scott Gordon, Barbara Osterfield, Wendell Cerne, John Graceffa, Maura Walsh, Lauren Mezzetti, Jill Joyce, Tom Strangie, Anastasia Mower, and Rardy Peña.
- Everyone else who has shared their insights, stories, and experiences in physics, many of which are reflected in some way in these notes.

I am reminded of Sir Isaac Newton's famous quote, "If I have seen further it is because I have stood on the shoulders of giants."

About the Author

Jeff Bigler is a physics teacher at Lynn English High School in Lynn, Massachusetts. He has degrees from MIT in chemical engineering and biology, and is a National Board certified teacher in Science– Adolescence and Young Adulthood. He worked in biotech and IT prior to starting his teaching career in 2003. He has taught both physics and chemistry at all levels from conceptual to AP[®].

He is married and has two adult daughters. His hobbies are music and Morris dancing.

Errata

As is the case in just about any large publication, these notes undoubtedly contain errors despite my efforts to find and correct them all.

Known errata for these notes are listed at: https://www.mrbigler.com/Physics-2/Notes-Physics-2-errata.shtml

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NGSS Standards/MA Curriculum Frameworks

Except where denoted with (MA), these standards are the same as the Next Generation Science (NGSS) Standards. Standards that are crossed out (like this) are covered in the Physics 1 notes. Note that both sets of notes may be necessary in order to cover all of the standards.

Standard	Topics	Chapters
HS-PS1-8	fission, fusion & radioactive decay: α , β & γ ; energy released/absorbed	9
HS-PS2-1	Newton's 2nd (F _{net} = ma), motion graphs; ramps, friction, normal force, gravity, magnetic force	Physics 1
HS-PS2-2	conservation of momentum	7
HS-PS2-3	lab: reduce impulse in a collision	—
HS-PS2-4	gravitation & coulomb's law including relative changes	6
HS-PS2-5	electromagnetism: current produces magnetic field & vice-versa, including examples	8
HS-PS2-9(MA)	Ohm's Law, circuit diagrams, evaluate series & parallel circuits for ΔV , I or R.	7
HS-PS2-10(MA)	free-body diagrams, algebraic expressions & Newton's laws to predict acceleration for 1-D motion, including motion graphs	Physics 1
HS-PS3-1	conservation of energy including thermal, kinetic, gravitational, magnetic or electrical including gravitational & electric fields	5
HS-PS3-2	energy can be motion of particles or stored in fields. kinetic → thermal, evaporation/condensation, gravitational potential energy , electric fields	4, 6
HS-PS3-3	lab: build a device that converts energy from one form to another.	Physics 1
HS-PS3-4a	zero law of thermodynamics (heat flow & thermal equilibrium)	5
HS-PS3-5	behavior of charges or magnets attracting & repelling	6, 8
HS-PS4-1	waves: $v = f\lambda \& T = 1/f$, EM waves traveling through space or a medium vs. mechanical waves in a medium	9, 10
HS-PS4-3	EM radiation is both wave & particle. Qualitative behavior of resonance, interference, diffraction, refraction, photoelectric effect and wave vs. particle model for both	10, 11
HS-PS4-5	Devices use waves and wave interactions with matter, such as solar cells, medical imaging, cell phones, wi-fi	10

MA Science Practices

Practice	Description
SP1	Asking questions.
SP2	Developing & using models.
SP3	Planning & carrying out investigations.
SP4	Analyzing & interpreting data.
SP5	Using mathematics & computational thinking.
SP6	Constructing explanations.
SP7	Engaging in argument from evidence.
SP8	Obtaining, evaluating and communicating information.

Big Ideas	Introduction: Laboratory & MathematicsPage: 9DetailsUnit: Laboratory & Mathematics
-	Introduction: Laboratory & Mathematics
	Unit: Laboratory & Mathematics
	Note that the topics of laboratory experiments, experimental design, uncertainty, solving word problems, vector math, and trigonometry are covered in the Physics 1 notes, and are not repeated here.
	Topics covered in this chapter:
	The AP [®] Physics Science Practices11
	Vectors15
	Vectors vs. Scalars in Physics23
	Vector Multiplication26
	Logarithms
	The purpose of this chapter is to teach prerequisite skills that will be used later in the course.
	• The AP [®] Physics Science Practices lists & describes the scientific practices that are required by the College Board for AP [®] Physics 2.
	• Vectors, Vectors vs. Scalars in Physics, and Vector Multiplication describe properties of vectors and how mathematics with vectors works.
	• Logarithms is a review of the base 10 and natural logarithm functions.
	Calculating uncertainty (instead of relying on significant figures) is a new and challenging skill that will be used in lab write-ups throughout the year.
	Standards addressed in this chapter:
	NGSS Standards/MA Curriculum Frameworks (2016):
	This chapter addresses the following MA science and engineering practices:
	Practice 1: Asking Questions and Defining Problems
	Practice 2: Developing and Using Models
	Practice 3: Planning and Carrying Out Investigations
	Practice 4: Analyzing and Interpreting Data
	Practice 6: Constructing Explanations and Designing Solutions
	Practice 7: Engaging in Argument from Evidence
	Practice 8 : Obtaining, Evaluating, and Communicating Information

Introduction: Laboratory & Mathematics Page: 10

Big Ideas	Details Unit: Laboratory & Mathematics
AP®	AP [®] Physics 2 Science Practices (2024):
	This chapter addresses the following AP Physics 1 science practices:
	SP 4.1 The student can justify the selection of the kind of data needed to answer a particular scientific question.
	SP 4.2 The student can design a plan for collecting data to answer a particular scientific question.
	SP 4.3 The student can collect data to answer a particular scientific question.
	SP 4.4 The student can evaluate sources of data to answer a particular scientific question.
	SP 5.1 The student can analyze data to identify patterns or relationships.
	SP 5.2 The student can refine observations and measurements based on data analysis.
	SP 5.3 The student can evaluate the evidence provided by data sets in relation to a particular scientific question.
	Skills learned & applied in this chapter:
	 Working with exponential and logarithmic functions.
	Prerequisite Skills:
	These are the mathematical understandings that are necessary for Physics 1 that are taught in the MA Curriculum Frameworks for Mathematics.
	 Construct and use tables and graphs to interpret data sets.
	 Solve simple algebraic expressions.
	 Perform basic statistical procedures to analyze the center and spread of data.
	 Measure with accuracy and precision (<i>e.g.</i>, length, volume, mass, temperature, time)
	 Convert within a unit (e.g., centimeters to meters).
	 Use common prefixes such as milli-, centi-, and kilo
	 Use scientific notation, where appropriate.
	 Use ratio and proportion to solve problems.
	<i>Fluency in all of these understandings is a prerequisite for this course.</i> Students who lack this fluency may have difficulty passing the class.

AP®

Details

The AP® Physics Science Practices

Unit: Laboratory & Measurement

NGSS Standards/MA Curriculum Frameworks (2016): SP1, SP2, SP3, SP4, SP5, SP6, SP7

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): SP1, SP2, SP3, SP4, SP5, SP6, SP7

Mastery Objective(s): (Students will be able to...)

• Describe what the College Board and the State of Massachusetts want you to know about how science is done.

Tier 2 Vocabulary: data, claim, justify

Language Objectives:

• Explain the what the student is expected to do for each of the AP[®] Science Practices.

Tier 2 Vocabulary: practice, pose, model

Notes:

The College Board has described the scientific method in practical terms, dividing them into seven Science Practices that students are expected to learn in AP Physics 1.

Science Practice 1: The student can use representations and models to communicate scientific phenomena and solve scientific problems.

A model is any mental concept that can explain and predict how something looks, works, is organized, or behaves. Atomic theory is an example of a model: matter is made of atoms, which are made of protons, neutrons, and electrons. The number, location, behavior and interactions of these sub-atomic particles explains and predicts how different types of matter behave.

- 1.1 The student can *create representations and models* of natural or man-made phenomena and systems in the domain.
- 1.2 The student can *describe representations and models* of natural or manmade phenomena and systems in the domain.
- 1.3 The student can *refine representations and models* of natural or man-made phenomena and systems in the domain.
- 1.4 The student can *use representations and models* to analyze situations or solve problems qualitatively and quantitatively.
- 1.5 The student can express key elements of natural phenomena across multiple representations in the domain.

The AP[®] Physics Science Practices Page: 12

Big Ideas	Details Unit: Laboratory & Measurement
AP®	Science Practice 2: The student can use mathematics appropriately.
	Physics is the representation of mathematics in nature. It is impossible to
	understand physics without a solid understand of mathematics and how it relates to
	physics. For AP Physics 1, this means having an intuitive feel for how algebra works, and how it can be used to relate quantities or functions to each other. If you are the
	type of student who solves algebra problems via memorized procedures, you may
	struggle to develop the kind of mathematical understanding that is necessary in AP
	Physics 1.
	2.1 The student can justify the selection of a mathematical routine to solve
	problems.
	2.2 The student can <i>apply mathematical routines</i> to quantities that describe natural phenomena.
	2.3 The student <i>can estimate numerically quantities</i> that describe natural phenomena.
	Science Practice 3: The student can engage in scientific questioning to extend
	thinking or to guide investigations within the context of the AP course.
	Ultimately, the answer to almost any scientific question is "maybe" or "it depends".
	Scientists pose questions to understand not just what happens, but the extent to which it happens, the causes, and the limits beyond which outside factors become
	dominant.
	3.1 The student can pose scientific questions.
	3.2 The student can refine scientific questions.
	3.3 The student can evaluate scientific questions.
	Science Practice 4 : The student can plan and implement data collection strategies in relation to a particular scientific question.
	Scientists do not "prove" things. Mathematicians and lawyers prove that something
	must be true. Scientists collect data in order to evaluate what happens under
	specific conditions, in order to determine what is likely true, based on the
	information available. Data collection is important, because the more and better the data, the more scientists can determine from it.
	4.1 The student can <i>justify the selection of the kind of data</i> needed to answer a
	particular scientific question.
	4.2 The student can <i>design a plan</i> for collecting data to answer a particular scientific question.
	4.3 The student can <i>collect data</i> to answer a particular scientific question.

Dialdoor	The AP® Physics Science Practices Page: 1
Big Ideas	Details Unit: Laboratory & Measureme 4.4 The student can <i>evaluate sources of data</i> to answer a particular scientific
AP®	question.
	Science Practice 5: The student can perform data analysis and evaluation of evidence.
	Just as data collection is important, analyzing data and being able to draw meaningful conclusions is the other crucial step to understanding natural phenomena. Scientists need to be able to recognize patterns that actually exist within the data, and to be free from the bias that comes from expecting a particula result beforehand.
	5.1 The student can <i>analyze data</i> to identify patterns or relationships.
	5.2 The student can <i>refine observations and measurements</i> based on data analysis.
	5.3 The student can <i>evaluate the evidence provided by data sets</i> in relation to particular scientific question.
	Science Practice 6: The student can work with scientific explanations and theories.
	In science, there are no "correct" answers, only claims and explanations. A scientific claim is any statement that is believed to be true. In order to be accepted, a claim must be verifiable based on evidence, and any claim or explanation must be able to make successful predictions, which are also testable. Science does not prove claims to be universally true or false; science provides supporting evidence. Other scientis will accept or believe a claim provided that there is sufficient evidence to support if and no evidence that directly contradicts it.
	6.1 The student can justify claims with evidence.
	6.2 The student can <i>construct explanations of phenomena based on evidence</i> produced through scientific practices.
	6.3 The student can articulate the reasons that scientific explanations and theories are refined or replaced.
	6.4 The student can make <i>claims and predictions about natural phenomena</i> based on scientific theories and models.
	6.5 The student can evaluate alternative scientific explanations.

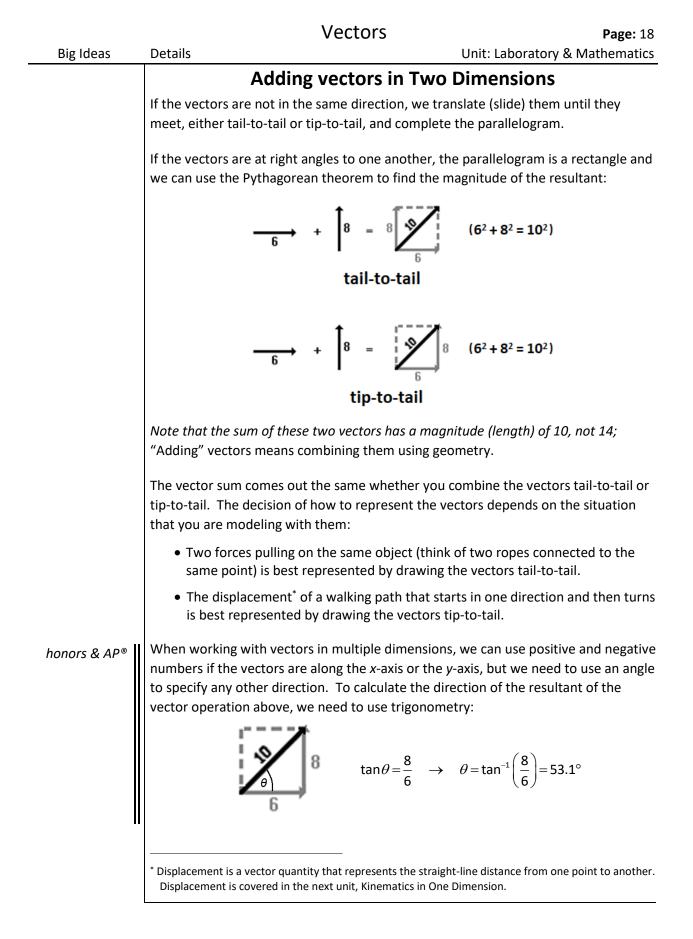
The AP[®] Physics Science Practices

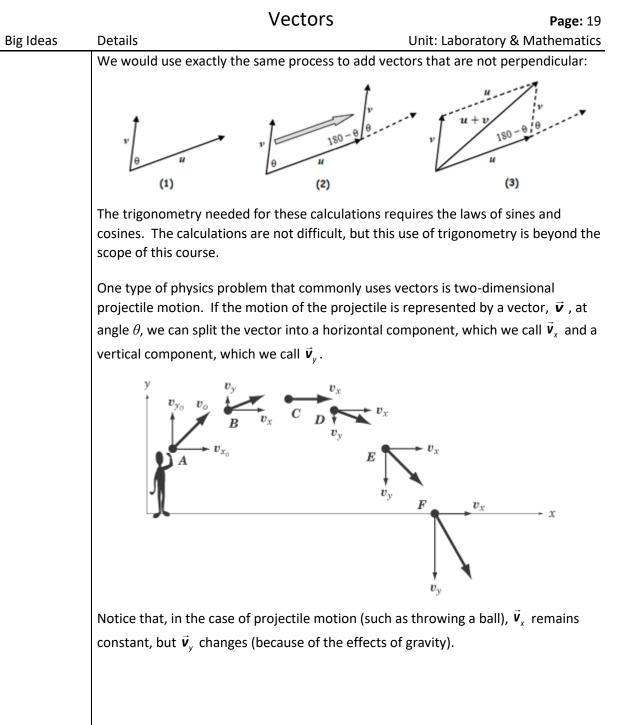
	THE AT THYSICS SCIENCE TRACTICES Page. 14
Big Ideas	Details Unit: Laboratory & Measurement
AP®	Science Practice 7: The student is able to connect and relate knowledge across
AP®	various scales, concepts, and representations in and across domains.
	If a scientific principle is true in one domain, scientists must be able to consider that principle in other domains and apply their understanding from the one domain to the other. For example, conservation of momentum is believed by physicists to be universally true on every scale and in every domain, and it has implications in the contexts of laboratory-scale experiments, quantum mechanical behaviors at the atomic and sub-atomic levels, and special relativity.
	7.1 The student can <i>connect phenomena and models</i> across spatial and temporal scales.
	7.2 The student can <i>connect concepts</i> in and across domain(s) to generalize or extrapolate in and/or across enduring understandings and/or big ideas.

		Ve	ectors	Page: 15
Big Ideas	Details			Unit: Laboratory & Mathematics
			Vectors	5
	Unit: Labora	tory & Mathematic	S	
	NGSS Standa	ards/MA Curriculur	n Frameworks (20	016): SP5
	AP [®] Physics	1 Learning Objectiv	ves/Essential Kno	wledge (2024): 1.1.A.1, 1.1.A.2,
	1.1.A.3,	1.1.A.3.i, 1.1.A.3.ii,	1.1.B.1, 1.5.A, 1.5	5.A.1, 1.5.A.2, 1.5.A.3
	Mastery Obj	jective(s): (Student	s will be able to)
	 Identif 	fy the magnitude ar	d direction of a v	ector.
	Combi Success Crite		Illy and calculate	the magnitude and direction.
	 Magnitude 	e is calculated corre	ectly (Pythagorear	n theorem).
	• Direct		(using trigonome	etry) or direction (<i>e.g.,</i> "south", "to
	Language Ol			
	• Explain	n what a vector is a	nd what its parts	are.
	Tier 2 Vocab	oulary: magnitude,	direction	
	Notes:			
	vector: a qua	antity that has a dir	ection as well as a	a magnitude (value/quantity).
	<i>E.g.,</i> if yo is north.	-	to the north, the	magnitude is $1\frac{m}{s}$ and the direction
	-	ntity that has a valu you think of as a "re		oes not have a direction. (A scalar ncluding its unit.)
	-	-		rection (<i>i.e.,</i> the value including its , the magnitude of the force is
	by two c	ouble vertical bars	(like double abso	agnitude of a vector is represented lute value bars) around the vector. $\vec{F} = 25 \text{ N}$. However, to make
	typesett $\left \vec{F} \right = 25 N$	-	mon to use regula	ar absolute value bars instead, <i>e.g.,</i>
		vector that is the re of two vectors).	sult of a mathem	atical operation (such as the

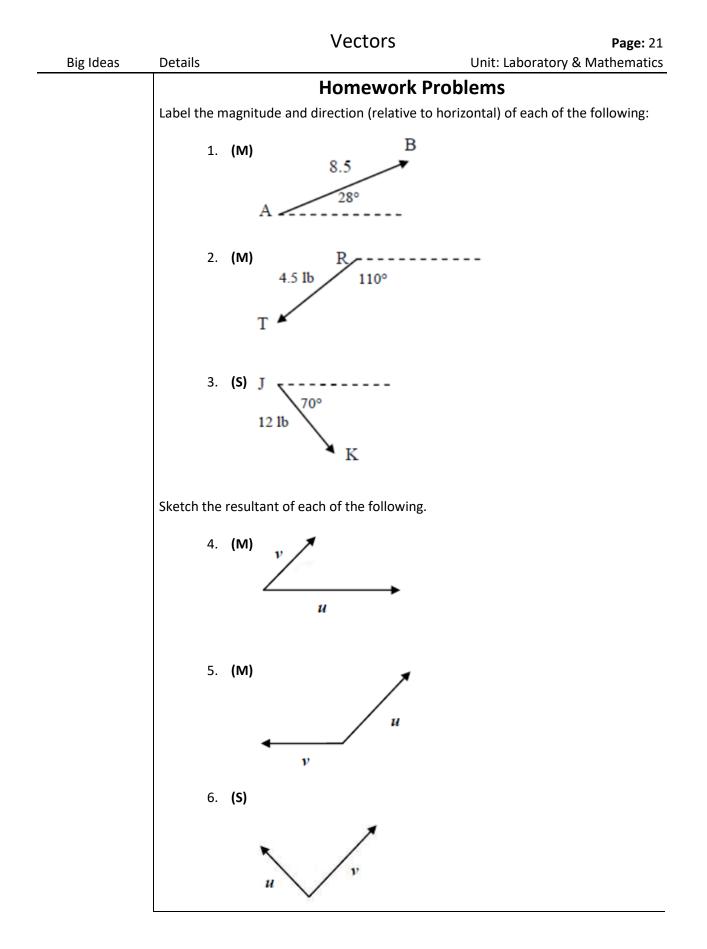
Vectors Page: 16
Details Unit: Laboratory & Mathematics
Variables that represent vectors are traditionally typeset in bold Italics . Vector variables may also optionally have an arrow above the letter:
J, F, v
Variables that represent scalars are traditionally typeset in <i>plain Italics:</i>
V, t, λ
Variable that represent only the magnitude of a vector (<i>e.g.,</i> in equations where the direction is not relevant) are typeset as if they were scalars:
For example, suppose \vec{F} is a vector representing a force of 25 N to the east. (Notice that the vector includes the magnitude or amount and the direction.)
If we needed a variable to represent only the magnitude of 25 N, we would use the variable <i>F</i> .
Vectors are represented graphically using arrows. The length of the arrow represents the magnitude of the vector, and the direction of the arrow represents the direction of the vector:
$\xrightarrow{10}$ \leftarrow $\xrightarrow{15}$ \uparrow 7
magnitude 10 magnitude 15 magnitude 7
direction: "to the direction: "to the left", direction: right", 0° +180° "up", +90°
The negative of a vector is a vector with the same magnitude in the opposite direction:
$\xrightarrow{10}$ \leftarrow^{-10}
Note, however, that we use positive and negative numbers to represent the direction of a vector, but a negative value for a vector does not mean the same thing as a negative number in mathematics. In math, $-10 < 0 < +10$, because positive

		Vectors	Page: 17
Big Ideas	Details		Unit: Laboratory & Mathematics
	However, a <i>velocity</i> of -10	$\frac{m}{s}$ means "10 $\frac{m}{s}$ in the n	egative direction". This means
	that $-10\frac{m}{s} > +5\frac{m}{s}$, because	se the first object is mov	ing faster than the second ($10\frac{m}{s}$
	<i>vs.</i> $5\frac{m}{s}$), even though the o	bjects are moving in opp	oosite directions.
		Translating Vect	tors
	Vectors have a magnitude a translate a vector (in the ge its size or orientation), and	ometry sense, which me	eans to move it without changing
	For example, consider a per force of 5 N to the right. W to be to the right, which me	e will define the positive	e direction
	If the force is moved to the still 5 N to the right (+5 N), same vector:		5 N
			Dimension horizontal), adding vectors is
	+	$\begin{array}{c} 5 \\ -5 \\ -5 \\ -5 \\ -5 \\ -5 \\ -5 \\ -15 \end{array} + \begin{array}{c} 10 \\ -5 \\ -5 \\ -15 \\ -15 \end{array}$	0
	(† -)	10 + -5 ↓ =	5





	Vectors		Page: 20			
Big Ideas	Details		Unit: Laboratory & Math	nematics		
	Because perpendicular vectors the two directions separately.	s do not affect each c	other, we can apply equat	ions to		
	For example, in projectile mot use the equation $\vec{d} = \vec{v}_o t + \frac{1}{2}\vec{a}_c$			-		
This gives us two equations.						
	In the horizontal (x)-direction:					
		$\vec{d}_x = \vec{v}_{o,x}t + \frac{1}{2}\vec{a}_x$	t^{0}			
		$\vec{d}_x = \vec{v}_x t$				
	In the vertical (y)-direction:					
		$\vec{\bm{d}}_y = \vec{\bm{v}}_{o,y} t + \frac{1}{2} \vec{\bm{a}}_y t^2$				
		$\vec{\bm{d}}_{y} = \vec{\bm{v}}_{o,y} t + \frac{1}{2} \vec{\bm{g}} t^{2}$				
	Note that each of the vector q components. For example, \vec{v}_o					
	direction) is independent of \vec{v}_{0} direction). This means we tree solve for one without affecting	_{o,y} (the component o at them as completely	f the initial velocity in the	e x-		



ig Ideas Details		Unit: Laboratory & Mathematic
Consider t	he following vectors $\vec{A} \otimes \vec{B}$.	
	has a magnitude of 9 and its s the positive horizontal direction ht).	$\vec{A} = 9$ $\vec{B} = 12$
	has a magnitude of 12 and its s the positive vertical direction	↓
7.	(M) Sketch the resultant of $\vec{A} + \vec{B}$, direction [*] .	and determine its magnitude and
8.	(S) Sketch the resultant of $\vec{A} - \vec{B}$ (w determine its magnitude and directi	

Vectors vs. Scalars in Physics

Unit: Laboratory & Mathematics

NGSS Standards/MA Curriculum Frameworks (2016): SP5

AP® Physics 1 Learning Objectives/Essential Knowledge (2024): 1.1.A.1, 1.1.A.3

Mastery Objective(s): (Students will be able to...)

• Identify vector vs. scalar quantities in physics.

Success Criteria:

• Quantity is correctly identified as a vector or a scalar.

Language Objectives:

- Explain why some quantities have a direction and others do not.
- Tier 2 Vocabulary: magnitude, direction

Notes:

In physics, most numbers represent quantities that can be measured or calculated from measurements. Most of the time, there is no concept of a "deficit" of a measured quantity. For example, quantities like mass, energy, and power can only be nonnegative, because in classical mechanics there is no such thing as "anti-mass," "anti-energy," or "anti-power."

However, vector quantities have a direction as well as a magnitude, and direction can be positive or negative.

A rule of thumb that works *most* of the time in a high school physics class is:

<u>Scalar quantities</u>. These are usually positive, with a few notable exceptions (*e.g.*, work and electric charge).

<u>Vector quantities</u>. Vectors have a direction associated with them. For onedimensional vectors, the direction is conveyed by defining a direction to be "positive". Vectors in the positive direction are expressed as positive numbers, and vectors in the opposite (negative) direction are expressed as negative numbers.

In some cases, you will need to split a vector into two component vectors, one vector in the *x*-direction, and a separate vector in the *y*-direction, in order to solve a problem. In these cases, you will need to choose which direction is positive and which direction is negative for <u>both</u> the *x*- and *y*-axes. Once you have done this, every vector quantity must be assigned a positive or negative value, according to the directions you have chosen.

Vectors vs. Scalars in Physics

Big Ideas	Details Unit: Laboratory & Mathematics
	<u>Differences</u> . The difference or change in a variable is indicated by the Greek letter Δ in front of the variable. Any difference can be positive or negative. However, note that a difference can either be a vector, indicating a change relative to the positive direction (<i>e.g.</i> , Δx , which indicates a change in position), or scalar, indicating an increase or decrease (<i>e.g.</i> , ΔV , which indicates a change in volume).
	Example:
	Suppose you have a problem that involves throwing a ball straight upwards with a velocity of $15\frac{m}{s}$. Gravity is slowing the ball down with a downward acceleration of
	$10\frac{m}{s^2}$. You want to know how far the ball has traveled in 0.5 s.
	Displacement, velocity, and acceleration are all vectors. The motion is happening in the <i>y</i> -direction, so we need to choose whether "up" or "down" is the positive direction. Suppose we choose "up" to be the positive direction. This means:
	• When the ball is first thrown, it is moving upwards. This means its velocity is in the <u>positive</u> direction, so we would represent the initial velocity as $\vec{v}_o = +15 \frac{m}{s}$.
	• Gravity is accelerating the ball downwards, which is the <u>negative</u> direction. We would therefore represent the acceleration as $\vec{a} = -10 \frac{m}{s^2}$.
	• Time is a scalar quantity, so its value is +0.5 s.
	If we had to substitute the numbers into the formula:
	$\vec{d} = \vec{v}_o t + \frac{1}{2}\vec{a}t^2$
	we would do so as follows:
	$\vec{d} = (+15)(0.5) + (\frac{1}{2})(-10)(0.5)^2$
	and we would find out that $\vec{d} = +6.25 \mathrm{m}$.
	The answer is <i>positive</i> . Earlier, we defined positive as "up", so the answer tells us that the displacement is upwards from the starting point.

Big Ideas	Details Unit: Laboratory & Mathematics
Big Ideas	Details Unit: Laboratory & Mathematics What if, instead, we had chosen "down" to be the positive direction?
	• When the ball is first thrown, it is moving upwards. This means its velocity is now in the <u>negative</u> direction, so we would represent the initial velocity as $\vec{v}_o = -15\frac{m}{s}$.
	• Gravity is accelerating the ball downwards, which is the <u>positive</u> direction. We would therefore represent the acceleration as $\vec{a} = +10 \frac{m}{s^2}$.
	• Time is a scalar quantity, so its value is +0.5 s.
	If we had to substitute the numbers into the formula:
	$\vec{\boldsymbol{d}} = \vec{\boldsymbol{v}}_o t + \frac{1}{2} \vec{\boldsymbol{a}} t^2$
	we would do so as follows:
	$\vec{d} = (-15)(0.5) + (\frac{1}{2})(10)(0.5)^2$
	and we would find out that $\vec{d} = -6.25 \mathrm{m}$.
	The answer is <u>negative</u> . However, remember that we defined "down" to be positive, which means "up" is the negative direction. This means the displacement is <u>upwards</u> from the starting point, as before.
	In any problem you solve, the choice of which direction is positive vs. negative is arbitrary. The only requirement is that <i>every vector quantity in the problem</i> needs to be consistent with your choice.

Vectors vs. Scalars in Physics

Page: 25

Details

Vector Multiplication

Unit: Laboratory & Mathematics

NGSS Standards/MA Curriculum Frameworks (2016): SP5

AP® Physics 1 Learning Objectives/Essential Knowledge (2024): 1.1.B.1

Mastery Objective(s): (Students will be able to...)

- Correctly use and interpret the symbols "•" and "×" when multiplying vectors.
- Finding the dot product & cross product of two vectors.

Success Criteria:

• Magnitudes and directions are correct.

Language Objectives:

• Explain how to interpret the symbols "•" and "×" when multiplying vectors.

Tier 2 Vocabulary: magnitude, direction, dot, cross

Notes:

With scalar (ordinary) numbers, there is only one way to multiply them, which you learned in elementary school. Vectors, however, can be multiplied in three different ways.

dot product: multiplication of two vectors that results in a scalar.

$\vec{A} \bullet \vec{B} = C$

<u>cross product</u>: multiplication of two vectors that results in a new vector.

$\vec{I} \times \vec{J} = \vec{K}$

<u>tensor product</u>: multiplication of two vectors that results in a tensor. $\vec{A} \otimes \vec{B}$ is a matrix of vectors that results from multiplying the respective components of each of the two vectors. It describes the effect of each component of the vector on each component of every other vector in the array. Tensors are beyond the scope of a high school physics course.

Multiplying a Vector by a Scalar

Multiplying a vector by a scalar is like multiplying a variable by a number. The magnitude changes, but the direction does not. For example, in physics, displacement equals velocity times time:

 $\vec{d} = \vec{v}t$

Velocity is a vector; time is a scalar. The magnitude is the velocity times the time, and the direction of the displacement is the same as the direction of the velocity.

If the two vectors have opposite directions, the equation needs a negative sign. For example, the force applied by a spring equals the spring constant (a scalar quantity) times the displacement:

 $\vec{F}_{s} = -k\vec{x}$

The negative sign in the equation signifies that the force applied by the spring is in the opposite direction from the displacement.

The Dot (Scalar) Product of Two Vectors

The scalar product of two vectors is called the "dot product". Dot product multiplication of vectors is represented with a dot:

 $\vec{A} \bullet \vec{B}^*$

The dot product of \vec{A} and \vec{B} is:

 $\vec{A} \bullet \vec{B} = AB \cos \theta$

where *A* is the magnitude of \vec{A} , *B* is the magnitude of \vec{B} , and θ is the angle between the two vectors \vec{A} and \vec{B} .

For example, in physics, <u>work</u> (a scalar quantity) is the dot product of the vectors <u>force</u> and <u>displacement</u> (distance):

$$W = \vec{F} \bullet \vec{d} = Fd \cos \theta$$

^{*} pronounced "A dot B"

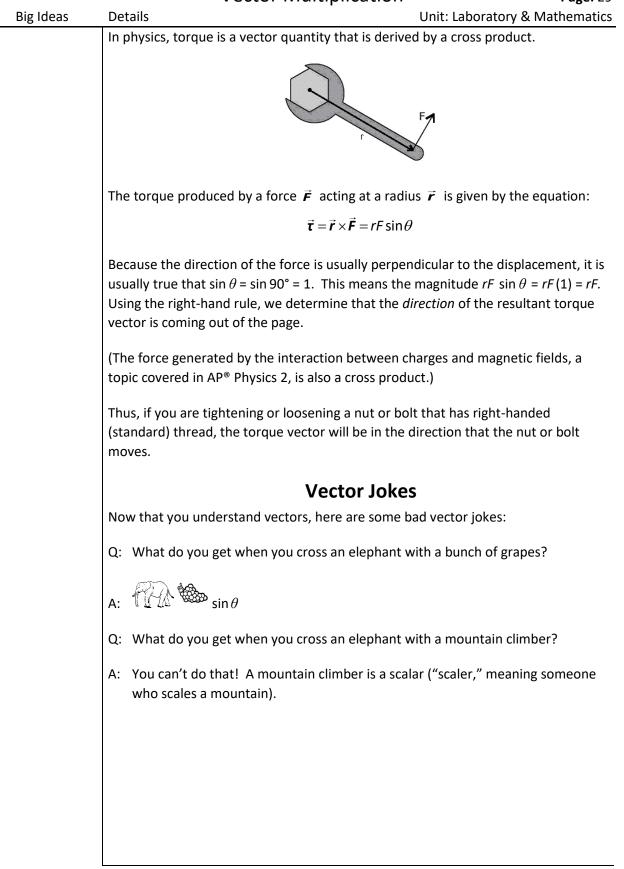
Big Ideas

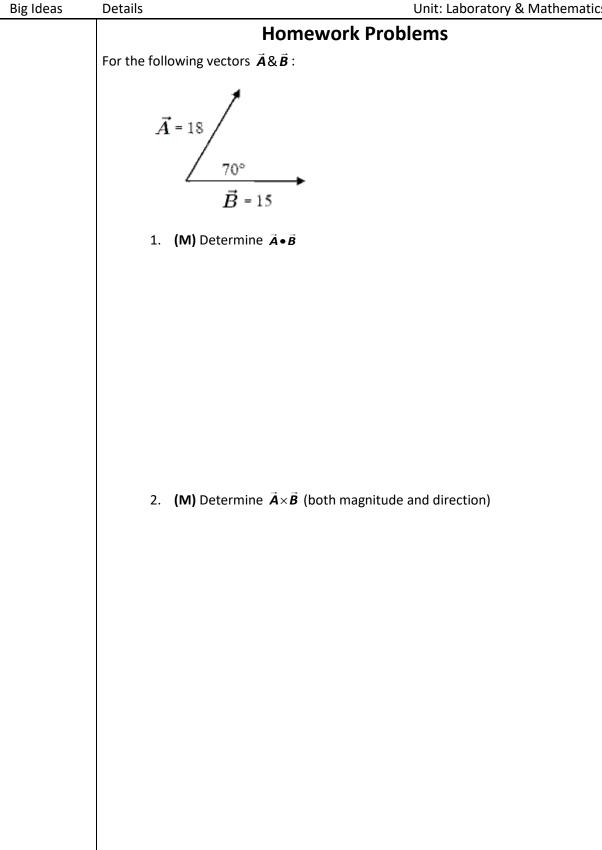
Details

Vector Multiplication

Big Ideas	Details Unit: Laboratory & Mathematics					
	The Cross (Vector) Product of Two Vectors					
	The vector product of two vectors is called the cross product. Cross product					
	multiplication of vectors is represented with a multiplication sign:					
	$\vec{A} \times \vec{B}^*$					
	The magnitude of the cross product of vectors \vec{A} and \vec{B} that have an angle of θ between them is given by the formula:					
	$\vec{A} \times \vec{B} = AB \sin \theta$					
	The direction of the cross product is a little difficult to make sense out of. You can figure it out using the "right hand rule":					
	Position your right hand so that your fingers curl from the first vector to the second. Your thumb points in the direction of the resultant vector. \vec{c}					
	Note that this means that the resultant vectors for $\vec{A} \times \vec{B}$ and $\vec{B} \times \vec{A}$ point in <i>opposite</i> directions, <i>i.e.</i> , the cross product of					
	two vectors is <u>not</u> commutative!					
	\vec{A} $\vec{A} \times \vec{B} = \vec{C}$					
	$\vec{B} imes \vec{A} = -\vec{C}$					
	On a two-dimensional piece of paper, a vector coming toward you (out of the page) is denoted by a set of \odot \odot \odot \odot \odot symbols, and a vector going away from you (into the page) is denoted by a set of \otimes \otimes \otimes \otimes \otimes \otimes symbols. Think of these symbols as representing an arrow inside a tube or pipe. The dot					
	represents the tip of the arrow coming toward you, and the "X" represents the fletches (feathers) on the tail of the arrow going away from you.)					
	* pronounced "A cross B"					

Vector Multiplication





AP® Physics 2 Learning Objectives/Essential Knowledge (2024): N/A

Knowledge/Understanding:

• What logarithms represent and an intuitive understanding of logarithmic quantities.

Skills:

• Use logarithms to solve for a variable in an exponent.

Language Objectives:

• Understand the use of the terms "exponential" and "logarithm" and understand the vernacular use of "log" (otherwise a Tier 1 word) as an abbreviation for "logarithm".

Tier 2 Vocabulary: function

Notes:

The logarithm may well be the least well-understood function encountered in high school mathematics.

The simplest logarithm to understand is the base-ten logarithm. You can think of the (base-ten) logarithm of a number as the number of zeroes after the number.

х		log10(x)
100 000	10 ⁵	5
10 000	10 ⁴	4
1 000	10 ³	3
100	10 ²	2
10	10 ¹	1
1	10 ⁰	0
0.1	10 ⁻¹	-1
0.01	10 ⁻²	-2
0.001	10 ⁻³	-3
0.000 1	10 ⁻⁴	-4
0.000 01	10 ⁻⁵	-5

As you can see from the above table, the logarithm of a number turns a set of numbers that vary exponentially (powers of ten) into a set that vary linearly.

Logarithms

Digldooc	Details	202	gantini		Page		
Big Ideas	Details			Unit: Laboratory 8			
	•	You can get a visual sense of the logarithm function from the logarithmic number					
	line below:						
	3	579	30	50 70 90 300	500 700 90		
	1 2 4	6 8 10	20	40 60 80 100 200	400 600 800		
				e same as the <i>distance</i> from			
				stance to every number on th	is number		
	is the logarithm of t	he number					
				distance from beginning			
		X	$\log_{10}(x)$	of number line			
		10 ⁰	0	0			
	10	0 ^{0.5} ≈ 3.16	0.5	½ cycle			
		10 ¹ = 10	1	1 cycle			
		$10^2 = 100$	2	2 cycles			
	1	$0^3 = 1000$	3	3 cycles			
				is true for numbers that are r			
	numbers get larger. The most useful ma into the linear part of			f logarithms is that they move	e an expon		
		-		$f_{10}(10) = (3)(1) = 3$			
	In fact, the logarithr	n function	works the s	same way for any base, not ju	ıst 10:		
		lo	g ₂ (2 ⁷) = 7 lo	$g_2(2) = (7)(1) = 7$			
	(In this case, the wo equation is:	ord "base" i	means the l	base of the exponent.) The g	مسمسما		
					eneral		
			$\log_x(a^b)$	$=b\log_x(a)$	eneral		
			ng for the ex	= <i>b</i> log _x (<i>a</i>) xponent in an equation. This in most mathematical equati	is, in fact,		
			ng for the ex	xponent in an equation. This	is, in fact,		
			ng for the ex	xponent in an equation. This	is, in fact,		
			ng for the ex	xponent in an equation. This	is, in fact,		
			ng for the ex	xponent in an equation. This	is, in fact,		

			Loga	arithms	Page: 3	33
Big Ideas	Details		Ū		Unit: Laboratory & Mathemati	CS
	Sample prob	lem:				
	Q: Solve $3^x = 3^x$	15 for <i>x</i> .				
		-		e) of both side t the base is 10	es. (Note that writing "log" without 0.)	
	$log(3^{x}) = lo$ x log(3) = lo (x)(0.477) = $x = \frac{1.176}{0.477} =$	og(15) = 1.176				
	This is the o	correct a	nswer, b	ecause 3 ^{2.465} =	=15	
			Log	garithmic	Graphs	
	A powerful too logarithmic gra If you plot an e semilogarithmi (meaning graph scale on one ax a straight line. The graph at th Notice where the the graph:	ph paper xponenti c ("semi- n paper t tis but no ne right is	to solve al function log") grate hat has a but the oth the function	e equations. on on oph paper a logarithmic her), you get ction $y = 2^x$.	50 40 30 20 10 9 8 7	
	1	Domain 0	Range 1		6 5	
	-	1	2		4	
		2	4		3	
		3	8			
		4	16		2	
		5	32			
	Notice also that intermediate va	-				
	the graph show		-	ie, al x – 2.0,] 5
		,				

-

Big Ideas	LogarithmsPage: 34DetailsUnit: Laboratory & Mathematics
	Natural Logarithms
	The natural logarithm comes from calculus—it is the solution to the problem:
	$\int \frac{1}{x} dx = \log_e(x)$
	where the base of this logarithm, " <i>e</i> ," is a constant (sometimes called "Euler's number") that is an irrational number equal to approximately 2.71828 18284 59045
	The natural logarithm is denoted "In", so we would actually write:
	$\int \frac{1}{x} dx = \ln(x)$
	The number "e" is often called the exponential function. In an algebra-based physics class, the exponential function appears in some equations whose derivations come from calculus, notably some of the equations relating to resistor-capacitor (RC) circuits.
	Finally, just as:
	$\log(10^{x}) = x$ and $10^{\log(x)} = x$
	it is similarly true that:
	$\ln(e^x) = x$ and $e^{\ln(x)} = x$

Details

Introduction: Thermal Physics (Heat)

Unit: Thermal Physics (Heat)

Topics covered in this chapter:

Heat & Temperature	39
Heat Transfer	43
Specific Heat Capacity & Calorimetry	51
Phase Diagrams	58
Phases & Phase Changes	63
Heating Curves	67
Thermal Expansion	75

This chapter is about heat as a form of energy and the ways in which heat affects objects, including how it is stored and how it is transferred from one object to another.

- *Heat & Temperature* describes the concept of heat as a form of energy and how heat energy is different from temperature.
- *Heat Transfer* describes how to calculate the rate of the transfer of heat energy from one object to another.
- Specific Heat Capacity & Calorimetry describes different substances' and objects' abilities to store heat energy.
- *Phase Diagrams* describes how to use a phase diagram to determine the state of matter of a substance at a given temperature and pressure.
- *Phases & Phase Changes* and *Heating Curves* addresses the additional calculations that apply when a substance goes through a phase change (such as melting or boiling).
- *Thermal Expansion* describes the calculation of the change in size of an object caused by heating or cooling.

New challenges specific to this chapter include looking up and working with constants that are different for different substances.

Big Ideas	Details Unit: Thermal Physics (Heat)
	Standards addressed in this chapter:
	NGSS Standards/MA Curriculum Frameworks (2016):
	HS-PS2-6. Communicate scientific and technical information about why the molecular-level structure is important in the functioning of designed materials.
	HS-PS3-1. Create a computational model to calculate the change in the energy of one component in a system when the change in energy of the other component(s) and energy flows in and out of the system are known.
	HS-PS3-2. Develop and use models to illustrate that energy at the macroscopic scale can be accounted for as either motions of particles or energy stored in fields.
	HS-PS3-4. Plan and conduct an investigation to provide evidence that the transfer of thermal energy when two components of different temperature are combined within a closed system results in a more uniform energy distribution among the components in the system (second law of thermodynamics).
AP [®] only	AP [®] Physics 2 Learning Objectives/Essential Knowledge (2024):
	9.1.B : Describe the temperature of a system in terms of the atomic motion within that system.
	9.1.B.1 : The temperature of a system is characterized by the average kinetic energy of the atoms within that system.
	9.1.B.1.i : The Maxwell–Boltzmann distribution provides a graphical representation of the energies and speeds of atoms at a given temperature.
	9.1.B.1.ii : The root-mean-square speed corresponding to the average kinetic energy for a particle of an ideal gas is related to the temperature of the gas by $K_{avg} = \frac{3}{2}k_{B}T = \frac{1}{2}mv_{rms}^{2}$
	9.3.A : Describe the transfer of energy between two systems in thermal contact due to temperature differences of those two systems.
	9.3.A.1 : Two systems are in thermal contact if the systems may transfer energy by thermal processes.
	9.3.A.1.i : Heating is the transfer of energy into a system by thermal processes.
	9.3.A.1.ii : Cooling is the transfer of energy out of a system by thermal processes.

Introduction: Thermal Physics (Heat)

Dialdeas	Details Page: 37
Big Ideas	Details Unit: Thermal Physics (Heat)
AP [®] only	9.3.A.2 : The thermal processes by which energy may be transferred between systems at different temperatures are conduction, convection, and radiation.
	9.3.A.3 : Energy is transferred through thermal processes spontaneously from a higher-temperature system to a lower-temperature system.
	9.3.A.3.i: In collisions between atoms from different systems, energy is most likely to be transferred from higher-energy atoms to lower-energy atoms.
	9.3.A.3.ii: After many collisions of atoms from different systems, the most probable state is one in which both systems have the same temperature.
	9.3.A.4 : Thermal equilibrium results when no net energy is transferred by thermal processes between two systems in thermal contact with each other.
	9.5.A : Describe the energy required to change the temperature of an object by a certain amount.
	9.5.A.1 : The amount of energy required to change the temperature of a material is related to the material's specific heat capacity.
	9.5.A.2 : The specific heat capacity of a material is an intrinsic property of that material that depends on the arrangement and interactions of the atoms that make up the material.
	9.5.B : Describe the rate at which energy is transferred by conduction through a given material.
	9.5.B.1 : The rate at which energy is transferred by conduction through a given material is related to the thermal conductivity, the physical dimensions of the material, and the temperature difference across the material.
	9.5.B.2 : The thermal conductivity of a material is an intrinsic property of that material that depends on the arrangement and interactions of the atoms that make up the material.
	15.4.A : Describe the electromagnetic radiation emitted by an object due to its temperature.
	15.4.A.1 : Matter will spontaneously convert some of its internal thermal energy into electromagnetic energy.
	15.4.A.2: A blackbody is an idealized model of matter that absorbs all radiation that falls on the body. If the body is in equilibrium at a constant temperature, then it must in turn emit energy.

Introduction: Thermal Physics (Heat)

	Introduction: Thermal Physics (Heat) Page: 38
Big Ideas	Details Unit: Thermal Physics (Heat)
AP® only	15.4.A.3: A blackbody will emit a continuous spectrum that only depends on the body's temperature. The radiation emitted by a blackbody is often modeled by plotting intensity per unit wavelength as a function of wavelength.
	15.4.A.3.i: The distribution of the intensity of a blackbody's spectrum as a function of temperature cannot be modeled using only classical physics concepts. A blackbody's spectrum is described by Planck's law, which assumes that the energy of light is quantized.
	15.4.A.3.ii: The peak wavelength emitted by a blackbody (the wavelength at which the blackbody emits the greatest amount of radiation per unit wavelength) decreases with increasing temperature, as described by Wien's law.
	15.4.A.3.iii: The rate at which energy is emitted (power) by a blackbody is proportional to the surface area of the body and to the temperature of the body raised to the fourth power, as described by the Stefan-Boltzmann law.
	Skills learned & applied in this chapter:
	 Working with material-specific constants from a table.
	• Working with more than one instance of the same quantity in a problem.
	 Combining equations and graphs.
	L

Heat & Temperature

Unit: Thermal Physics (Heat)

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS3-1, HS-PS3-2, HS-PS4-3a

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 9.1.B, 9.1.B.1, ,

9.1.B.1.i, 9.1.B.1.ii

Mastery Objective(s): (Students will be able to...)

• Explain heat energy in macroscopic and microscopic terms.

Success Criteria:

Details

Big Ideas

• Descriptions & explanations account for observed behavior.

Language Objectives:

• Explain the difference between heat and temperature.

Tier 2 Vocabulary: heat, temperature

Labs, Activities & Demonstrations:

- Heat a small weight and large weight to slightly different temperatures.
- Fire syringe.
- Steam engine.
- Incandescent light bulb in water.
- Mixing (via molecular motion/convection) of hot *vs.* cold water (with food coloring).

Vocabulary:

<u>heat</u>: energy that can be transferred by moving atoms or molecules via transfer of momentum.

<u>temperature</u>: a measure of the average kinetic energy of the particles (atoms or molecules) of a system.

<u>thermometer</u>: a device that measures temperature, most often via thermal expansion and contraction of a liquid or solid.

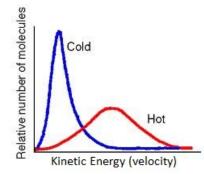
Notes:

Heat is energy that is stored as the translational kinetic energy of the particles that make up an object or substance.

Heat & Temperature

As you (should) recall from chemistry, particles (atoms or molecules) are always moving (even at absolute zero), and that energy can transfer via elastic collisions between the particles of one object or substance and the particles of another. (We will explore these concepts in more detail in the topic *Kinetic-Molecular Theory*, starting on page 88.)

Note that heat is the energy itself, whereas temperature is a measure of the quality of the heat—the average of the kinetic energies of the individual molecules:



Note that the particles of a substance have a range of kinetic energies, and the temperature is the average. Notice that when a substance is heated, the particles acquire a wider range of kinetic energies, with a higher average.

When objects are placed in contact, heat is transferred from each object to the other via the transfer of momentum that occurs when the individual molecules collide. Molecules that have more energy transfer more energy than they receive. Molecules that have less energy receive more energy than they transfer. This means three things:

- 1. Individual collisions transfer energy in both directions. The particles of a hot substance transfer energy to the cold substance, but the particles of the cold substance also transfer energy to the hot substance.
- 2. The net (overall) flow of energy is from objects with a higher temperature (more kinetic energy) to objects with a lower temperature (less kinetic energy). *I.e.,* more energy is transferred from the hot substance to the cold substance than *vice versa*.
- 3. If you wait long enough, all of the molecules will have the same temperature (*i.e.*, the same average kinetic energy).

Big Ideas

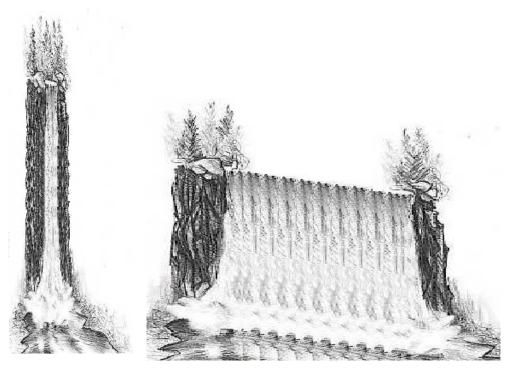
Details

Heat & Temperature

This means that the *temperature* of one object relative to another determines which direction the heat will flow, much like the way the elevation (vertical position) of one location relative to another determines which direction water will flow.

However, the total heat (energy) contained in an object depends on the mass as well as the temperature, in the same way that the total change in energy of the water going over a waterfall depends on the mass of the water as well as the height.

Consider two waterfalls, one of which is twice the height of the second, but the second of which has ten times as much water going over it as the first:



 $\Delta U = mg(2h)$

Big Ideas

Details

 $\Delta U = (10m)gh$

In the above pictures, each drop of water falling from the waterfall on the left has more gravitational potential energy, but more total energy goes over the waterfall on the right.

Similarly, each particle in an object at a higher temperature has more thermal energy than each particle in another object at a lower temperature.

If we built a waterway between the two falls, water could flow from the top of the first waterfall to the top of the second, but not *vice versa*.

Similarly, the net flow of heat is from a smaller object with higher temperature to a larger object with a lower temperature, but not *vice versa*.

system: the region or collection of objects under being considered in a problem.

surroundings: everything that is outside of the system.

Details

Big Ideas

E.g., if a metal block is heated, we would most likely define the <u>system</u> to be the block, and the <u>surroundings</u> to be everything else.

We generally use the variable Q to represent heat in physics equations.

Heat flow is always represented in relation to the system.

Heat Flow	Sign of Q	System	Surroundings
from the surroundings	+ (positive)	gains heat (gets	lose heat
into the system		warmer)	(get colder)
from the system	– (negative)	loses heat (gets	gain heat
out to the surroundings		colder)	(get hotter)

A positive value of Q means heat is flowing <u>into</u> the system. Because the heat is transferred from the molecules outside the system to the molecules in the system, the energy of the system increases, and the energy of the surroundings decreases.

A negative value of Q means heat is flowing <u>out of</u> the system. Because the heat is transferred from the molecules in the system to the molecules outside the system, the energy of the system decreases, and the energy of the surroundings increases.

This can be confusing. Suppose you set a glass of ice water on a table. When you pick up the glass, your hand gets colder because heat is flowing from your hand (which is part of the surroundings) into the system (the glass of ice water). This means the system (the glass of ice water) is gaining heat, and the surroundings (your hand, the table, *etc.*) are losing heat. The value of *Q* would be positive in this example.

In simple terms, you need to remember that your hand is part of the *surroundings*, not part of the system.

<u>thermal equilibrium</u>: when all of the particles in a system have the same average kinetic energy (temperature). When a system is at thermal equilibrium, no net heat is transferred. (*I.e.,* collisions between particles may still transfer energy, but the average temperature of the particles in the system—what we measure with a thermometer—is not changing.)

	Heat Transfer Page:
eas	Details Unit: Thermal Physics (He
	Heat Transfer
	Unit: Thermal Physics (Heat)
	NGSS Standards/MA Curriculum Frameworks (2016): HS-PS3-4a
	AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 9.3.A, 9.3.A.1, 9.3.A.1.i, 9.3.A.1.ii, 9.3.A.2, 9.3.A.3, 15.4.A, 15.4.A.1, 15.4.A.2, 15.4.A.3, 15.4.A.3.i, 15.4.A.3.ii, 15.4.A.3.iii
	Mastery Objective(s): (Students will be able to)
	• Explain heat transfer by conduction, convection and radiation.
	 Calculate heat transfer using Fourier's Law of Heat Conduction.
	Success Criteria:
	 Descriptions & explanations account for observed behavior.
	• Variables are correctly identified and substituted correctly into the correct equations.
	 Algebra is correct and rounding to appropriate number of significant figures reasonable.
	Language Objectives:
	 Explain the mechanisms by which heat is transferred.
	Tier 2 Vocabulary: conduction, radiation
	Labs, Activities & Demonstrations:
	Radiometer & heat lamp.
	Almond & cheese stick.
	• Flammable soap bubbles.
	• Drop of food coloring in water vs. ice water
	Notes:
	Heat transfer is the flow of heat energy from one object to another. Heat transfer usually occurs through three distinct mechanisms: conduction, radiation, and convection.
	<u>conduction</u> : transfer of heat through collisions of particles by objects that are <u>in</u> <u>direct contact</u> with each other. Conduction occurs when there is a net transfe of momentum from the molecules of an object with a higher temperature transfer to the molecules of an object with a lower temperature.
	<u>thermal conductivity</u> (<i>k</i>): a measure of the amount of heat that a given length of a substance can conduct in a specific amount of time. Thermal conductivity is
	measured in units of $\frac{J}{ms \cdot c}$ or $\frac{W}{m \cdot c}$.

Heat Transfer

<u>conductor</u>: an object that allows heat to pass through itself easily; an object with high thermal conductivity.

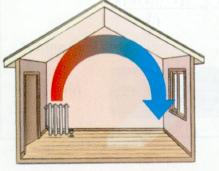
<u>insulator</u>: an object that does not allow heat to pass through itself easily; a poor conductor of heat; an object with low thermal conductivity.

<u>radiation</u>: transfer of heat <u>through space</u> via electromagnetic waves (light, microwaves, *etc.*)

<u>convection</u>: transfer of heat <u>by motion of particles</u> that have a higher temperature exchanging places with particles that have a lower temperature. Convection usually occurs when air moves around a room.

Natural convection occurs when particles move because of differences in density. In a heated room, because cool air is more dense than warm air, the force of gravity is stronger on the cool air, and it is pulled harder toward the ground than the warm air. The cool air displaces the warm air, pushing it upwards out of the way.

In a room with a radiator, the radiator heats the air, which causes it to expand and be displaced upward by the cool air nearby. When the (less dense) warm air reaches the ceiling, it spreads out, and it continues to cool as it spreads. When the air reaches the opposite wall, it is forced downward toward the floor, across the floor, and back to the radiator.

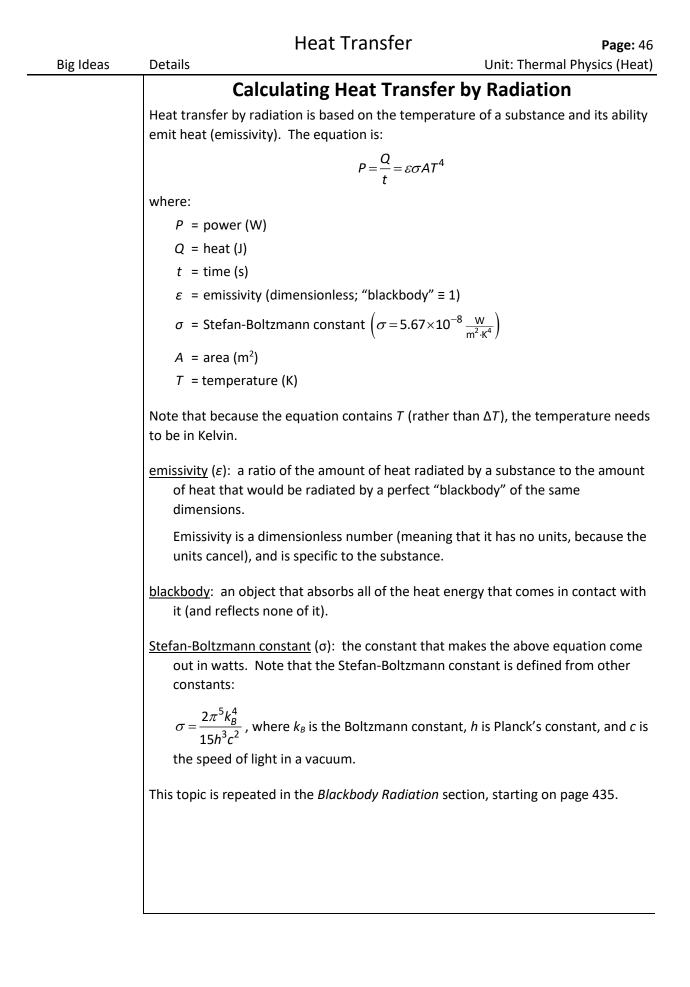


<u>Forced convection</u> can be achieved by moving heated or cooled air using a fan.
 Examples of this include ceiling fans and convection ovens. If your radiator does not warm your room enough in winter, you can use a fan to speed up the process of convection. (Make sure the fan is moving the air in the same direction that would happen from natural convection. Otherwise, the fan will be fighting against physics!)

Big Ideas

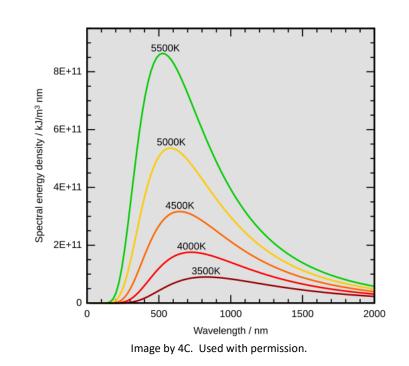
Details

Ideas Det	ails	Unit: Thermal Physics (Hea
	Calculating Heat Transfer by	Conduction
Неа	t transfer by conduction can be calculated using Fo	
Con	duction:	
	$P = \frac{Q}{t} = \pm kA \frac{\Delta T}{L}$	
whe	ι _	
	P = power(W)	
	Q = heat transferred (J) t = time (s)	T_1 A T_2
	$k = \text{coefficient of thermal conductivity } \left(\frac{W}{\text{m}^{\circ}\text{C}}\right)$	
	A = cross-sectional area (m2)	
	ΔT = temperature difference (K or °C)	
	L = length(m)	
	± sign means that the value can be positive or neg	-
is ch	nosen based on whether the heat transfers into (+)	or out of (–) the system.
	e that for insulation (the kind you have in the walls	
	It the lowest possible thermal conductivity—you do duct the heat from the inside of your house to the	
	ple think that bigger numbers are better, the indus	
	effectiveness of insulation called the "R value". It	
$\frac{k}{L}$,	which means lower conductivity and more thicknes	ss gives better insulation.
San	nple Problem:	
	A piece of brass is 5.0 mm (0.0050 m) thick and ha 0.010 m ² . If the temperature on one side of the m temperature on the other side is 25°C, how much through the metal in 30. s? The coefficient of ther is $120 \frac{W}{m^{\circ}C}$.	etal is 65°C and the heat will be conducted
A:	$\frac{Q}{t} = kA \frac{\Delta T}{L}$	
	$\frac{Q}{30} = (120)(0.010) \left(\frac{65 - 25}{0.0050}\right) = 9600$	
	Q = 288000 J = 288 kJ	
	(Note that because the quantities of heat that we values are often given in kilojoules or megajoules i	
	values are orten given in knojoules of megajoules i	naceuu or jourea.j



Wien's Displacement Law

In 1893, German physicist Wilhelm Wien discovered that radiation from a blackbody occurs in the form of electromagnetic radiation, over a range of wavelengths. The wavelength at which the maximum energy is radiated decreases as the temperature increases:



The wavelength of maximum radiation is described by the equation:

$$\lambda_{max} = \frac{b}{T}$$

where:

 $\lambda_{max} =$ wavelength of maximum radiated energy

b = Wien's displacement constant $= 2.897771955 \times 10^{-3} \text{m} \cdot \text{K}$

T = temperature (K)

Heat Transfer

Big Ideas	Details Unit: Thermal Physics (Heat)
honors (not AP®)	Wien's displacement law was superseded in 1900, when German physicist Max Planck derived a more general equation, now called Planck's radiation law. This law gives an equation for the spectral energy density (energy per unit volume per unit frequency):
	$u_{v}(f,T) = \frac{8\pi h f^{3}}{c^{3}} \cdot \frac{1}{e^{\binom{h f_{k_{B}T}}{k_{B}T}} - 1}$
	where:
	$u_{\nu}(f,T) =$ spectral energy density (a function of frequency & temperature) h = Planck's constant = 6.626 070 15 × 10 ⁻³⁴ J·s
	f = frequency (Hz)
	$c =$ speed of light in a vacuum $= 2.99792458 \frac{\text{m}}{\text{s}}$
	$k_{B} = \text{Boltzmann constant} = 1.380649 \times 10^{-23} \frac{\text{J}}{\text{K}}$
	T = temperature (K)

Heat Transferpage: 49Big IdeasDetailsUnit: Thermal Physics (Heat)Immediate the state of thermal conductivity in Table K. Thermal
Properties of Selected Materials on page 504 of your reference tables.1. (5) The surface of a hot plate is made of 12.0 mm (0.012 m) thick aluminum
and has an area of 64 cm² (which equals 0.0064 m²). If the heating coils
maintain a temperature of 80.°C underneath the surface and the air
temperature is 22°C, how much heat can be transferred through the plate in
60. s?Answer: 464 000 J° or 464 kl2. (5) A cast iron frying pan is 5.0 mm thick. If it contains boiling water
(100°C), how much heat will be transferred into your hand if you place your
hand against the bottom for two seconds?
(Assume your hand has an area of 0.0040 m², and that body temperature is
37°C.)Answer: +8 064 J or +8.064 kl
(positive because the direction is stated as "Into your hand")3. (M) A plate of metal has thermal conductivity k and thickness L. One side
has a temperature of T, and the other side has a temperature of T, derive
an expression for the cross-sectional area A that would be needed in order
to transfer a certain amount of heat, Q, through the plate in time t.Answer:
$$A = \frac{QL}{kt(T_b - T_c)}$$
* Note: Questions #1 and #3 do not specify the direction of heat transfer, so the answer could be either
positive or negative.

		Heat Transfer	Page: 50
Big Ideas	Details		Unit: Thermal Physics (Heat)
	4.	(M) A glass window in a house has an area of	
		2.4 mm (2.4 $\times 10^{^{-3}}$ m) . The temperature inside	e the house is 21 °C, and the
		outside temperature is 0 °C.	
		a. (M) How much heat is lost through the due to conduction?	e window in 1 hour (3600 s)
		Use 1.0 W for the thermal conductivi	ity of the glass.
		Answer: $-21\ 100\ 000\ J = -21\ 100\ kJ$	through the using and)
		(negative because heat is <u>lost</u>	through the window)
		b. (M – honors; A – AP®) How much hea	t is lost through the window in
		1 hour (3600 s) due to radiation? (Assu	ume the temperature of the
		entire glass is 21 °C for this problem.)	
		Hint: Remember to convert the temper	ature to Kelvin.
		Answer: $-940\ 000\ J = -940\ kJ$	
		(negative because heat is <u>lost</u>	through the window)
		a (M. honowa A. AD®) Which mode a	f haat transfor (conduction us
		c. (M – honors; A – AP [®]) Which mode or radiation) accounts for the greater and	

Specific Heat Capacity^{*} & Calorimetry⁺

Unit: Thermal Physics (Heat)

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS3-1, HS-PS4-3a

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): 9.5.A, 9.5.A.1, 9.5.A.2

Mastery Objective(s): (Students will be able to ...)

- Calculate the heat transferred when an object with a known specific heat capacity is heated.
- Perform calculations related to calorimetry.
- Describe what is happening at the molecular level when a system is in thermal equilibrium.

Success Criteria:

- Variables are correctly identified and substituted correctly into the correct equations.
- Algebra is correct and rounding to appropriate number of significant figures is reasonable.

Language Objectives:

- Explain what the specific heat capacity of a substance measures.
- Explain how heat is transferred between one substance and another.

Tier 2 Vocabulary: heat, specific heat capacity, "coffee cup" calorimeter

Labs, Activities & Demonstrations:

• Calorimetry lab.

Notes:

Different objects have different abilities to hold heat. For example, if you enjoy pizza, you may have noticed that the sauce holds much more heat (and burns your mouth much more readily) than the cheese or the crust.

The amount of heat that a given mass of a substance can hold is based on its specific heat capacity.

^{*} Physicists call this quantity "specific heat". Chemists call it "heat capacity". The term "specific heat capacity" is used so that physicists and chemists can talk to one another and realize that they are discussing the same concept.

⁺ Calorimetry is usually taught in chemistry. However, the topic was moved from chemistry to physics in the Massachusetts Curriculum Frameworks starting in 2016.

Specific Heat Capacity & Calorimetry

specific heat capac	ity (C): a measure of the amount of heat required per gram of a
substance to p	roduce a specific temperature change in the substance.

- C_p : specific heat capacity, measured at constant pressure. For gases, this means the measurement was taken while allowing the gas to expand as it was heated.
- C_{v} : specific heat capacity, measured at constant volume. For gases, this means the measurement was made in a sealed container, allowing the pressure to rise as the gas was heated.

For solids and liquids, $C_p \approx C_v$ because the pressure and volume change very little with heating. For gases, $C_p > C_v$ (always). For ideal gases, $C_p - C_v = R$, where R is a constant known as "the gas constant."

When there is a choice, C_p is more commonly used than C_v because it is easier to measure. When dealing with solids and liquids, most physicists just use C for specific heat capacity and don't worry about the distinction.

Calculating Heat from a Temperature Change

The amount of heat gained or lost when an object changes temperature is given by the equation:

$$Q = mC\Delta T = m\int_{T_1}^{T_2} C(T)dT$$

where:

Big Ideas

Details

Q = heat (J or kJ) m = mass (g or kg) $C = specific heat capacity (usually \frac{kJ}{kg \cdot K} = \frac{J}{g \cdot K})$ C(T) = specific heat capacity as a function of temperature $\Delta T = temperature change (K \text{ or } ^{\circ}C)^{*}$

Because problems involving heat often involve large amounts of energy, heat is often expressed in kilojoules (kJ) rather than joules.

Note that
$$1\frac{kJ}{kg\cdot K} \equiv 1\frac{kJ}{kg\cdot ^{\circ}C} \equiv 1\frac{J}{g\cdot ^{\circ}C}$$
 and $1\frac{cal}{g\cdot ^{\circ}C} \equiv 1\frac{kcal}{kg\cdot ^{\circ}C} = 4.18\frac{J}{g\cdot ^{\circ}C} = 4.18\frac{kJ}{kg\cdot K}$

You need to be careful with the units. If the mass is given in kilograms (kg), your specific heat capacity will have units of $\frac{kJ}{kg.^{\circ}C}$ and the heat energy will come out in kilojoules (kJ). If mass is given in grams, you will use units of $\frac{J}{g.^{\circ}C}$ and the heat energy will come out in joules (J).

^{*} Because 1 K is the same size as 1 °C, the two units are equivalent for ΔT values. Note, however, that T in equations must be in kelvin, because a temperature of 0 in an equation must mean absolute zero.

Specific Heat Capacities of Some Substances

Substance	Specific Heat Capacity (^{kJ} / _{kg·K})	Substance	Specific Heat Capacity (^{kJ} / _{kg·K})
water at 20°C	4.181	aluminum	0.897
ethylene glycol	2.460	glass	0.84
(anti-freeze)		iron	0.450
ice at −10 °C	2.080	copper	0.385
steam at 100 °C	2.11	brass	0.380
steam at 130 °C	1.99	silver	0.233
vegetable oil	2.00	lead	0.160
air	1.012	gold	0.129

Calorimetry

calorimetry: the measurement of heat flow

In a calorimetry experiment, heat flow is calculated by measuring the mass and temperature change of an object and applying the specific heat capacity equation.

calorimeter: an insulated container for performing calorimetry experiments.

<u>coffee cup calorimeter</u>: a calorimeter that is only an insulated container—it does not include a thermal mass (such as a mass of water). It is usually made of Styrofoam, and often resembles a coffee cup.

<u>bomb calorimeter</u>: a calorimeter for measuring the heat produced by a chemical reaction. A bomb calorimeter is a double-walled metal container with water between the layers of metal. The heat from the chemical reaction causes the temperature of the water to increase. Because the mass and specific heat capacity of the calorimeter (water plus metal) are known, the heat produced by the reaction can be calculated from the increase in temperature of the water.

It has a great name, but a bomb calorimeter doesn't involve actually blowing anything up. $\textcircled{\mbox{$\odot$}}$

Big Ideas	Details Unit: Thermal Physics (Heat)
	Solving Coffee Cup Calorimetry Problems
	Most coffee cup calorimetry problems involve placing a hot object in contact with a colder one. Many of them involve placing a hot piece of metal into cold water.
	To solve the problems, assume that both objects end up at the same temperature.
	If we decide that heat gained (going into a substance) by each object that is getting hotter is positive, and heat lost (coming out of a substance) by every substance that is getting colder is negative, then the basic equation is:
	Heat Lost + Heat Gained = Change in Thermal Energy $\sum Q_{lost} + \sum Q_{gained} = \Delta Q$
	If the calorimeter is insulated, then no heat is gained or lost by the entire system, which means $\Delta Q = 0$. This is often represented as $-\sum Q_{lost} = \sum Q_{gained}$
	If we have two substances (#1 and #2), one of which is getting hotter and the other of which is getting colder, then our equation becomes:
	Heat Lost + Heat Gained = Change in Thermal Energy $\sum Q_{lost} + \sum Q_{gained} = \Delta Q = 0$ $m_1 C_1 \Delta T_1 + m_2 C_2 \Delta T_2 = 0$
	In this example, ΔT_1 would be negative and ΔT_2 would be positive.
	To solve a calorimetry problem, there are six quantities that you need: the two masses, the two specific heat capacities, and the two temperature changes. (You might be given initial and final temperatures for either or both, in which case you'll need to subtract. Remember that if the temperature increases, ΔT is positive, and if the temperature decreases, ΔT is negative.) The problem will usually give you all but one of these and you will need to find the missing one.
	If you need to find the final temperature, use $\Delta T = T_f - T_i$ on each side. You will have both T_i numbers, so the only variable left will be T_f . (The algebra is straightforward, but ugly.)

Specific Heat Capacity & Calorimetry Page: 55 Unit: Thermal Physics (Heat)

	Specific fleat Capacity & Calofiffetty Page: 55
Big Ideas	Details Unit: Thermal Physics (Heat)
	Sample Problems:
	Q: An 0.050 kg block of aluminum is heated and placed in a calorimeter containing
	0.100 kg of water at 20. °C. If the final temperature of the water was 30. °C, to
	what temperature was the aluminum heated?
	A: To solve the problem, we need to look up the specific heat capacities for aluminum and water in <i>Table K. Thermal Properties of Selected Materials</i> on page 504 of your Physics Reference Tables. The specific heat capacity of aluminum is $0.898 \frac{J}{g^{-C}}$, and the specific heat capacity for water is $4.181 \frac{J}{g^{-C}}$.
	We also need to realize that we are looking for the initial temperature of the aluminum AT is always final initial which means $AT = 20$. T
	aluminum. ΔT is always final – initial , which means $\Delta T_{AI} = 30 - T_{i,AI}$. (Because
	the aluminum starts out at a higher temperature, this will give us a negative number, which is what we want.)
	$m_{\rm Al}C_{\rm Al}\Delta T_{\rm Al}$ + $m_{\rm w}C_{\rm w}\Delta T_{\rm w}$ =0
	$(0.050)(0.897)(30 - T_i) + (0.100)(4.181)(30 - 20) = 0$
	$0.0449(30 - T_i) + 4.181 = 0$
	$1.3455 - 0.0449T_i + 4.181 = 0$
	$5.5265 = 0.0449T_i$
	$T_i = \frac{5.5265}{0.0449} = 123.2 \text{°C}$
	 Q: An 0.025 kg block of copper at 95°C is dropped into a calorimeter containing 0.075 kg of water at 25°C. What is the final temperature?
	A: We solve this problem the same way. The specific heat capacity for copper is $0.385 \frac{J}{g^*C}$, and $\Delta T_{cu} = T_f - 95$ and $\Delta T_w = T_f - 25$. This means T_f will appear in two
	places. The algebra will be even uglier, but it's still a straightforward Algebra 1 problem:
	$m_{\rm Cu}C_{\rm Cu}\Delta T_{\rm Cu}$ + $m_{\rm w}C_{\rm w}\Delta T_{\rm w}$ = 0
	$(0.025)(0.385)(T_f - 95_i) + (0.075)(4.181)(T_f - 25) = 0$
	$0.009625(T_f - 95) + 0.3138(T_f - 25) = 0$
	$0.009625 T_f - (0.009625)(95) + 0.3136 T_f - (0.3138)(25) = 0$
	$0.009625 T_f - 0.9144 + 0.3138 T_f - 7.845 = 0$
	$0.3234 T_f = 8.759$
	$T_f = \frac{8.759}{0.3234} = 27 ^{\circ}\text{C}$

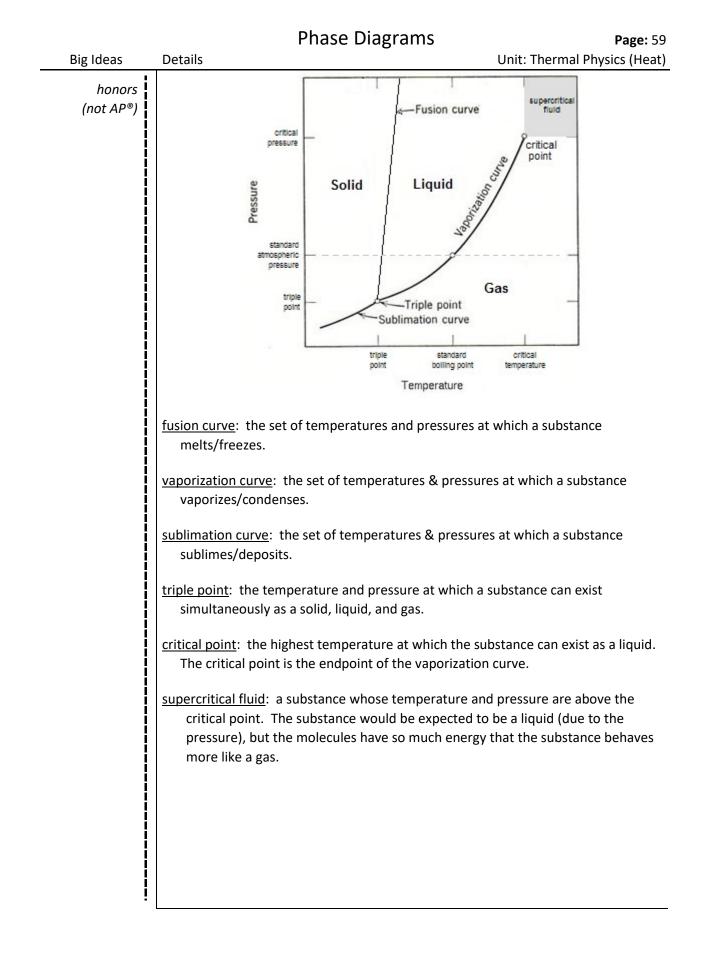
Specific Heat Capacity & Calorimetry Page: 56 Unit: Thermal Physics (Heat)

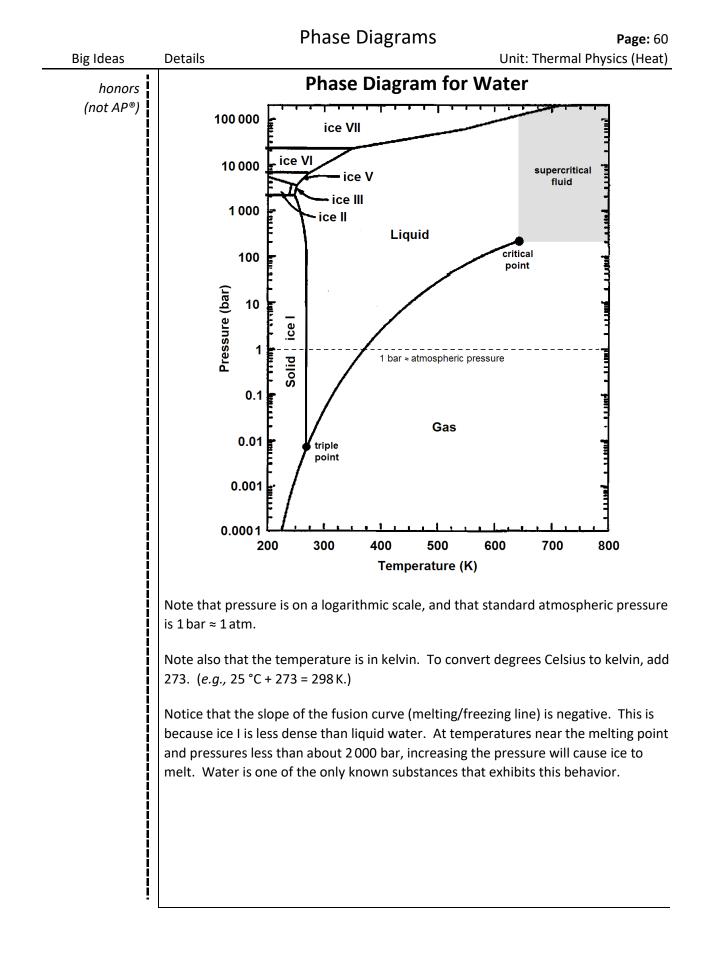
	Specific field Capacity & Calofifield y Page: 56					
Big Ideas	Details Unit: Thermal Physics (Heat)					
	Homework Problems					
	You will need to look up specific heat capacities in <i>Table K. Thermal Properties of Selected Materials</i> on page 504 of your Physics Reference Tables.					
	 (S) 375 kJ of heat is added to a 25.0 kg granite rock. If the temperature increases by 19.0 °C, what is the specific heat capacity of granite? 					
	Answer: 0.790 ^{kJ} / _{kg.°C}					
	2. (M) A 0.040 kg block of copper at 95 °C is placed in 0.105 kg of water at an unknown temperature. After equilibrium is reached, the final temperature is 24 °C. What was the initial temperature of the water?					
	Answer: 21.5 °C 3. (S) A sample of metal with a specific heat capacity of 0.50 $\frac{kJ}{kg^{+}C}$ is heated to 98 °C and then placed in an 0.055 kg sample of water at 22 °C. When equilibrium is reached, the final temperature is 35 °C. What was the mass of the metal?					
	Answer: 0.0948 kg					

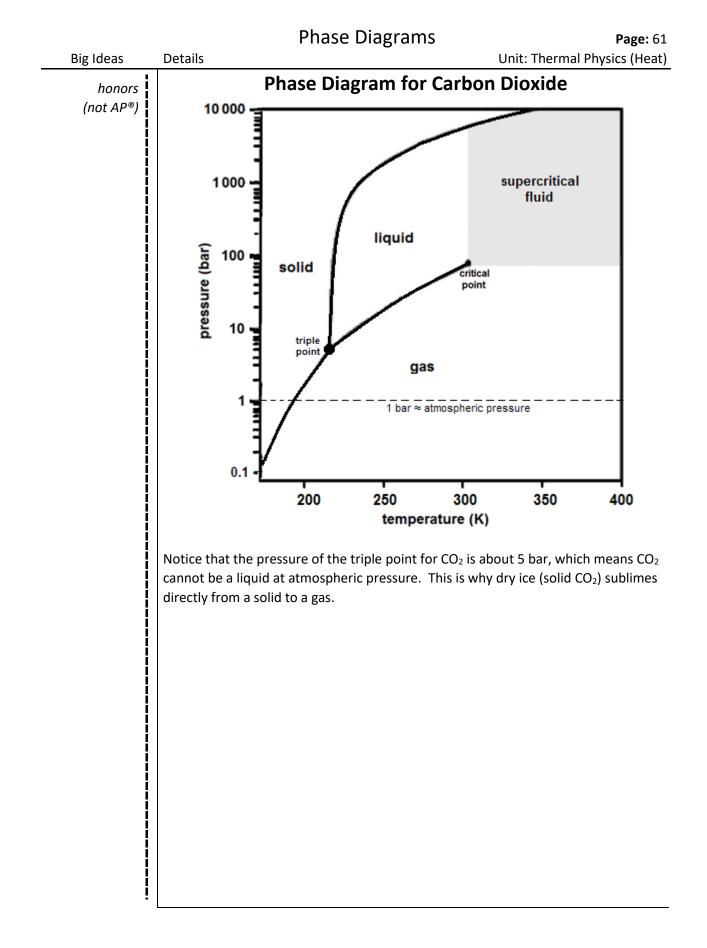
Specific Heat Capacity & Calorimetry

Big Ideas	Details	Unit: Thermal Physics (Heat)
	4.	(S) A 0.280 kg sample of a metal with a specific heat capacity of $0.430 \frac{kl}{kg^{\circ}C}$ is heated to 97.5 °C then placed in an 0.0452 kg sample of water at 31.2 °C. What is the final temperature of the metal and the water?
	5.	Answer: 57 °C (M) A sample of metal with mass m is heated to a temperature of T_m and placed into a mass of water M with temperature T_w . Once the system reaches equilibrium, the temperature of the water is T_f . Derive an expression for the specific heat capacity of the metal, C_m .
	6.	Answer: $C_m = \frac{MC_w(T_f - T_w)}{m(T_m - T_f)}$ (A) You want to do an experiment to measure the conversion of gravitational potential energy to kinetic energy to heat by dropping 2.0 kg of copper off the roof of LEHS, a height of 14 m. How much will the temperature of the copper increase? (<i>Hint: Remember that potential energy is measured in J but specific heat capacity problems usually use</i> kJ.)
		Answer: 0.36°C

	Thase Diagrams	1 4601 3				
Big Ideas	Details	Unit: Thermal Physics (Hea				
honors (not AP®)	Phase Diagrams [*]					
	Unit: Thermal Physics (Heat)					
	NGSS Standards/MA Curriculum Frameworks (2016)): HS-PS1-11(MA)				
	AP [®] Physics 2 Learning Objectives/Essential Knowle	dge (2024) : N/A				
ļ	Mastery Objective(s): (Students will be able to)					
	 Identify the phase of a substance at any combine pressure. 	nation of temperature and				
ļ	 Determine the melting and boiling points of a substance any pressure. 					
	Success Criteria:					
	 Phases are correctly identified as solid, liquid, g accordance with the temperature and pressure diagram. 					
	 Melting and boiling point temperatures are cor from its phase diagram for a given pressure. 	rrectly identified for a substand				
	 The effects of a pressure or temperature change sublime, etc.) are correctly explained based on 					
İ	Language Objectives:					
İ	• Explain the regions of a phase diagram and the	•				
İ	region and the temperature and pressure of the substance. Tier 2 Vocabulary: phase, curve, fusion, solid, liquid, gas, vapor					
į		0				
ļ	Notes:					
	The phase of a substance (solid, liquid, gas) depends pressure.	on its temperature and				
	phase diagram: a graph showing the phase(s) preser pressures.	nt at different temperatures ar				
	* Phase diagrams are usually taught in chemistry. However, they and heating curves, which were moved from chemistry to phys					







Phase Diagrams

Big Ideas	Details Unit: Thermal Physics (Heat)
honors	Homework Problems
(not AP®)	Answer these questions based on the phase diagrams for water and carbon dioxide on the previous pages.
	 (M) Approximately what pressure would be necessary to boil water at a temperature of 350 K?
	 (M) What is the minimum pressure necessary for water to exist as a liquid at 350 K?
	 (S) At approximately what temperature would water boil if the pressure is 10 bar?
	4. (S) What is the highest temperature at which carbon dioxide can exist as a liquid?
	5. (M) At 1.0 bar of pressure, what is the temperature at which carbon dioxide sublimes?
	6. (S) At room temperature (25 °C ≈ 300 K), what is the minimum pressure at which liquid carbon dioxide can exist?
	 (M) Describe the phase transitions and temperatures for water going from 200 K to 400 K at a pressure of 0.1 bar.
	8. (S) Describe the phase transitions and temperatures for carbon dioxide going 200 K to 300 K at a pressure of 10 bar.
!	

Big Ideas	Details Unit: Thermal Physics (Heat)					
honors	Phases & Phase Changes [*]					
(not AP®)	Unit: Thermal Physics (Heat)					
İ	NGSS Standards/MA Curriculum Frameworks (2016): HS-PS1-3, HS-PS2-8(MA)					
	AP [®] Physics 2 Learning Objectives/Essential Knowledge (2024): N/A					
	Mastery Objective(s): (Students will be able to)					
	 Compare observable states of matter and phase transitions with behavior at the molecular level. 					
	Success Criteria:					
	 Descriptions include connectedness and motion of molecules. 					
	 Descriptions include comparative descriptions of molecular speed. 					
	 Descriptions relate molecular motion and speed to temperature. 					
İ	Language Objectives:					
	 Explain phase changes in terms of changes in molecular behavior. 					
	Tier 2 Vocabulary: phase, solid, liquid, gas, vapor					
	Labe Activities & Demonstrations					
i	Labs, Activities & Demonstrations:					
	 evaporation from boiling water on cloth 					
	Notes:					
	macroscopic: objects or bulk properties of matter that we can observe directly.					
	microscopic: objects or properties of matter that are too small to observe directly.					
	Note that <i>macroscopic</i> properties of a substance are often determined by <i>microscopic</i> interactions between the individual molecules. ⁺					
	<u>phase</u> : a term that relates to how rigidly the atoms or molecules in a substance are connected.					
	<u>solid</u> : molecules are rigidly connected. A solid has a definite shape and a definite volume.					
	* Phase changes are generally taught in chemistry classes. However, because the calorimetry and heating curves topics were moved from chemistry to physics in the Massachusetts Curriculum Frameworks starting in 2016, it is useful to review them here.					
	[†] In this section, the term "molecules" is used to refer to the particles that make up a substance. In chemistry, a molecule is a group of atoms that are covalently bonded together, and a substance can be made of individual atoms, molecules, crystals, or other types of particles. In these notes, the term "particles" is preferred, but "molecules" is used in this section because it conjures the impression of particles that are attached or bonded together in some way. This gives most students a reasonably correct picture of entities that are firmly attached to each other and cannot be pulled apart by physical means.					

Phases & Phase Changes

Big Ideas	Details Unit: Thermal Physics (Heat)
honors (not AP®)	liquid: molecules are loosely connected; bonds are continuously forming and breaking. A liquid has a definite volume, but not a definite shape.
(NOLAP*)	gas: molecules are not connected. A gas has neither a definite shape nor a definite volume. Gases will expand to fill whatever space they occupy.
	plasma: the system has enough heat to remove electrons from atoms, which means the system is comprised of charged particles moving very rapidly.
	phase change: when an object or substance changes from one phase to another through gaining or losing heat.
	Breaking bonds requires energy. Forming bonds releases energy. This is true for the intermolecular bonds that hold a solid or liquid together as well as for chemical bonds.
	As you probably know from experience, you need to add energy to turn a solid to a liquid (melt it), or to turn a liquid to a gas (boil it).
	• This is why evaporation causes cooling—because the system (the water) needs to absorb heat from its surroundings in order to make the change from a liquid to a gas (vapor).
	• This is also why lids keep drinks hot. The lid is a barrier which significantly reduces the amount of evaporation.
	• When you perspire, the water absorbs heat from you in order to evaporate, which cools you off.
	It is less obvious that energy is released when a gas condenses or a liquid freezes.
	 Ice in your ice tray needs to give off heat in order to freeze. (Your freezer needs to remove that heat in order to make this happen.)
	• Burns from steam are much more dangerous than burns from water, because the steam releases a large amount of heat (which is absorbed by your body) as it condenses.
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Phases & Phase Changes

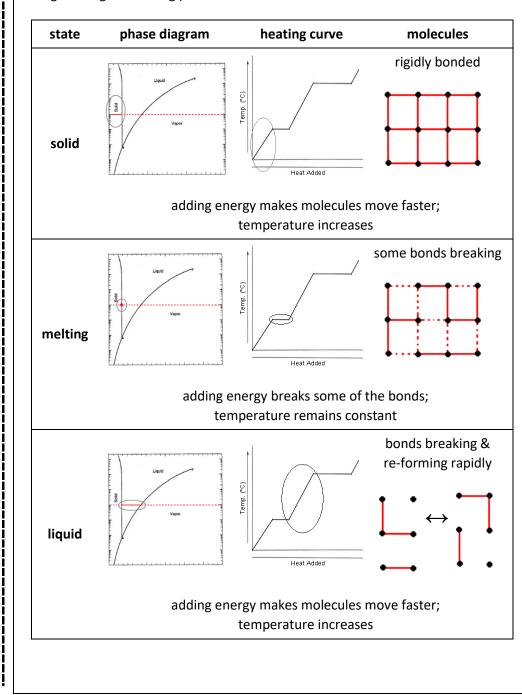
honors (not AP®)

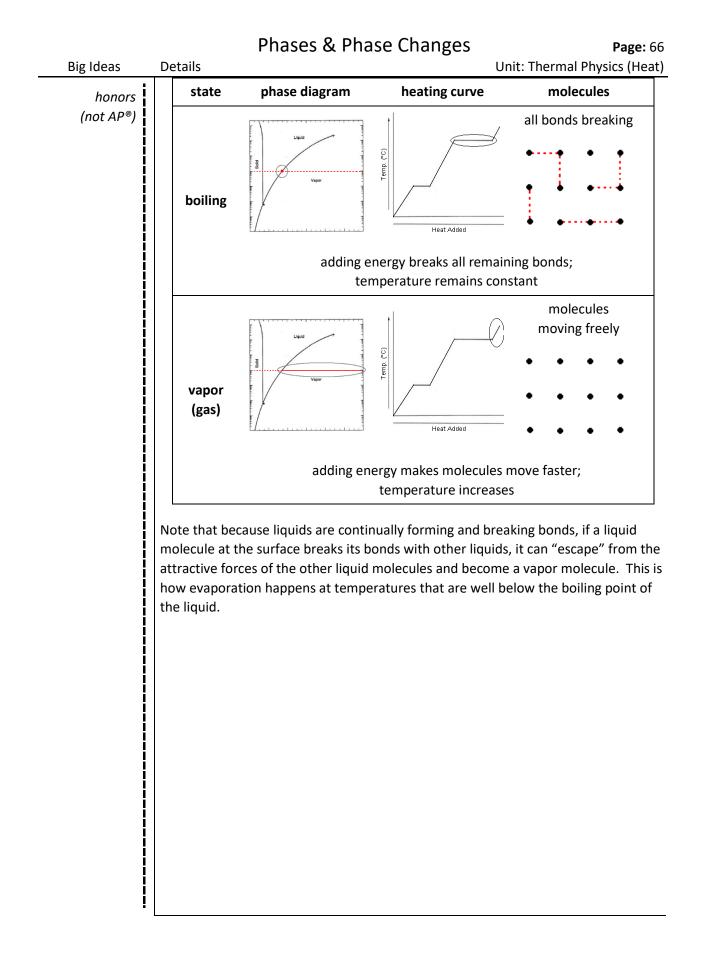
Details

Big Ideas

States of Matter

The following table shows interactions between the molecules and some observable properties for solids, liquids and gases. (The table includes heating curves, which will be discussed in more detail later in the next section, *Heating Curves* starting on page 67. For now, understand that a heating curve shows how the temperature changes as heat is added. Notice in particular that the temperature stays constant during melting and boiling.)





Big Ideas	Details Unit: Thermal Physics (Heat)
honors (not AP®)	Heating Curves [*]
	Unit: Thermal Physics (Heat)
	NGSS Standards/MA Curriculum Frameworks (2016): HS-PS3-1, HS-PS3-2, HS-PS3-4a
	AP [®] Physics 2 Learning Objectives/Essential Knowledge (2024): N/A Mastery Objective(s): (Students will be able to)
	 Determine the amount of heat required for all of the phase changes that occur over a given temperature range.
	Success Criteria:
	 Variables are correctly identified and substituted correctly into the correct equations.
	 Algebra is correct and rounding to appropriate number of significant figures is reasonable.
	Language Objectives:
ļ	 Explain what the heat is used for in each step of a heating curve. Tier 2 Vocabulary: specific heat capacity, curve, phase
	Labs, Activities & Demonstrations:
ļ	Evaporation from washcloth.
	• Fire & ice (latent heat of paraffin).
	Notes:
	<u>phase</u> : a term that relates to how rigidly the atoms or molecules in a substance are connected.
	solid: molecules are rigidly connected. A solid has a definite shape and volume.
	<u>liquid</u> : molecules are loosely connected; bonds are continuously forming and breaking. A liquid has a definite volume, but not a definite shape.
	gas: molecules are not connected. A gas has neither a definite shape nor a definite volume. Gases will expand to fill whatever space they occupy.
	plasma: the system has enough heat to remove electrons from atoms, which means the system is comprised of particles with rapidly changing charges.
	* Heating curves are usually taught in chemistry. However, the topic was moved from chemistry to physics in the Massachusetts Curriculum Frameworks starting in 2016.

honors
(not AP®)

Details

Big Ideas

<u>phase change</u>: when an object or substance changes from one phase to another through gaining or losing heat.

Breaking bonds requires energy. Forming bonds releases energy. This is true for the bonds that hold a solid or liquid together as well as for chemical bonds (regardless of what previous teachers may have told you!)

I.e., you need to add energy to turn a solid to a liquid (melt it), or to turn a liquid to a gas (boil it). Energy is released when a gas condenses or a liquid freezes. (*E.g.,* ice in your ice tray needs to give off heat in order to freeze. Your freezer needs to remove that heat in order to make this happen.)

The reason evaporation causes cooling is because the system (the water) needs to absorb heat from its surroundings (*e.g.*, your body) in order to make the change from a liquid to a gas (vapor). When the water absorbs heat from you and evaporates, you have less heat, which means you have cooled off.

Calculating the Heat of Phase Changes

<u>heat of fusion</u> (ΔH_{fus}) (sometimes called "latent heat" or "latent heat of fusion"): the amount of heat required to melt one kilogram of a substance. This is also the heat released when one kilogram of a liquid substance freezes. For example, the heat of fusion of water is $334 \frac{1}{g} = 334 \frac{kJ}{kg}$. The heat required to melt a sample

of water is therefore:

$$Q = m \Delta H_{fus} = m (334 \frac{J}{g})$$

<u>heat of vaporization</u> (ΔH_{vap}): the amount of heat required to vaporize (boil) one kilogram of a substance. This is also the heat released when one kilogram of a gas condenses. For example, the heat of vaporization of water is $2260 \frac{J}{g} \equiv 2260 \frac{kJ}{kg}$. The heat required to boil a sample of water is therefore:

$$Q = m \Delta H_{vap} = m (2260 \frac{J}{g})$$

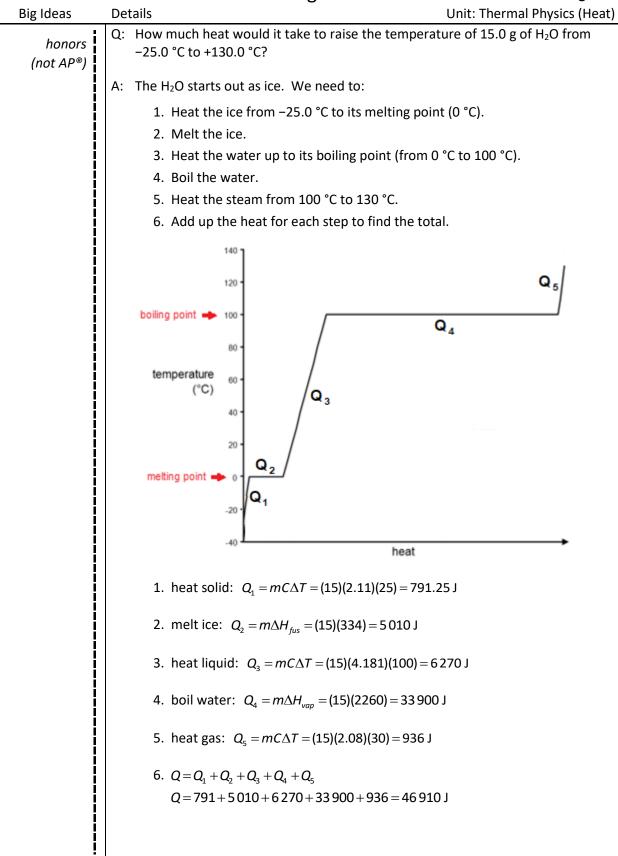
(Again, pay attention to the units. If your mass is in kg, you will need to use the units $\frac{kJ}{kg}$ for your ΔH values; if your mass is in g, you will need to use the units $\frac{J}{g}$ for your ΔH values.)

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Heating Curves Big Ideas Details Unit: Thermal Physics (Heat) heating curve: a graph of temperature vs. heat added. The following is a heating honors curve for water: (not AP®) 140 gas 120 boiling point 🛋 100 80 boiling temperature 60 (°C) liquid 40 melting 20 melting point 0 -20 solid 40 heat In the "solid" portion of the curve, the sample is solid water (ice). As heat is added, the temperature increases. The specific heat capacity of ice is $2.11 \frac{\text{kJ}}{\text{kg}^{\circ}\text{C}}$, so the heat required is: $Q_{solid} = mC\Delta T = m(2.11 \frac{kJ}{kg^{\circ}C})(\Delta T)$ In the "melting" portion of the curve, the sample is a mixture of ice and water. As heat is added, the ice melts, but the temperature remains at 0°C until all of the ice is melted. The heat of fusion of ice is $334 \frac{kJ}{kg}$, so the heat required is: $Q_{melt} = m \Delta H_{fus} = m(334 \frac{k}{kg})$ In the "liquid" portion of the curve, the sample is liquid water. As heat is added, the temperature increases. The specific heat capacity of liquid water is $4.18 \frac{kJ}{kg^{.0}C}$, so the heat required is: $Q_{liquid} = mC\Delta T = m(4.18 \frac{k}{kg^{\circ}C})(\Delta T)$ ļ

Big Ideas	Details Unit: Thermal Physics (Heat)					
honors (not AP®)	In the "boiling" portion of the curve, the sample is a mixture of water and water vapor (steam). As heat is added, the water boils, but the temperature remains at 100°C until all of the water has boiled. The heat of vaporization of water is 2260 $\frac{kl}{kg}$,					
	so the heat required is:					
	$Q_{boil} = m \Delta H_{vop} = m(2260 rac{\mathrm{kJ}}{\mathrm{kg}})$					
	In the "gas" portion of the curve, the sample is water vapor (steam). As heat is added, the temperature increases. The specific heat capacity of steam is approximately 2.08 $\frac{kJ}{kg^{\circ}C}$ (at 100°C; the specific heat capacity of steam decreases as					
ł	the temperature increases), so the heat required is:					
	$Q_{gas} = mC\Delta T = m(2.08 \frac{k}{kg^{\circ}C})(\Delta T)$					
	Steps for Solving Heating Curve Problems A heating curve problem is a problem in which a substance is heated across a temperature range that passes through the melting and/or boiling point of the substance, which means the problem includes heating or cooling steps and melting/freezing or boiling/condensing steps.					
	 Sketch the heating curve for the substance over the temperature range in question. Be sure to include the melting and boiling steps as well as the heating steps. 					
	2. From your sketch, determine whether the temperature range in the problem passes through the melting and/or boiling point of the substance.					
	3. Split the problem into:					
	a. Heating (or cooling) steps within each temperature range.					
Ì	b. Melting or boiling (or freezing or condensing) steps.					
	4. Find the heat required for each step.					
1	a. For the heating/cooling steps, use the equation $Q = mC \Delta T$.					
	b. For melting/freezing steps, use the equation $Q = m \Delta H_{fus}$.					
	c. For boiling/condensing steps, use the equation $Q = m \Delta H_{vap}$.					
	5. Add the values of Q from each step to find the total.					





Big Ideas	Details	Unit: Thermal Physics (Heat)						
honors								
(not AP [®]) For the following problems, use data from the fo					ne followir	ng table:		
		C (sol.)	M.P.	∆H _{fus}	C (liq)	B.P.	ΔH _{vap}	C _p (gas)
l		$\left(\frac{kJ}{kg \cdot C}\right)$	(°C)	$\left(\frac{kJ}{kg}\right)$	$\left(\frac{kJ}{kg \cdot C}\right)$	(°C)	$\left(\frac{kJ}{kg}\right)$	$\left(\frac{kJ}{kg \cdot C}\right)$
	water	2.11	0	334	4.18	100	2260	2.08*
	potassium	0.560	62	61.4	1.070	760	2025	0.671
	mercury	0.142	-39	11.3	0.140	357	293	0.104
	silver	0.217	962	111	0.318	2212	2360	—
	*Note that because increasing te		e change fron	n heating, the	specific heat	capacity of g	ases, C _p , incr	eases with
ł		0.0250 kg	samnle of	water is l	heated fro	00 _40 _	C to 150	°C
		_	-					
		etch the he nperature,	-		-			ure on the
	<i>y</i> -a	xis.						
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İ								
	h Cal	culato tho	haat raa	uired for e	ach stan (of the hea	ting curv	e, and the
		al heat rec	-		achstept			e, and the
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ļ	Ans	swer: 80.0	ΤKJ					
	<u> </u>							

 <i>honors</i> (<i>not AP</i>[®]) 2. (S) A 0.085 kg sample of mercury is heated from 25°C to 500. °C. a. Sketch the heating curve for the above process. Label the statemperature, melting point, boiling point, and final temperature, <i>y</i>-axis. 	
(not AP [®]) a. Sketch the heating curve for the above process. Label the statemperature, melting point, boiling point, and final temperature.	
b. Calculate the heat required for each step of the heating curve total heat required.	e, and the
Answer: 30.12 kJ	

Heating Curves

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Big Ideas	Details	Unit: Thermal Physics (Heat)
honors (not AP®)	3.	(S) A 0.045 kg block of silver at a temperature of 22°C is heated with 20.0 kJ of energy. You want to determine the final temperature and what the physical state (solid, liquid, gas) of the silver at that temperature.
		a. Sketch the heating curve for silver. Label the starting temperature, melting point, and boiling point on the y-axis.
		b. Calculate the total heat required by calculating the heat for each step until the entire 20.0 kJ is accounted for.
		Answers: liquid, 1369°C

Heating Curves

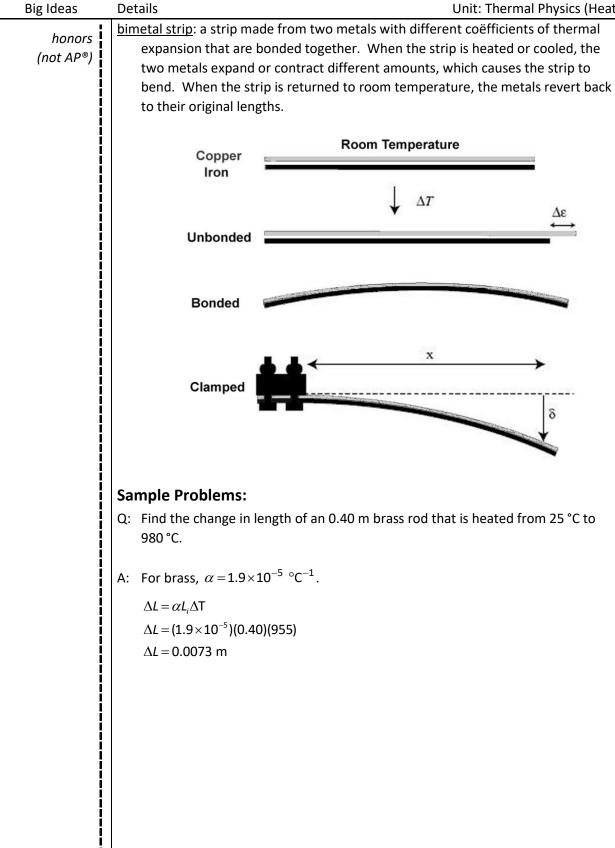
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Big Ideas	Details Unit: Thermal Physics (Heat)
honors	Thermal Expansion
(not AP®)	Unit: Thermal Physics (Heat)
i	NGSS Standards/MA Curriculum Frameworks (2016): N/A
ļ	AP [®] Physics 2 Learning Objectives/Essential Knowledge (2024): N/A
	Mastery Objective(s): (Students will be able to)
	 Calculate changes in length & volume for solids, liquids and gases that are undergoing thermal expansion or contraction.
1	Success Criteria:
	 Variables are correctly identified and substituted correctly into the correct equations.
	• Algebra is correct and rounding to appropriate number of significant figures is reasonable.
ł	Language Objectives:
i	• Explain what the heat is used for in each step of a heating curve.
ļ	Tier 2 Vocabulary: expand, contract
Ĩ	Labs, Activities & Demonstrations:
1	 Balloon with string & heat gun.
İ	• Brass ball & ring.
	• Bi-metal strip.
İ	Notes:
	expand: to become larger
	<u>contract</u> : to become smaller
	thermal expansion: an increase in the length and/or volume of an object caused by a change in temperature.
	When a substance is heated, the particles it is made of move farther and faster. This causes the particles to move farther apart, which causes the substance to expand.
	Solids tend to keep their shape when they expand. (Liquids and gases do not have a definite shape to begin with.)
	A few materials are known to contract with increasing temperature over specific temperature ranges. One well-known example is liquid water, which contracts as it heats from 0 °C to 4 °C. (Water expands as the temperature increases above 4 °C.)
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		inci	inui Expui			i age.		
Big Ideas	Details			-		al Physics (Hea		
honors	Thermal Expansion of Solids and Liquids							
(not AP®)	-	Thermal expansion is quantified in solids and liquids by defining a coëfficient of						
ļ	thermal expans	thermal expansion. The changes in length and volume are given by the equation:						
ļ			Length	: $\Delta L = \alpha L_i \Delta T$				
ļ			Volume	: $\Delta V = \beta V_i \Delta T$				
ł	where:							
	$\Delta L = chang$	e in length (r	n)					
ļ	$L_i = initial le$	ength (m)						
İ	α = linear o	oëfficient of	thermal expa	nsion (°C ⁻¹ or l	K ⁻¹)			
ļ	$\Delta V = changenerative changenerativ$	ge in volume	(m³)					
ļ		volume (m³)						
	β = volume	etric coëfficie	ent of thermal	expansion (°C	⁻¹ or K ⁻¹)			
ļ	$\Delta T = temperature$	erature chan	ge (°C or K)					
	Values of α and	d β at 20°C fo	or some solids	and liquids:				
ļ	Substance	α(°C ⁻¹)	β(°C ⁻¹)	Substance	α(°C ⁻¹)	β (°C ⁻¹)		
	aluminum	2.3×10 ⁻⁵	6.9×10 ⁻⁵	gold	1.4×10^{-5}	4.2×10 ⁻⁵		
ļ	copper	1.7×10 ⁻⁵	5.1×10 ⁻⁵	iron	1.18×10^{-5}	3.33×10 ⁻⁵		
ļ	brass	1.9×10 ⁻⁵	5.6×10 ⁻⁵	lead	2.9×10 ⁻⁵	8.7×10 ⁻⁵		
ļ	diamond	1×10 ⁻⁶	3×10 ⁻⁶	mercury	6.1×10 ⁻⁵	1.82×10^{-4}		
İ	ethanol		7.5×10 ⁻⁴	silver	1.8×10^{-5}	5.4×10 ⁻⁵		
	glass	8.5×10 ⁻⁶	2.55×10^{-6}	water (liq.)	6.9×10^{-5}	2.07×10^{-4}		
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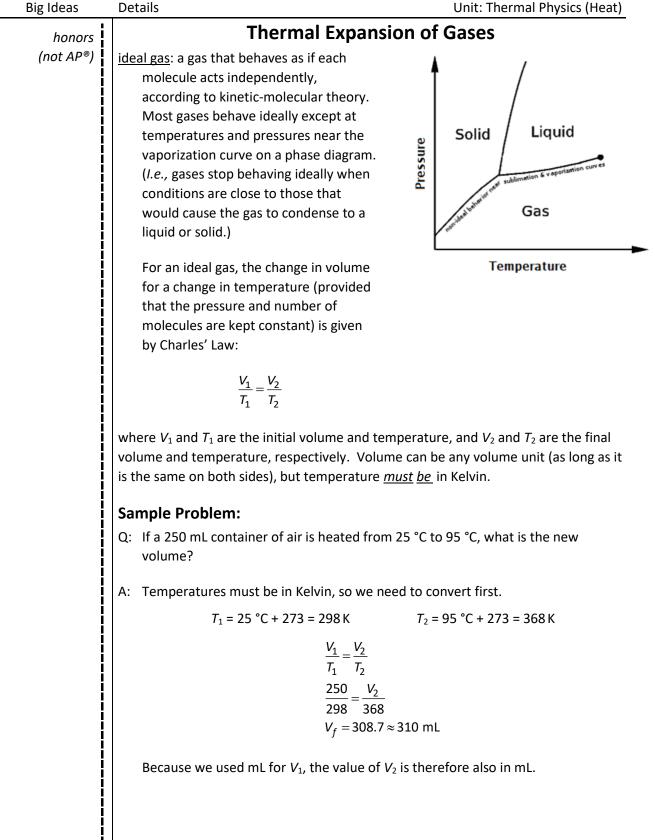
Page: 77 Unit: Thermal Physics (Heat)





Big Ideas	Details Unit: Thermal Physics (Heat)
honors (not AP®)	Q: A typical mercury thermometer contains about 0.22 cm ³ (about 3.0 g) of mercury. Find the change in volume of the mercury in a thermometer when it is heated from 25 °C to 50. °C.
	A: For mercury, $\beta = 1.82 \times 10^{-4} \text{ °C}^{-1}$.
	$\Delta V = \beta V_i \Delta T$
	$\Delta V = (1.82 \times 10^{-4})(0.22)(25)$
	$\Delta V = 0.00091~\mathrm{cm}^3$
	If the distance from the 25 °C to the 50 °C mark is about 3.0 cm, we could use this information to figure out the bore (diameter of the column of mercury) of the thermometer:
	$V = \pi r^2 h$
	$0.00091 = (3.14)r^2(3.0)$
	$r^2 = \frac{0.00091}{(3.14)(3.0)} = 9.66 \times 10^{-5}$
	$r = \sqrt{9.66 \times 10^{-5}} = 0.0098 \text{ cm}$
	The bore is the diameter, which is twice the radius, so the bore of the thermometer is (2)(0.0098) = 0.0197 cm, which is about 0.20 mm.

Big Ideas	Details	Unit: Thermal Physics (Heat)				
honors		Homework Problems				
(not AP®)	You will need to look up coëfficients of thermal expansion in <i>Table K. Thermal Properties of Selected Materials</i> on page 504 of your Physics Reference Tables.					
		brass rod is 27.50 cm long at 25 °C. How long would the rod be if it heated to 750. °C in a flame?				
	Answ	er: 27.88 cm				
ļ	2. (M) A	A steel bridge is 625 m long when the temperature is 0 °C.				
	a	If the bridge did not have any expansion joints, how much longer would the bridge be on a hot summer day when the temperature is 35 °C?				
		(Use the linear coëfficient of expansion for iron.)				
		Answer: 0.258 m				
	b	. Why do bridges need expansion joints?				
Ì						
	the o	A 15.00 cm long bimetal strip is aluminum on one side and copper on ther. If the two metals are the same length at 20.0 °C, how long will be at 800. °C?				
	Δηςω	ers: aluminum: 15.269 cm; copper: 15.199 cm				
		glass volumetric flask is filled with water exactly to the 250.00 mL line				
		°C. What volume will the water occupy after it cools down to 20. °C?				
ļ	Answ	er: 248.45 mL				



		Thermal Expansion	Page: 82
Big Ideas	Details		Unit: Thermal Physics (Heat)
honors		Homework Proble	ms
honors (not AP®)	1.	(S) A sample of argon gas was cooled, and its 250. mL. If its final temperature was -45.0 °C, temperature?	volume went from 380. mL to
	2.	Answer: 347 K or 74 °C (M) A balloon contains 250. mL of air at 50 °C cooled to 20.0 °C, what will be the new volum	
!		Answer: 226.8mL	

Unit: Thermodynamics

Details

Topics covered in this chapter:

Kinetic-Molecular Theory	88
Gas Laws	92
Ideal Gas Law	
Energy Conversion	
Thermodynamics	
Pressure-Volume (PV) Diagrams	126
Heat Engines	138
Efficiency	143

This chapter is about heat as a form of energy and the ways in which heat affects objects, including how it is stored and how it is transferred from one object to another.

- *Kinetic-Molecular Theory* explains the implications of the theory that gases are made of large numbers of independently moving particles.
- *Gas Laws* and *The Ideal Gas Law* describe and explain relationships between pressure, volume, temperature and the number of particles in a sample of gas.
- *Energy Conversion* describes conversion between heat and other forms of energy.
- *Thermodynamics* describes the transfer of energy into or out of a sample of gas.
- *Pressure-Volume (PV) Diagrams* and *Heat Engines* describe the relationship between changes in pressure and volume, heat, and work done on or by a gas.
- *Efficiency* describes the relationship between the work obtained from changes to a sample of gas and the maximum amount of energy that is theoretically available.

New challenges specific to this chapter include looking up and working with constants that are different for different substances.

Big Ideas	Details Unit: Thermodynami
	Standards addressed in this chapter:
	Next Generation Science Standards (NGSS):
	HS-PS2-6. Communicate scientific and technical information about why the molecular-level structure is important in the functioning of designed materials.
	HS-PS3-1. Create a computational model to calculate the change in the energy of one component in a system when the change in energy of the other component(s) and energy flows in and out of the system are known.
	HS-PS3-2. Develop and use models to illustrate that energy at the macroscopic scale can be accounted for as either motions of particles or energy stored fields.
	HS-PS3-4. Plan and conduct an investigation to provide evidence that the transfer of thermal energy when two components of different temperatur are combined within a closed system results in a more uniform energy distribution among the components in the system (second law of thermodynamics).
AP [®] only	AP [®] Physics 2 Learning Objectives/Essential Knowledge (2024):
	9.1.A : Describe the pressure a gas exerts on its container in terms of atomic motion within that gas.
	9.1.A.1 : Atoms in a gas collide with and exert forces on other atoms in the g and with the container in which the gas is contained.
	9.1.A.1.i: Collisions involving pairs of atoms or an atom and a fixed object can be described and analyzed using conservation of momentum principles.
	9.1.A.1.ii: The pressure exerted by a gas on a surface is the ratio of the surface of the magnitudes of the perpendicular components of the forces exerted by the gas's atoms on the surface to the area of the surface.
	9.1.A.1.iii : Pressure exists throughout the gas itself, not just at the boundary between the gas and the container.
	9.2.A : Describe the properties of an ideal gas.
	9.2.A.1 : The classical model of an ideal gas assumes that the instantaneous velocities of atoms are random, the volumes of the atoms are negligible compared to the total volume occupied by the gas, the atoms collide elastically, and the only appreciable forces on the atoms are those that occur during collisions.

Big Ideas	Details Unit: Thermodynamics
AP® only	9.2.A.2 : An ideal gas is one in which the relationships between pressure, volume, the number of moles or number of atoms, and temperature of a gas can be modeled using the equation $PV = nRT = Nk_BT$
	9.2.A.3 : Graphs modeling the pressure, temperature, and volume of gases can be used to describe or determine properties of that gas.
	9.2.A.4 : A temperature at which an ideal gas has zero pressure can be extrapolated from a graph of pressure as a function of temperature.
	9.3.A : Describe the transfer of energy between two systems in thermal contact due to temperature differences of those two systems.
	9.3.A.1 : Two systems are in thermal contact if the systems may transfer energy by thermal processes.
	9.3.A.1.i : Heating is the transfer of energy into a system by thermal processes.
	9.3.A.1.ii : Cooling is the transfer of energy out of a system by thermal processes.
	9.3.A.3 : Energy is transferred through thermal processes spontaneously from a higher-temperature system to a lower-temperature system.
	9.3.A.3.i : In collisions between atoms from different systems, energy is most likely to be transferred from higher-energy atoms to lower-energy atoms.
	9.3.A.3.ii : After many collisions of atoms from different systems, the most probable state is one in which both systems have the same temperature.
	9.3.A.4 : Thermal equilibrium results when no net energy is transferred by thermal processes between two systems in thermal contact with each other.
	9.4.A : Describe the internal energy of a system.
	9.4.A.1 : The internal energy of a system is the sum of the kinetic energy of the objects that make up the system and the potential energy of the configuration of those objects.
	9.4.A.1.i: The atoms in an ideal gas do not interact with each other via conservative forces, and the internal structure is not considered. Therefore, an ideal gas does not have internal potential energy.
	9.4.A.1.ii : The internal energy of an ideal monatomic gas is the sum of the kinetic energies of the constituent atoms in the gas.

Big Ideas	Details	Unit: Thermodynamics
AP® only	inter	Changes to a system's internal energy can result in changes to the rnal structure and internal behavior of that system without changing motion of the system's center of mass.
	9.4.B: Des	cribe the behavior of a system using thermodynamic processes.
	ener	The first law of thermodynamics is a restatement of conservation of gy that accounts for energy transferred into or out of a system by k, heating, or cooling.
	9.4.B.:	1.i : For an isolated system, the total energy is constant.
	en	1.ii: For a closed system, the change in internal energy is the sum of ergy transferred to or from the system by heating, or work done on e system.
	pr	1.iii : The work done on a system by a constant or average external essure that changes the volume of that system (for example, a piston mpressing a gas in a container) is defined as $W = -P\Delta V$.
		Pressure-volume graphs (also known as PV diagrams) are esentations used to represent thermodynamic processes.
		2.i: Lines of constant temperature on a PV diagram are called otherms.
	ex	2.ii: The absolute value of the work done on a gas when the gas pands or compresses is equal to the area underneath the curve of a ot of pressure vs. volume for the gas.
	betv the s volu pres	Special cases of thermal processes depend on the relationship veen the configuration of the system, the nature of the work done on system, and the system's surroundings. These include constant me (isovolumetric), constant temperature (isothermal), and constant sure (isobaric), as well as processes where no energy is transferred to om the system through thermal processes (adiabatic).
	9.6.A : Des	scribe the change in entropy for a given system over time.
	an is	The second law of thermodynamics states that the total entropy of solated system can never decrease and is constant only when all sesses the system undergoes are reversible.
		Entropy can be qualitatively described as the tendency of energy to ad or the unavailability of some of the system's energy to do work.
	9.6.A.2	2.i : Localized energy will tend to disperse and spread out.
	cu	2.ii : Entropy is a state function and therefore only depends on the rrent state or configuration of a system, not how the system reached at state.

AP [®] only	9.6.A.2.iii : Maximum entropy occurs when a system is in thermodynamic equilibrium.
	9.6.A.3 : The change in a system's entropy is determined by the system's interactions with its surroundings.
	9.6.A.3.i : Closed systems spontaneously move toward thermodynamic equilibrium.
	9.6.A.3.ii : The entropy of a closed system never decreases, but the entropy of an open system can decrease because energy can be transferred into or out of the system.
	Skills learned & applied in this chapter:
	 Working with material-specific constants from a table.
	 Working with more than one instance of the same quantity in a problem.
	 Combining equations and graphs.

Big Ideas

Details

Kinetic-Molecular Theory

Unit: Thermodynamics

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-8(MA)

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 9.1.A, 9.1.A.1,

9.1.A.1.i, 9.1.A.ii, 9.1.B, 9.1.B.1, 9.1.B.1.i, 9.1.B.1.ii

Mastery Objective(s): (Students will be able to ...)

• Explain how each aspect of Kinetic-Molecular Theory applies to gases.

Success Criteria:

- Descriptions account for behavior at the molecular level.
- Descriptions account for measurable properties, *e.g.*, temperature, pressure, volume, *etc*.

Language Objectives:

• Explain how gas molecules behave and how their behavior relates to properties we can measure.

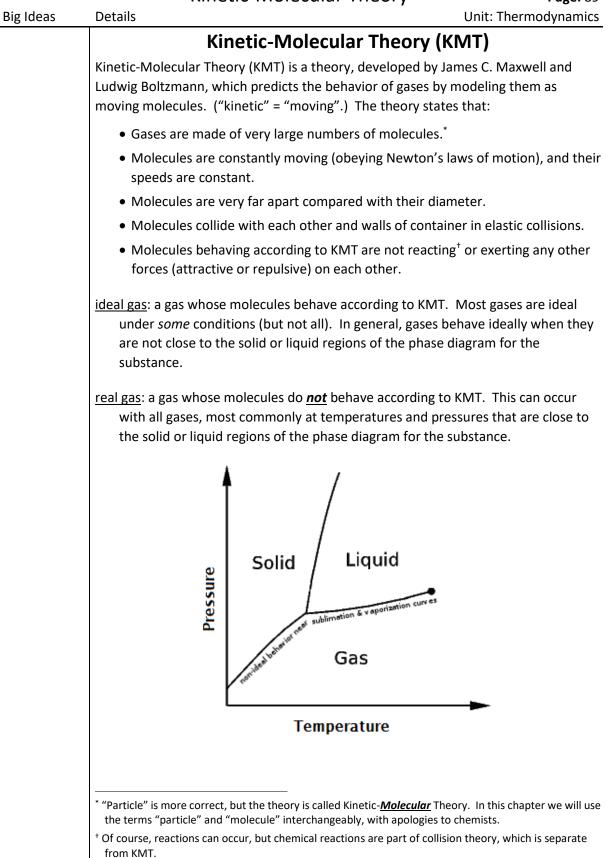
Tier 2 Vocabulary: kinetic, gas, ideal, real

Notes:

In chemistry you learned about matter, including its composition, structure, and changes that it can undergo. In physics, we are interested in matter to the extent that it can be used to bring objects or energy in contact with each other and transfer forces, energy or momentum from one object or collection of objects to another. This chapter is about gases and using properties of gases to convert between mechanical and thermal energy.

State	Description	Uses		
solid	Particles rigidly bonded. Bonds difficult to break. (Definite shape & definite volume)	Construction materials where structure is important. Conduction of heat and/or electricity. Storage of heat as thermal mass.		
liquid	Particles loosely bonded and have limited movement. Bonds continuously breaking & reforming. (Definite volume, but indefinite shape.)	Chemical reactions & heat transfer where continual mixing of materials is needed. Storage of heat as thermal mass.		
gas	Particles not bonded and able to move freely. (Indefinite shape & volume.)	Heat and materials transfer in large spaces. <i>Conversion of energy between heat and mechanical work.</i>		

Properties of Different States of Matter



Big	Ideas	

Details

Measurable Properties of Gases

All gases have the following properties that can be measured:

Property	Variable	S.I. Unit	Description		
amount	N	_	amount of gas (particles)		
amount			amount of gas (moles)		
	n	mole (mol)	$(1 \text{ mol} = 6.02 \times 10^{23} \text{ particles})$		
volume	V	cubic meter (m³)	space that the gas takes up		
temperature	Т	kelvin (K)	ability to transfer heat through collisions with other molecules (average kinetic energy of the particles)		
pressure	Р	pascal (Pa)	average force on the walls of the container due to collisions between the molecules and the walls		

Notes about calculations:

- Moles are based on the definition that 1 mole = 6.022 140 76×10²³ particles .

 mole was originally the number of carbon atoms in exactly 12 grams of carbon-12, such that the molar mass of a substance is the same number of grams as the average atomic mass of one atom in atomic mass units. This definition persisted, despite the fact that the base mass unit of the MKS system is the kilogram.
- Temperature must be absolute, which means you <u>must</u> use Kelvin. A temperature of 0 in a gas laws calculation can only mean absolute zero.
- Pressures must be absolute. (For example, you can't use a tire gauge because it measures "gauge pressure," which is the difference between atmospheric pressure and the pressure inside the tire.) A pressure of 0 in a gas laws calculation can only mean that there are no molecules colliding with the walls.

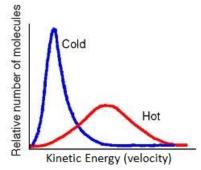
Other Common Units

- Volume can be measured in liters (L) or milliliters (mL). $1 \text{ m}^3 = 1000 \text{ L}$ and 1 L = 1000 mL
- Pressure can be measured in many different units.
 - 1 atm = 101 325 Pa = 14.696 psi = 760 mm Hg = 29.92 in. Hg
 - 1 bar = 100000 Pa = 100 kPa \approx 1 atm

Temperature and Particle Motion

Particles of all substances, whether solids, liquids, or gases, are in constant motion. As described in *Phases & Phase Changes* starting on page 63, the particles of solids and liquids are bonded to one or more other particles. Gas particles, however, are not bonded to other particles. As stated above, these particles move at high speeds in straight lines until they collide with other particles or the walls of the container.

As described in *Heat & Temperature*, starting on page 39, temperature is related to the average kinetic energy of the particles. The kinetic energies follow the Maxwell-Boltzmann probability distribution, which is characterized by a longer tail on the right side. (The equation requires multivariable calculus and is beyond the scope of this course.)



The relationship between the kinetic energy and the average velocity of the molecules is characterized by the equation:

$$K_{avg} = \frac{3}{2}k_{B}T = \frac{1}{2}mv_{rms}^{2}$$

where:

Big Ideas

Details

 $K_{avg} =$ average kinetic energy of the particles (J)

 $k_{B} = \text{Boltzmann constant} = 1.38 \times 10^{-23} \frac{\text{J}}{\text{K}}$

T = absolute temperature (K)

m = mass of a particle (kg)

 $v_{rms} = \text{root mean square velocity}(\frac{m}{s})$

The "root mean square velocity" simply means that v^2 is an average, which we call the "mean square velocity". v is the square root of this quantity, so we call it the "root mean square velocity".

Root mean square velocity is also discussed in *Thermodynamics*, starting on page 109.

	Gas Laws Page:	92
deas	Details Unit: Thermodynam	ics
	Gas Laws	
	Unit: Thermodynamics	
	NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-8(MA)	
	AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 9.2.A, 9.2.A.1, 9.2.A.2, 9.2.A.3, 9.2.A.4	
	Mastery Objective(s): (Students will be able to)	
	• Qualitatively describe the relationship between any two of the quantities: <i>number of particles, temperature, pressure,</i> and <i>volume</i> in terms of Kinetic Molecular Theory (KMT).	
	 Quantitatively determine the number of particles, temperature, pressure, or volume in a before & after problem in which one or more of these quantitie is changing. 	
	Success Criteria:	
	 Descriptions relate behavior at the molecular level to behavior at the macroscopic level. 	
	 Solutions have the correct quantities substituted for the correct variables. 	
	• Chosen value of the gas constant has the same units as the other quantities the problem.	in
	 Algebra and rounding to appropriate number of significant figures is correct 	
	Language Objectives:	
	 Identify each quantity based on its units and assign the correct variable to it 	
	 Understand and correctly use the terms "pressure," "volume," and "temperature," and "ideal gas." 	
	 Explain the placement of each quantity in the ideal gas law. 	
	Tier 2 Vocabulary: ideal, law	

		Gas Laws	Page: 93
Big Ideas	Details		Unit: Thermodynamics
	Labs, Activities &	& Demonstrations:	
	 Vacuum pum 	p (pressure & volume) with:	
	\circ balloon (air	vs. water)	
	 shaving creating 	am	
	 Absolute zero 	apparatus (pressure & temperatu	ire)
	 Balloon with t 	tape (temperature & volume)	
	 Can crush (pro 	essure, volume & temperature)	
	Notes:		
	kinetic-molecul and move freely collide, the colli	behaves as if each molecule acts i ar theory. Specifically, this means y in straight lines at constant speed sions are perfectly elastic, which n nergy or momentum lost. (See the s on page 88.)	the molecules are far apart ds. When the molecules neans they bounce off each

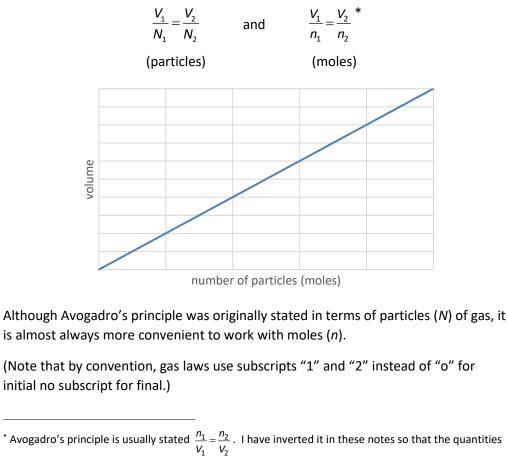
Details

Avogadro's Principle

In 1811, Italian physicist Amedeo Avogadro (whose full name was Lorenzo Romano Amedeo Carlo Avogadro di Quaregna e di Cerreto) published the principle that equal volumes of an ideal gas at the same temperature and pressure must contain equal numbers of particles.

Demonstration	Outcome	What the molecules are doing	Conclusion
put more (moles of) air into a balloon $n \uparrow$	the volume of the balloon got larger V↑	crowding each other → pushing each other farther away	<i>n</i> and <i>V</i> are directly proportional. $\frac{V}{n} = \text{constant}$

If the pressure and temperature are constant, then for an ideal gas:



in the numerator and denominator are the same as the quantities in the numerator and denominator of the combined gas law.

ig Ideas	Details	-		nit: Thermodyna
		Boyle	e's Law	
	In 1662, British physic pressure and volume		ert Boyle published hi sely proportional.	s findings that th
	Demonstration	Outcome	What the molecules are doing	Conclusion
	decrease pressure by putting a balloon in a vacuum chamber	the volume of the air inside the balloon increased	expanding the space = more surface area → less force per unit area	<i>P</i> and <i>V</i> are inversely proportional.
	₽↓	v↑	(less pressure)	<i>PV</i> = constant
			$=P_2V_2$	
	absolute pressure			
	absolute			
			volume	

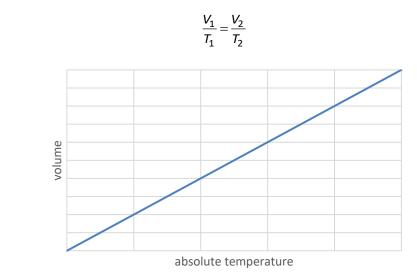
Details

Charles' Law

In the 1780s, French physicist Jacques Charles discovered that the volume and temperature of a gas were directly proportional.

Demonstration	Outcome	What the molecules are doing	Conclusion
place masking tape around balloon and heat with hot air gun T↑	the volume of the air got larger and expanded the balloon except where the tape pinched it $V\uparrow$	moving more slowly → pushing each other less far away	V and T are directly proportional. $\frac{V}{T} = \text{constant}$

If pressure and the number of particles are constant, then for an ideal gas:



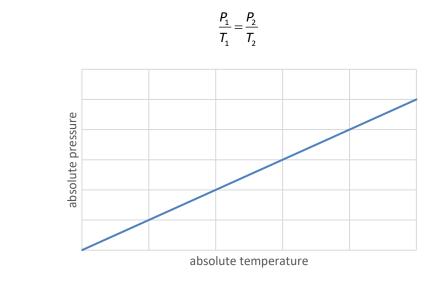
Note that if a plot of temperature *vs.* volume is extrapolated to a volume of zero, the *x*-intercept will be absolute zero.

Gay-Lussac's Law

In 1702, French physicist Guillaume Amontons discovered that there is a relationship between the pressure and temperature of a gas. However, precise thermometers were not invented until after Amontons' discovery, so it wasn't until 1808, more than a century later, that French chemist Joseph Louis Gay-Lussac confirmed this law mathematically. The pressure law is most often attributed to Gay-Lussac, though some texts refer to it as Amontons' Law.

Demonstration	Outcome	What the molecules are doing	Conclusion
increase temperature by heating a metal sphere full of air τ \uparrow	the pressure of the air increased P^{\uparrow}	moving faster → colliding with more force	<i>P</i> and <i>T</i> are directly proportional. $\frac{P}{T} = \text{constant}$

If volume and the number of particles are constant, then for an ideal gas:



Note that at absolute zero, gas molecules do not exert any pressure on the walls of the container.

Big Ideas	Gas Laws Details Unit:	Page: 98 Thermodynamic		
	The Combined Gas Law	mermouynamie		
	We can combine each of the above principles. When we do this (k the numerator and <i>n</i> (or <i>N</i>) and <i>T</i> in the denominator for consisten following relationship for an ideal gas:			
	$\frac{P_1 V_1}{n_1 T_1} = \frac{P_2 V_2}{n_2 T_2} = \text{constant} \qquad \frac{P_1 V_1}{N_1 T_1} = \frac{P_2 V_2}{N_2 T_2} = \text{constant}$	nt		
	using moles using particles			
	Note, however, that in most situations where we want to calculate properties of a gas, the number of moles or particles remains constant. This means $n_1 = n_2$ or $N_1 = N_2$, and we can cancel it from the equation. This gives:			
	$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2}$			
	The above equation is called the "combined gas law", which is used "before/after" problems involving ideal gases.	d to solve most		
	When using the combined gas law, any quantity that is not changing may be cancelled out of the equation. (If a quantity is not mentioned in the problem, you can assume that it is constant and may be cancelled.)			
	For example, suppose a problem doesn't mention anything about t That means T is constant and you can cancel it. When you cancel 7 of the combined gas law, you get:	•		
	$\frac{P_1V_1}{\mathcal{I}_1} = \frac{P_2V_2}{\mathcal{I}_2}$ which simplifies to $P_1V_1 = P_2V_2$ (Boyle's L	aw)		
	Solving Problems Using the Combined G	ias Law		
	You can use this method to solve any "before/after" gas law proble			
	1. Determine which variables you have.			
	2. Determine which values are <i>initial</i> (#1) vs. <i>final</i> (#2).			
	 Start with the combined gas law and cancel any variables t not changing or omitted (assumed not to be changing). 	hat are explicitly		
	 Substitute your numbers into the resulting equation and so all initial and final quantities have the same units, and don temperatures <u>must</u> be in Kelvin!) 	-		

		Gas Laws	S Page: 95
Big Ideas	Detai	ls	Unit: Thermodynamics
	use S	.I. units when solving problems usin rtant to use the same units for the	h sides of the equation, it is not necessary to ng the combined gas law. It is, however, <i>same quantity on both sides of the</i>
	Sam	ple problem:	
		gas has a temperature of 25 °C and o 35 °C, what will the new pressure	d a pressure of 1.5 bar. If the gas is heated be?
	A: 1. Find which variables we have.		
		We have two temperatures (25 the new pressure that we're loo	°C and 35 °C), and two pressures (1.5 bar an king for).
	2	-	ne gas ("heated"). Anything that was true is time "1", and anything that is true about '2".
		Time 1 ("before"):	<u>Time 2 ("after")</u> :
		<i>P</i> ₁ = 1.5 bar	$P_2 = P_2$
		<i>T</i> ₁ = 25 °C + 273 = 298 K	<i>T</i> ₂ = 35 °C + 273 = 308 K
	3	. Set up the formula. We can can mention it:	cel volume (<i>V</i>), because the problem doesn
		$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$ which gives	us $\frac{P_1}{T_1} = \frac{P_2}{T_2}$ (Gay-Lussac's Law)
	4	. Plug in our values and solve:	
			$\frac{P_2}{18 \text{ K}} \rightarrow P_2 = 1.55 \text{ bar}$

	Gas	Laws	Page: 100
Big Ideas	Details		Unit: Thermodynamics
	Hom	ework Problems	
	Solve these problems by using one convert temperatures to Kelvin!	e of the gas laws in this sec	tion. Remember to
	 (M) A sample of oxygen gas occupies a volume of 250. mL at a pres 740. torr. What volume will it occupy at 800. torr?). mL at a pressure of
	Answer: 231.25 mL 2. (M) A sample of O₂ is at a 2.30 L. To what temperature	•	•
	Answer: 612 °C 3. (S) H ₂ gas was cooled from What was its original press		ressure is 750 torr.
	Answer: 980 torr 4. (S) A 2.00 L container of N be necessary to decrease t (<i>Hint: notice that the press</i> one of them so that both p	he pressure to 98.0 kPa? Sures are in different units.	You will need to convert
	Answer: 6.62 L		и кга.j

		Page: 101
Big Ideas Details		Unit: Thermodynamics
	S) A sample of air has a volume of 60.0 mL at S.T.P. sample have at 55.0 °C and 745 torr?	What volume will the
	Answer: 73.5 mL	
	M) N₂ gas is enclosed in a tightly stoppered 500. mI Latm. The flask, which is rated for a maximum press neated to 680. °C. Will the flask explode?	
,	Answer: $P_2 = 3.25$ atm. Yes, the flask will explode.	
t	A scuba diver's 10. L air tank is filled to a pressure of emperature of 32.0 °C. When the diver is breathing water temperature is 8.0 °C, and the pressure is 2.1 I	the air underwater, the
	a. (M) What volume of air does the diver use?	
	Answer: 921 L	
	b. (S) If the diver uses air at the rate of 8.0 L/min, air last?	how long will the diver's
	Answer: 115 min	

leas	Details	Unit: Thermodynami
	Ideal Gas Law	
	Unit: Thermodynamics	
	NGSS Standards/MA Curriculum Frameworks (2016): H	HS-PS2-8(MA)
	AP® Physics 2 Learning Objectives/Essential Knowledge	e (2024): 9.2.A, 9.2.A.1,
	9.2.A.2, 9.2.A.3, 9.2.A.4	
	Mastery Objective(s): (Students will be able to)	
	Describe the relationship between any two variab	oles in the ideal gas law.
	 Apply the ideal gas law to problems involving a satisfies 	mple of gas.
	Success Criteria:	
	Solutions have the correct quantities substituted	for the correct variables.
	 Chosen value of the gas constant has the same un the problem. 	nits as the other quantities i
	Algebra and rounding to appropriate number of s	ignificant figures is correct.
	Language Objectives:	
	Identify each quantity based on its units and assign Eventain the placement of each quantity in the idea	-
	 Explain the placement of each quantity in the idea Tier 2 Vocabulary: ideal, law 	al gas law.
	Notes:	
	ideal gas: a gas that behaves according to Kinetic-Molec	cular Theory (KMT).
		-
	When we developed the combined gas law, before we comoles or particles, we had the equations:	cancelled the number of
	moles of particles, we had the equations.	
	$\frac{P_1 V_1}{n_1 T_1} = \frac{P_2 V_2}{n_2 T_2} = \frac{PV}{nT} = R \text{ (constant)} \qquad \frac{P_1 V_1}{N_1 T_1} = \frac{P_2 V_2}{N_2}$	$\frac{V_2}{T_2} = \frac{PV}{NT} = k_B$ (constant)
	using moles u	using particles
	where <i>n</i> is the number of moles of gas, and <i>N</i> is the num mole is 6.02×10^{23} particles, which means <i>N</i> = (6.02×10^{23} cm s = (6.02	
	Because P, V, n and T are all of the quantities needed to	specify the conditions of a
	ideal gas, this expression must be true for <i>any ideal gas</i> in m^3 , <i>P</i> is in Pa, <i>n</i> is in moles, and <i>T</i> is in Kelvin, then:	
	$R = 8.31 \frac{J}{\text{mol-K}}$ and $k_B = 1.38 \times 10^{-1}$	$0^{-23} \frac{J}{K}$
	<i>R</i> is called "the gas constant," and $k_{\rm B}$ is Boltzmann's con	stant.
	We can rearrange $\frac{PV}{nT} = R$ and $\frac{PV}{NT} = k_{B}$ to get the ideal	gas law in its familiar form:

Ideal Gas Law

Page: 102

Other	Va	ابنوج	of	R
Other	va	iues	UL.	n

Details

Big Ideas

The purpose of the gas constant *R* is to convert the quantity nT from units of mol·K to units of pressure × volume. This constant can have different values, depending on the units that it needs to cancel:

$$\begin{split} R &= 8.31 \frac{J}{mol \cdot K} \equiv 8.31 \frac{m^{3} \cdot Pa}{mol \cdot K} \equiv 8.31 \frac{L \cdot kPa}{mol \cdot K} \equiv 8.31 \times 10^{-3} \frac{kJ}{mol \cdot K} \\ R &= 0.0821 \frac{L \cdot atm}{mol \cdot K} \qquad R = 62.4 \frac{L \cdot torr}{mol \cdot K} \qquad R = 1.987 \frac{cal}{mol \cdot K} \equiv 1.987 \frac{BTU}{lb - mol \cdot R} \end{split}$$

Use of non-S.I. units, such as atm or torr, is more common in chemistry. In this course, we will use the S.I. units of m^3 for volume and Pa for pressure. The unit $Pa \cdot m^3$ is equivalent to a joule.

Solving Problems Using the Ideal Gas Law

If a gas behaves according to the ideal gas law, simply substitute the values for pressure, volume, number of moles (or particles), and temperature into the equation. Be sure your units are correct (especially that temperature is in Kelvin), and that you use the correct constant, depending on whether you know the number of particles or the number of moles of the gas.

Sample Problem:

A 3.50 mol sample of an ideal gas has a pressure of 120000 Pa and a temperature of 35 °C. What is its volume? $T \rightarrow K$

Answer:

Note that because pressure is given in pascals (Pa), we need to use the value of the gas constant that also uses Pa: $R = 8.31 \frac{\text{m}^3 \cdot \text{Pa}}{\text{mol} \cdot \text{K}}$

<i>P</i> = 120 000 Pa	<i>n</i> = 3.50 mol
V = V	$R = 8.31 \frac{\text{m}^3 \cdot \text{Pa}}{\text{mol} \cdot \text{K}}$

T = 35 °C + 273 = 308 K

Then we substitute these numbers into the ideal gas law and solve:

$$PV = nRT$$

 $V = \frac{nRT}{P} = \frac{(3.50)(8.31)(308)}{120\,000} = 0.0747\,\text{m}^3$

Ideal Gas Law

Big Ideas		
honors	Details	Unit: Thermodynan
nonors	Real G	iases
(not AP®)	As stated previously, when the temperature solid or liquid regions of the phase diagram for the substance, gases start to exhibit non-ideal behaviors. Recall the following definition of a real gas: <u>real gas</u> : a gas whose molecules do <u>not</u> behave according to kinetic-molecular theory (KMT). This occurs most commonly at temperatures and pressures that are close to the solid or liquid regions	Solid Liquid Solid Evaporization curves Gas
	of the phase diagram for the substance. In the late 19 th century, the Dutch physicist correction to the ideal gas law that can be a The van der Waals Equation applies correct terms in the equation: $\left(P + a \frac{n^2}{V^2}\right) (V + a \frac{n^2}{V^2}) = 0$	ipplied to real gases.
	in this equation, the constants <i>a</i> and <i>b</i> are p looked up or determined experimentally. The corrected pressure term ($P + a \frac{n^2}{V^2}$ inste	
	each other slightly at low pressures, but rep	
	together. This repulsion acts like additional	-
	together. This repulsion acts like additional The corrected volume term $(V - nb)$ instead assumes that the molecules are far enough the volumes of the molecules themselves as As the molecules are brought closer togethe up by <i>n</i> moles of molecules from the availab	pressure. of V) term is because the ideal gas law apart that we do not need to consider s part of the volume of their container er, we have to subtract the space take

Ideal Gas Law

Big Ideas	Details Unit: Thermodynamics
	Homework Problems
	Use the ideal gas law to solve the following problems. Be sure to choose the
	appropriate value for the gas constant, and to convert temperatures to Kelvin.
	 (M) A sample of 1.00 moles of oxygen at 50.0 °C and 98.6 kPa occupies what volume?
	Answer: 27.2 L
	2. (S) If a steel cylinder with a volume of 1.50 L contains 10.0 moles of oxygen, under what pressure is the oxygen if the temperature is 27.0 °C?
	Answer: 164 atm = 125 000 torr = 16 600 kPa 3. (S) In a gas thermometer, the pressure of 0.500 L of helium is 113.30 kPa at a temperature of −137 °C. How many moles of gas are in the sample?
	Answer: 0.050 mol 4. (M) A sample of 4.25 mol of hydrogen at 20.0 °C occupies a volume of 25.0 L. Under what pressure is this sample?
	Answer: 4.09 atm = 3 108 torr = 414 kPa

Energy Conversion

Unit: Thermodynamics

Details

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS3-1

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): N/A

Mastery Objective(s): (Students will be able to ...)

Describe the conversion of energy between heat and other forms.

Success Criteria:

• Descriptions & explanations account for observed behavior.

Language Objectives:

• Describe and explain an example of conversion of heat into mechanical work.

Tier 2 Vocabulary: heat, energy

Labs, Activities & Demonstrations:

- steam engine
- fire syringe
- metal spheres & paper

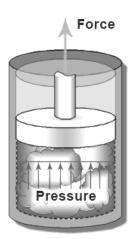
Notes:

The law of conservation of energy states that total energy is always conserved, but that energy can be converted from one form to another.

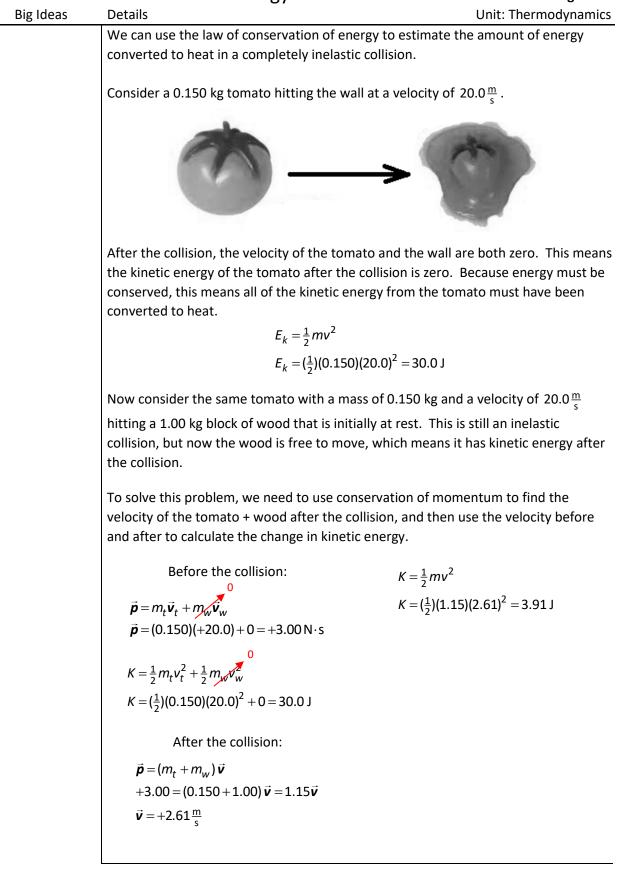
We have already seen this in mechanics with the conversion between gravitational potential energy and kinetic energy.

Heat is energy. Like other forms of energy, it can do work. For example, in a steam engine, heat is used to boil water in a sealed container. As more water boils, there is more gas in the boiler, which makes the pressure increase. If the gas can only expand by pushing against something (like a piston), the force from the pressure can do work by moving the piston and whatever it's connected to.

In mechanics, recall that collisions can be elastic or inelastic. In an elastic collision, kinetic energy is conserved; in an inelastic collision, some of the kinetic energy is converted to other forms, mostly heat.



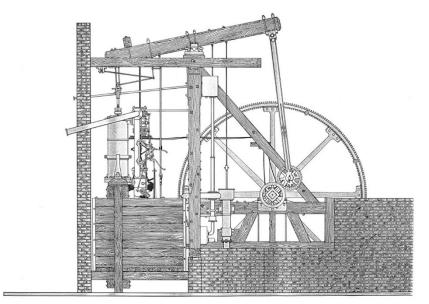
Energy Conversion



Energy Conversion

This means there is 30.0 - 3.91 = 26.1 J of kinetic energy that is "missing" after the collision. This "missing" energy is mostly converted to heat. If you could measure the temperature of the tomato and the wood extremely accurately before and after the collision, you would find that both would be slightly warmer as a result of the "missing" 26.1 J of energy.

The first instance of a machine using heat to do work was in 1698, when Thomas Savery patented a steam-driven water pump. In 1769, Scottish engineer James Watt and investor John Roebuck patented a steam engine that could be used for a variety of purposes, including running sawmills, cotton mills, and anything else that required a large amount of force. Watt built his first prototype steam engine in 1788.



James Watt's prototype steam engine, 1788

The invention of the steam engine was a significant factor in the spread of the industrial revolution, and all of the societal changes that went with it.

Thermodynamics is the study of heat energy and its conversion to other forms of energy. In chemistry, thermodynamics is thermal energy that drives chemical reactions. In physics, thermodynamics is thermal energy that can be converted to mechanical work (which you may recall from physics 1, is a force applied over a distance).

Big Ideas

Details

Unit: Thermodynamics

Details

Big Ideas

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-6

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): 9.3.A, 9.3.A.4, 9.4.A, 9.4.A.1, 9.4.A.1.i, 9.4.A.1.ii, 9.4.A.2, 9.4.B, 9.4.B.1, 9.4.B.1.i, 9.4.B.1.ii,

9.4.B.1.iii, 9.6.A, 9.6.A.1, 9.6.A.2, 9.6.A.2.i, 9.6.A.2.iii, 9.6.A.3, 9.6.A.3.i, 9.6.A.3.ii Mastery Objective(s): (Students will be able to...)

• Calculate kinetic energy, internal energy and work done by the particles of a gas.

Success Criteria:

- Solutions have the correct quantities substituted for the correct variables.
- Algebra and rounding to appropriate number of significant figures is correct.

Language Objectives:

• Describe the different types of energy (kinetic, internal, work) and explain what they measure.

Tier 2 Vocabulary: internal, energy, work

Labs, Activities & Demonstrations:

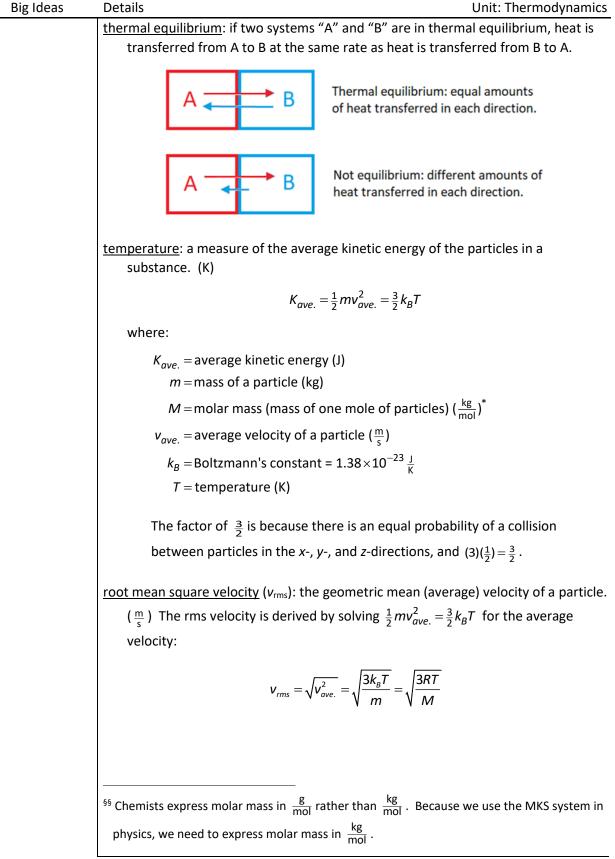
- heat exchange dice game
- dice distribution game
- entropy (microstates) percentile dice game

Notes:

thermodynamics: the study of heat-related (thermal) energy changes (dynamics)

Thermodynamics is an application of the law of conservation of energy. In Physics 1, we studied changes between gravitational potential energy and kinetic energy. Thermodynamic changes involve the same principle; the details and the equations, however, are quite different.

As was the case with gas laws, the topic of thermodynamics is studied by both chemists and physicists. Chemists tend to be more concerned with the heat produced and consumed by chemical changes and reactions. Physicists tend to be more concerned with the conversion between thermal energy (regardless of how it is produced) and other forms of energy, particularly mechanical.



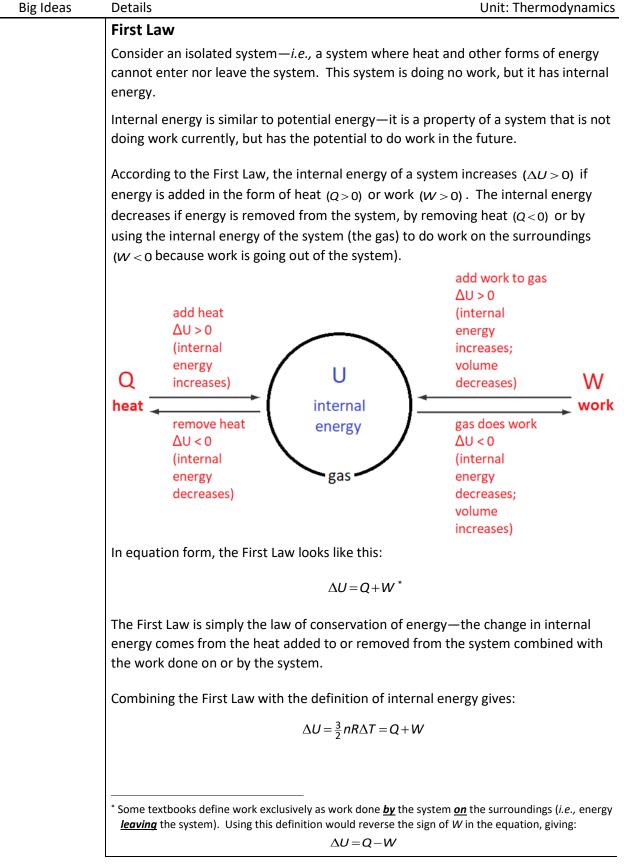
Thermodynamic	
Details	Unit: Thermodynam
<u>internal energy</u> (U [*]): the total thermal energy of its particles.	of a system due to the kinetic energ
If the kinetic energy of a single particle is	$K_{ave.} = \frac{3}{2}k_BT$, then the total kinetic
energy in a system that has N particles wo	-
$U = NK_{ave.}$	$=\frac{3}{2}Nk_{B}T$
Because it is generally unwieldy to perform numbers of particles, it is more convenier gives the equation for the internal energy particles:	t to use moles. Substituting nR for N
$U = \frac{3}{2}I$	nRT
Similarly, a <u>change</u> in internal energy (ΔU <u>change</u> in temperature (ΔT):) is related to the corresponding
$\Delta U = \frac{3}{2} nR\Delta T$	$\left(=\frac{3}{2}Nk_{B}\Delta T\right)$
heat (Q): thermal energy transferred into or o	ut of a system. (J)
<u>work</u> (W): mechanical energy (such as the app transferred into or out of a system. (J)	lication of a force over a distance)
The work that a gas can do comes from its a force on it as it expands. If the pressure $W = Fd$	is constant:
$P = \frac{F}{A} \rightarrow$	
$\therefore W = (h)$	(Δx)
$\Delta V = \lambda$	
$\therefore W =$	$P\Delta V$
If a gas does work by expanding, the ener system) to the object that the gas is pushi	ng against (the surroundings). This
means that when the volume increases (Δ system (W is negative). Conversely, if wo entering the system in order to compress decreases (ΔV is negative). This means th signs, which gives the equation:	the gas (W is positive), and the volu
system (<i>W</i> is negative). Conversely, if wo entering the system in order to compress decreases (ΔV is negative). This means th	the gas (W is positive), and the volur at W and $P\Delta V$ must have opposite
system (<i>W</i> is negative). Conversely, if wo entering the system in order to compress decreases (ΔV is negative). This means th signs, which gives the equation:	the gas (<i>W</i> is positive), and the volu at <i>W</i> and <i>P</i> ∆ <i>V</i> must have opposite
system (<i>W</i> is negative). Conversely, if wo entering the system in order to compress decreases (ΔV is negative). This means th signs, which gives the equation: W = -H	the gas (W is positive), and the volur at W and $P\Delta V$ must have opposite

Big Ideas

	inermodynamics	Page: 12
Ideas Deta	ils	Unit: Thermodynami
	f pressure is not constant, then $W\!=\!-\Delta$ (PV) , which m	neans you would need to
	calculate PV at each point, taking the limit as the dista	
	points shrinks to zero, and add them up. In calculus, t	his is the integral:
	$W = -\int P \mathrm{d}V$, where P is a function of V.	
	n an algebra-based course, we will limit ourselves to p	problems where the
	pressure is constant, or where the pressure change is linear a	
	average pressure, giving:	
	$W = -P_{ave.}\Delta V$	
entr	opy (S): "unusable" thermal energy in a system. Energy	gy in the form of entropy
	unavailable because it has "escaped" or "spread out".	(Entropy will be discuss
	further in the Second Law of Thermodynamics.)	
	Laws of Thermodynami	cs
The	laws of thermodynamics describe the behavior of syst	
	iges in heat energy.	
	nistorical reasons, the laws are numbered from $0-3^*$ ir	ostead of 1-4 because th
	v was added after the others, and the laws are often r	
num		
	0. If a system is at thermal equilibrium, every compo	nent of the system has t
	same temperature. ("You have to play the game."	•
	1. Heat always flows from a region of higher internal	energy to a region of
	lower internal energy. Because internal energy is	directly proportional to
	temperature, this is equivalent to saying that heat	flows from a region of
	higher temperature to a region of lower temperat	•
	get more heat out of a system than you put in. ("	You can't win.")
	2. In almost every change, some energy is irretrievab	ly lost to the
	surroundings. Entropy is a measure of this "lost" e	
	universe is always increasing, which means on any	
	always get out less energy than you put in. ("You	can't break even.")
	3. Conservation of energy always applies. In any clos	sed system, the total
	energy (internal energy + entropy + work) remains	
	"lost," it turned into an increase in entropy. ("You	
	game.")	
	re is one type of person in the world: those who start coun	ting from zero and those w
· · ·	rt counting from one.	

	Thermouynamics	Page: 113
Big Ideas	Details	Unit: Thermodynamics
	Zeroth Law (or Zero Law)	
	The zeroth law says that if you have multiple systems in heat transferred from "A" to "B" is equal to the heat transtended the transtended from the systems must have the same temperature. The	insferred from "B" to "A"),
	 If we have three (or more) systems "A," "B," and " equilibrium with B, and B is in thermal equilibrium B, and C must all have the same temperature, and equilibrium with C. (This is akin to the transitive p mathematics.) 	n with C, this means that A, d A is therefore in thermal
	 If an object with a higher temperature (a "hotter" object with a lower temperature (a "colder" object object with higher temperature to the object with temperatures are the same (the objects are in the 	ct), heat will flow from the lower temperature until the

Details



	mernodynamics	rage. 113
Big Ideas	Details	Unit: Thermodynamics
	Sample Problem:	
	Q: A cylinder containing 1.8 mol of an ideal gas with a temperature of 275 K has a piston with a weight on top. combined mass of the piston plus the weight is 2.0 kg, ar the cross-sectional area of the piston is 0.01 m ² . The vol of the gas in the cylinder is 0.033 m ³ .	nd
	Heat is added, and the volume of the gas increases to 0.040 m ³ . How much heat was added to the gas?	o gas
	A: When the gas is heated, the following occur:	
	 In order to increase the volume, the gas has to expansion which means the temperature needs to increase. We know how much the volume increased, and the press remains constant (the piston pushes the same amount) 	e fure
	throughout the process). We can use $\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2}$ to f	ind
	the final temperature of the gas.	
	$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2} \rightarrow \frac{0.033}{275} = \frac{0.040}{T_2} \rightarrow$	$T_2 = 333 \mathrm{K}$
	2. The increase in temperature means the internal energy increased. We can use $\Delta U = \frac{3}{2}nR\Delta T$ to find out how	
	energy of the gas increased (ΔU). The equation ΔU = some of the heat energy needed to be used for the in energy, and the rest of it was used to do the work of r	crease in internal
	$\Delta U = \frac{3}{2} nR\Delta T \Rightarrow \Delta U = (\frac{3}{2})(1.8)(8.31)(333)$	3–275) = 1301 J
	3. We can calculate the work used to raise the piston from physics 1: $W = mg\Delta h$ (Note that $\Delta V = A\Delta h$.)	om the work equation
	$W = -mg\Delta h = -mg\frac{\Delta V}{A} = -(2)(10)\frac{0.007}{0.01} = -14$ J	
	The work is negative because the energy is going out (remember that the system is the gas) and into the su	•
	4. Once we have ΔU and W , we can find Q by applying	the first law:
	$\Delta U = Q + W$	
	1301 = Q + (-14)	
	1315 J=Q	

Alternatively, we could calculate the work using $W = -P\Delta V$, but we would need
to use gauge pressure rather than absolute pressure. (See the explanation
below.)

The first two steps are the same as above.

Big Ideas

Details

- 1. This step is the same as step #1 above—we need to find the temperature change necessary to produce the change in volume.
- 2. This step is the same as step #2 above—we need to calculate the change in internal energy of the gas caused by the change in temperature.
- 3. Instead of calculating the work using equations from physics 1, we can use $W = -P\Delta V$. However, pressure needs to be the amount of pressure that is doing the work, which is the difference in pressure between the inside of the piston and the outside of the piston. (This would be the gauge pressure inside the cylinder.) We can calculate this using the pressure equation from fluids in physics 1:

$$P = \frac{F}{A} = \frac{(2)(10)}{0.01} = 2\,000\,\text{Pa}$$

This is the pressure at which the gas needs to do work.

Once we have the pressure, the work is given by:

 $W = -P\Delta V$ $\Delta V = 0.040 - 0.033 = 0.007 \text{ m}^3$ W = -(2000)(0.007) = -14 J

4. Once we have ΔU and W, we can find Q by applying the first law:

 $\Delta U = Q + W$ 1301 = Q + (-14)1315 J = Q

-	-
Details	Unit: Thermodynamics
Second Law	
The Second law tells us that heat energy cannot flow from hotter one unless work is done on the system. This is why your ice cream melts.	•
One consequence of this law is that no machine can work machines generate some heat, and some of that heat is al surroundings.	•
Entropy	
Because energy must be conserved, we have to account for but has "gotten lost" ("escaped" or "spread out") and is no system. Energy that has spread out and cannot be recover	o longer usable by the
For example, when an egg falls to the floor and breaks, gra energy is converted to a combination of internal energy (t the temperature of the egg), and entropy (heat energy that environment and "lost"). Over time, the internal energy in to the environment and "lost" as the egg cools off. Ultimatic gravitational potential energy ends up converted to entro energy that is dissipated and cannot be recovered.	he measurable increase in at is radiated to the n the egg is also radiated ately, all of the
Entropy is sometimes called "disorder" or "randomness", sense this is not correct. The entropy of your room is a <i>th</i> the heat energy in your room, not a commentary on the a the floor!	ermodynamic property of
Whenever heat is transferred from an object with a higher with a lower temperature, the heat "spreads out" as it wa amount of energy that goes into this "spread" is called ent	rms the colder object. The
T ₁ (hot) $\Delta S = Entropy = \frac{Q}{T}$	T ₂ (cold)
	Second Law The Second law tells us that heat energy cannot flow from hotter one unless work is done on the system. This is why your ice cream melts. One consequence of this law is that no machine can work machines generate some heat, and some of that heat is al surroundings. Entropy Because energy must be conserved, we have to account for but has "gotten lost" ("escaped" or "spread out") and is n system. Energy that has spread out and cannot be recover For example, when an egg falls to the floor and breaks, greenergy is converted to a combination of internal energy (the the temperature of the egg), and entropy (heat energy the environment and "lost"). Over time, the internal energy it to the environment and "lost" as the egg cools off. Ultimated gravitational potential energy ends up converted to entrope energy that is dissipated and cannot be recovered. Entropy is sometimes called "disorder" or "randomness", sense this is not correct. The entropy of your room is a <i>th</i> the heat energy in your room, not a commentary on the at the floor! Whenever heat is transferred from an object with a higher with a lower temperature, the heat "spreads out" as it was amount of energy that goes into this "spread" is called en The spread sout" as it was amount of energy that goes into this "spread" is called en the floor!

If the heat could be transferred in a way that is completely reversible (which is impossible and would take an infinite amount of time), then you would be able to recover the energy that was converted to entropy when transferring it back to the hotter object. We call this fictitious heat "reversible heat," denoted Q_{rev} .

honors (not AP®)

Big Ideas

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 $\Delta S = \frac{Q_{rev}}{T}$

Real energy transfers that take place in finite amounts of time can never recover all of the energy that was turned into entropy. This means the actual increase in entropy is always more than the amount that would occur in a reversible process:

$$\Delta S = \frac{Q_{rev}}{T} \ge \frac{Q}{T}$$

In other words, the energy that is lost to entropy by transfer of an amount of heat Q

would be exactly $\frac{Q}{T}$ for a completely reversible process (*i.e.*, $Q = Q_{rev}$), and more

than that for any real process.

Because actual heat transfer in a finite amount of time cannot be completely reversible, some heat is lost to the surroundings and the actual entropy change is always greater than the actual heat change at a given temperature. The concept of a reversible process is an idealization that represents the maximum amount of work that could theoretically be extracted from the process.

Consequences of the Second Law

- The total entropy of an isolated system can never decrease and is constant only when all of the thermodynamic processes are reversible.
- Localized energy will tend to disperse (spread out). When this happens, thermal energy is lost to the surroundings, and the entropy of the system increases.
- Entropy is a state function, which means the entropy of a system does not depend on the energy pathway the system follows.
- Closed systems spontaneously move toward thermodynamic equilibrium (*i.e.*, all parts of the system have the same temperature). When a system has reached thermodynamic equilibrium, the system's entropy is maximized.
- Because the universe is a closed system, the entropy of the universe is always increasing.
- The entropy of an open system can be decreased through a transfer of energy into the system from the surroundings.

In physics, there is a hierarchy of thinking. Conservation of energy, conservation of momentum, and the Second Law are at the top of the hierarchy. Just as special relativity tells us that time, distance and mass all need to be changeable in order to maintain conservation of energy and momentum, the Second Law explains why time cannot move backwards—to do so would require a decrease in the entropy of the universe.

Third Law

Details

Big Ideas

The Third Law tells us that in an isolated system, the total energy of the system must be constant. (An isolated system is a system for which it is not possible to exchange energy with the surroundings.) This makes intuitive sense; because energy must be conserved, if no energy can be added or taken away, then the total energy cannot change.

Thermodynamic Quantities and Equations

Big Ideas

Details

Because energy is complex and exists in so many forms, there are many thermodynamic quantities that can be calculated in order to quantify the energy of different portions of a system. The following is a list of some of the more familiar ones:

Variable	Name	Description
Q	heat	Thermal energy (heat) transferred into or out of a system due to a difference in temperature.
W	work	Mechanical energy transferred into or out of a system through the action of a force applied over a distance. $W = \vec{F} \cdot \vec{d} = -P\Delta V$
U*	internal energy	Total thermal (non-chemical) energy contained within the particles of a system because of their kinetic energy. $U = \frac{3}{2}nRT \qquad \Delta U = Q + W = \frac{3}{2}nR\Delta T$
S	entropy	Energy that is "lost" (inaccessible) because it has spread to the surroundings or has spread to separate microstates and cannot be utilized by the particles of the system.
A	Helmholtz free energy	Useful work that could theoretically be obtained from a system. $A = U - TS \qquad \Delta A = \Delta U - T\Delta S$
Н	enthalpy	Heat energy available in a chemical reaction. $H = U + PV$ $\Delta H = \Delta U + P\Delta V = \Delta U - W$
G	Gibbs free energy	Total energy available in a chemical reaction. $G = H - TS$ $\Delta G = \Delta H - T\Delta S$

Selected Thermodynamic Quantities

Because this is a physics course, we will leave enthalpy and Gibbs free energy to the chemists.

* Some chemistry textbooks use the variable *E* instead of *U*.

Details

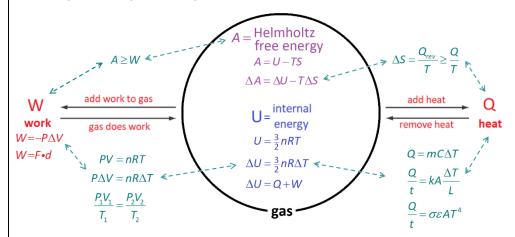
Big Ideas

Thermodynamics Equations Used in This Course

Most of the thermodynamics problems encountered in this course are applications of the following equations:

Equation	Quantities that are Changing	
$U = \frac{3}{2}nRT$ $\Delta U = \frac{3}{2}nR\Delta T$	internal energy vs. temperature	
$\Delta U = Q + W$	internal energy vs. heat & work	
$PV = nRT$ $P\Delta V = nR\Delta T$	pressure & volume vs. temperature	
$W = -P \Delta V^*$	work vs. volume	

What makes thermodynamics challenging is that there are many relationships between the quantities in these equations, as shown in the following thermodynamics equation map:



It is often necessary to combine equations. For example:

$$\Delta U = \frac{3}{2} nR\Delta T = Q + W$$
$$-W = P\Delta V = nR\Delta T$$

(Note that we moved the negative sign from $W = -P\Delta V$ to the other side of the equation.)

^{*} In an algebra-based course, we need to restrict ourselves to problems in which the pressure remains constant during volume changes. In a calculus-based course, this equation would be $W = -\int P dV$, where *P* is a function of *V*.

The problems that you will encounter will involve a change in a measurable state variable (pressure, volume and/or temperature). To solve these problems, you will need to:

- 1. Determine what the change involves:
 - heat transfer (Q)

Big Ideas

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- work (*W*) resulting from a change in volume (ΔV).
- a change in internal energy (ΔU) resulting from a change in temperature (ΔT).

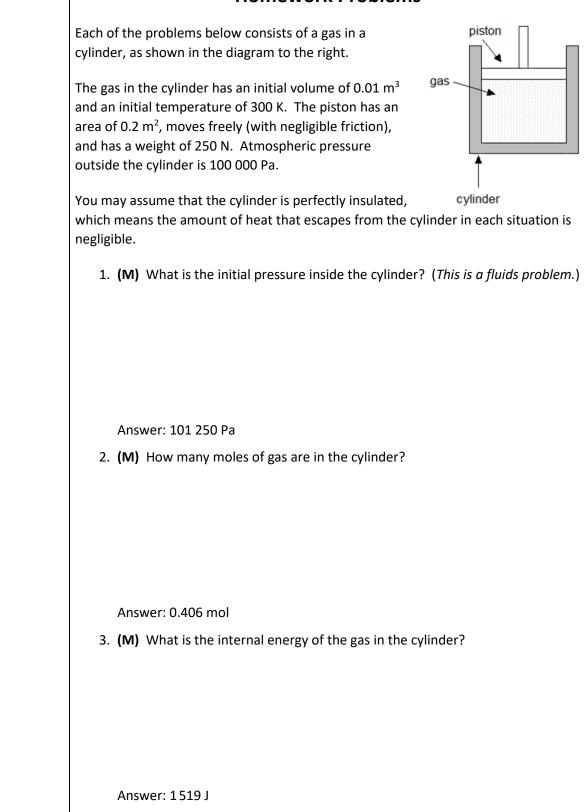
(There can be more than one of these happening at the same time.)

2. If necessary, determine initial and/or final values of these state variables in relation to other variables using equations such as:

•
$$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2}$$

- PV = nRT
- 3. Apply algebraic combinations of these equations to find each of the necessary quantities to answer the question.

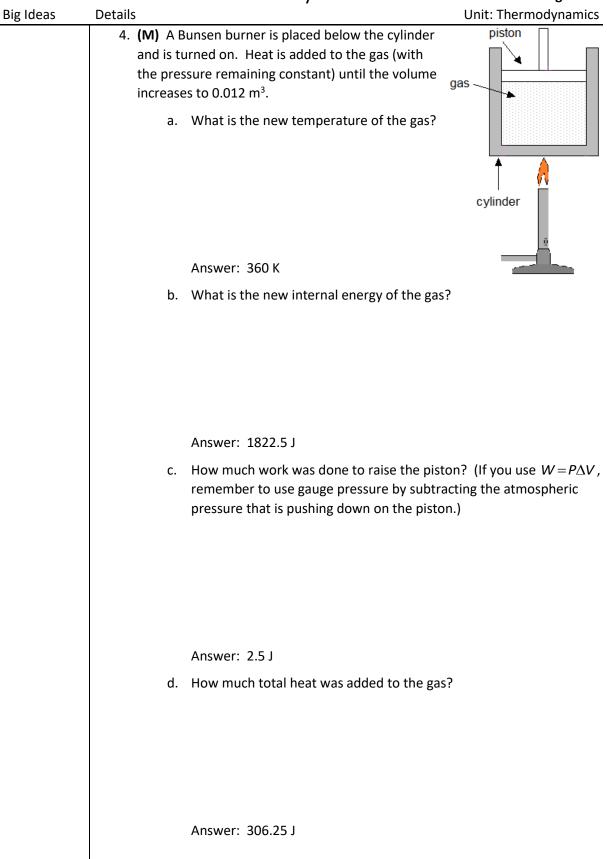
Homework Problems



Big Ideas

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Big Ideas	Details	5	Unit: Thermodynamics
	5.		ppose instead that the piston from problem #4 above was fixed in
		-	and was not allowed to move, so the volume remains constant at
		0.01 m³	while the 306.25 J of heat from question 4d was added.
		a.	What is the new temperature of the gas?
			Answer: 360.5 K
		b.	What is the new pressure of the gas?
			Answer: 121 667 Pa
		с.	If the piston is then released and allowed to move freely, what will
			the new pressure be inside the cylinder?
			Answer: 101 250 Pa (the same as in problem #1 above)

Details

Unit: Thermodynamics

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-6

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 9.4.B, 9.4.B.2, 9.4.B.2.i, 9.4.B.ii, 9.4.B.3

Mastery Objective(s): (Students will be able to ...)

• Determine changes in heat, work, internal energy and entropy from a pressure-volume (PV) diagram.

Success Criteria:

- Correct equation is chosen.
- Solutions have the correct quantities substituted for the correct variables.
- Sign is correct for work (positive vs. negative).
- Algebra is correct.

Language Objectives:

- Explain what is physically happening to a gas for each section of a PV diagram.
- Tier 2 Vocabulary: internal, energy, heat, work

Notes:

P-V diagram: a graph that shows changes in pressure vs. changes in volume.

Recall that:

$W = -\int P dV$

On a graph, the integral is the area "under the curve" (meaning the area between the curve and the *x*-axis).

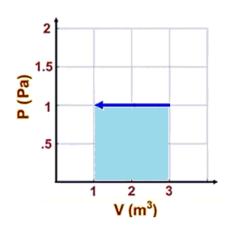
Therefore, if we plot a graph of pressure vs. volume with pressure on the y-axis and volume on the x-axis, the integral would therefore be represented by the area between the curve (pressure) and the x-axis.

This means that the work done by a thermodynamic change equals the area under a P-V graph.*

^{*} While the above explanation requires calculus, as stated earlier we will limit ourselves to areas that can be calculated using simple geometry equations. Note that some of these will result in situations that would not be realistically achievable in the "real world".

Big Ideas Details

In the following example, suppose that a gas is compressed from 3 m^3 to 1 m^3 at a pressure of 1 Pa. (A pressure of 1 Pa is much smaller than you would encounter in any real problem; these numbers were chosen to keep the math simple.)



The pressure is P = 1 Pa, and the change in volume is $\Delta V = -2$ m³. Because pressure is constant, we can use $W = -P\Delta V = -(1)(-2) = +2$ J.

 $P\Delta V$ is the area under the graph. Because it is a rectangular region, the area is the base of the rectangle times the height. The base is 2 m³ and the height is 1 Pa, which gives an area of 2 J.

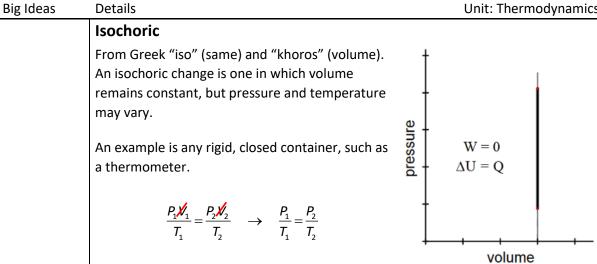
Note that the arrow showing the change points to the <u>left</u>, which indicates that the volume is <u>decreasing</u>. Because work must be put <u>into</u> the gas in order to compress it, this means that the work done **on** the gas will be positive.^{*} This is where the negative sign comes from. $W = -P\Delta V$ means that:

- If work is done on the gas (work is positive), the gas is compressed and the change in volume is therefore negative.
- If work is done by the gas on the surroundings (work is negative), the gas expands and the change in volume is therefore positive.

We will look at the effects of changes in pressure *vs.* volume in four types of pressure-volume changes:

- isochoric (constant volume)
- isothermal (constant temperature)
- adiabatic (no heat loss)
- isobaric (constant pressure).

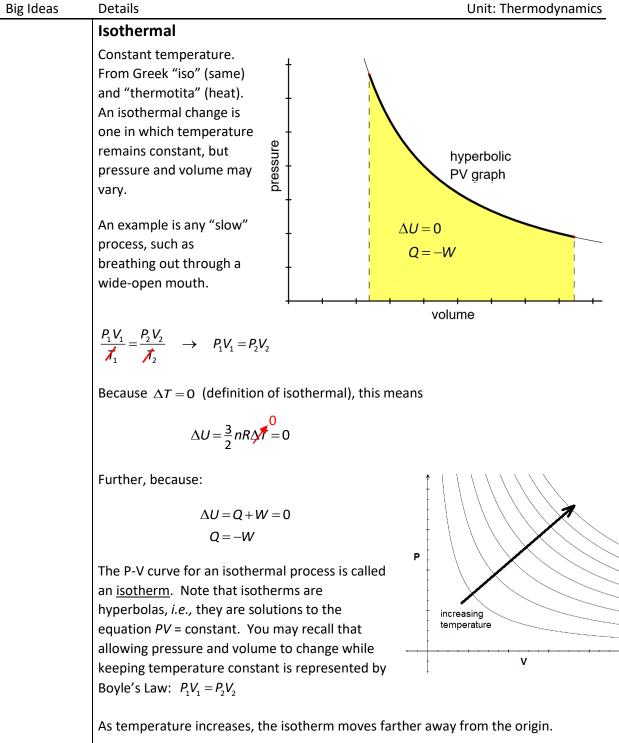
^{*} Unless explicitly stated otherwise, positive work means work done **on** the gas, meaning that energy is added to the gas and the internal energy of the gas increases.

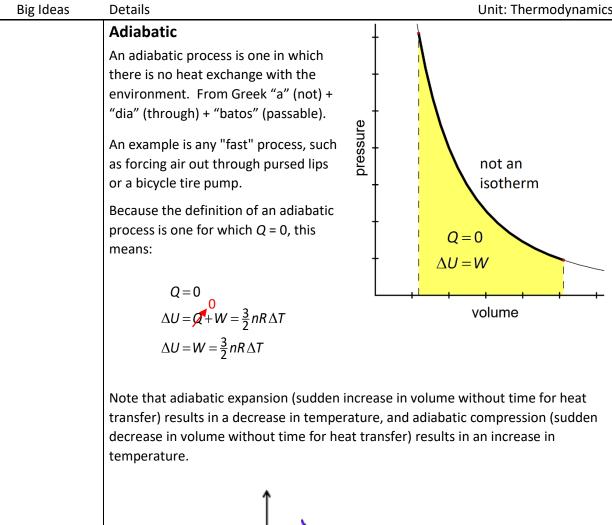


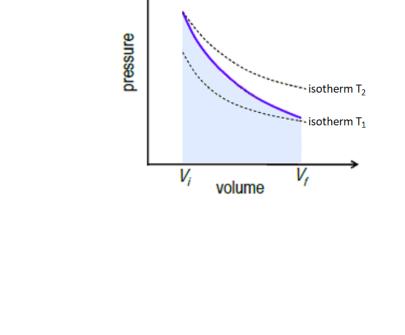
Because the volume is not changing, there is no way for the gas to displace anything. (Recall from Physics 1 that $W = \vec{F} \cdot \vec{d}$.) If there is no displacement, there is no work, which means W = 0.

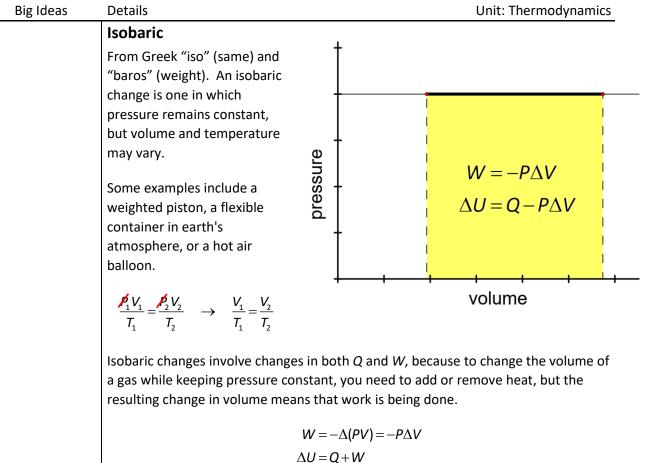
$$\Delta U = Q + W = \frac{3}{2} nR \Delta T$$
$$\Delta U = Q = \frac{3}{2} nR \Delta T$$

Another way to think of a constant volume change is that if you add heat to a rigid container of gas, none of the energy can be converted to work, so all of it must be converted to an increase in internal energy (*i.e.*, an increase in temperature).









$$\Delta U = Q + (-P\Delta V)$$
$$\Delta U = Q - P\Delta V$$

Adding $P\Delta V$ to both sides gives $Q = \Delta U + P\Delta V$.

Now, because $\Delta U = \frac{3}{2}nR\Delta T$ and $P\Delta V = nR\Delta T = \frac{2}{2}nR\Delta T$, that means:

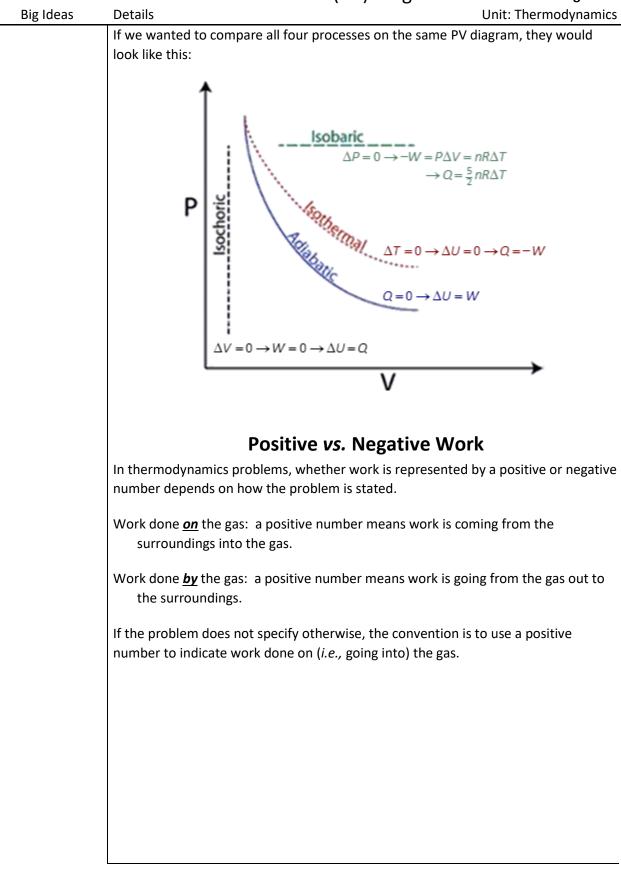
$$Q = \Delta U + P\Delta V$$

$$\downarrow \qquad \downarrow \qquad \downarrow$$

$$Q = \frac{3}{2}nR\Delta T + \frac{2}{2}nR\Delta T$$

$$Q = \frac{5}{2}nR\Delta T$$

This makes sense, because some of the heat is used to do the work of expanding the gas $(P\Delta V = nR\Delta T)$, and some of the heat is used to increase the temperature. $(\Delta U = \frac{3}{2} nR\Delta T)$.



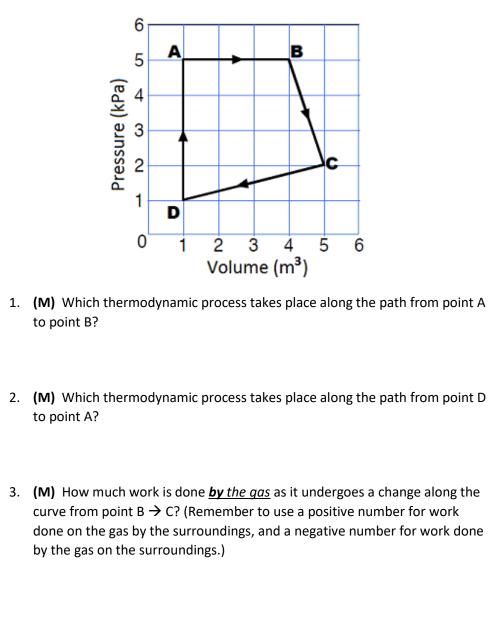
Big Ideas	Details	Unit: Thermodynamics
	Sample Problem	
	Q: Calculate the work done as the pressure and volume of a ground to point A to point B along each of paths 1, 2, and 3.	gas are taken from
	V (10 ⁻³ m ³)	
	A: Process #1 is first isobaric (constant pressure), then isocho	oric (constant volume).
	For the isobaric part of the process:	
	$W = -P\Delta V$	
	$W = -(1 \times 10^5)(1 \times 10^{-3} - 3 \times 10^{-3})$	
	$W = -(1 \times 10^5)(-2 \times 10^{-3})$	
	$W = 2 \times 10^2 = 200 \text{ J}$	
	For the isochoric process, there is no change in volume, w does no work (because it cannot push against anything).	-
	The total work for process #1 is therefore 200 J.	
	Notice that the work is equal to the area under the PV gra rectangular area with a base of 2×10^{-3} m ³ and a height of	
	$W = (1 \times 10^5)(2 \times 10^{-3}) = 200 \text{ J}$	
	Note that because the arrow points to the left, this means <i>decreasing</i> . That means <i>work is being done on the gas</i> , where <i>represented by a positive number</i> . (We have to make this time we use the graph to calculate the work.)	hich means the <i>work is</i>
	For process #2, the area is the 200 J square that we calcula plus the area of the triangle above it, which is $\frac{1}{2}bh = \frac{1}{2}(2 \times 10^{-5})$ Therefore, 200 J + 100 J = 300 J.	•
	For process #3, the area under the curve is $W = (2 \times 10^5)(2$	$\times 10^{-3}) = 400 \text{ J}.$

Details

Big Ideas

Homework Problems*

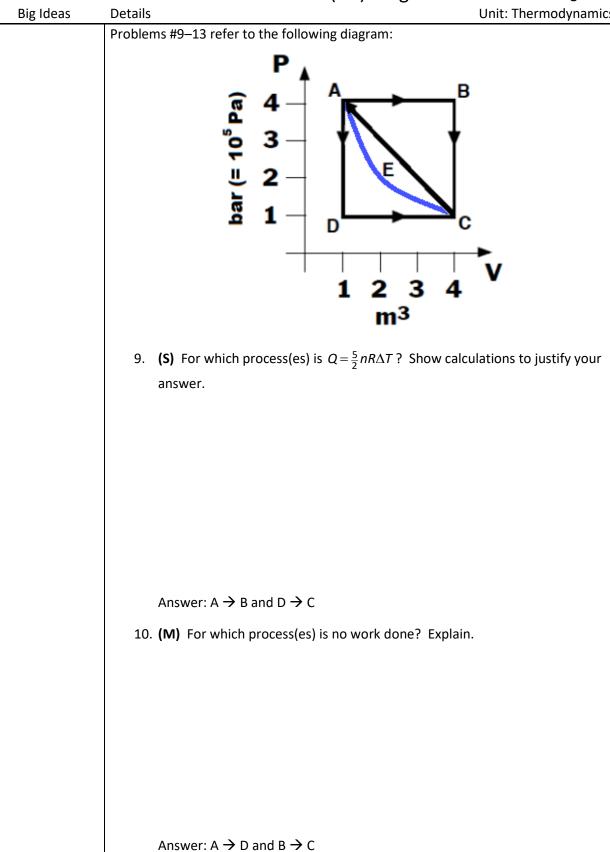
Problems #1–8 refer to the following PV diagram, in which 2 moles of gas undergo the pressure and volume changes represented by the path from point A to B to C to D and back to A.



Answer: +3500 J

* These problems are from a worksheet by Tony Wayne.

		Pressure-Volume (PV) Diagrams	Page: 135
Big Ideas	Details		Unit: Thermodynamics
	4.	(S) How much work is done <u>on the gas</u> as it underg curve from point C \rightarrow D?	oes a change along the
		Answer: +6000 J	
	5.	(S) How much net work is done <u>by the gas</u> on the s undergoes a change along the curve from point A $-\frac{1}{2}$	
		Answer: +12 500 J	
	6.	(S) What is the temperature of the 2 moles of gas a	at point A?
		Answer: 300.8 K	
	7.	(M) What is the change in internal energy of the gas from point D \rightarrow A?	as during the process
		Answer: 6000 J	
	8.	(M) How much work is done on or by the gas durin $D \rightarrow A$?	g the process from point
		Answer: zero	



	Pressure-volume (PV) Diagrams	Page: 137
Big Ideas E	Details	Unit: Thermodynamics
	11. (M) Which thermodynamic process takes place alor	g path E?
	12. (M) Calculate the heat exchanged in process A → B released? Explain.	? Is heat added or
	Answer: 3×10^6 J; heat is added because the temper 13. (M) Does path $A \rightarrow D \rightarrow C \rightarrow E \rightarrow A$ require more o $A \rightarrow D \rightarrow C \rightarrow A$? Explain.	
	14. (S) Calculate the work done <u>by the gas</u> in processes A → D → C → A.	A → B → C → A and
	Answer: A \rightarrow B \rightarrow C \rightarrow A: 450 000 J A \rightarrow D \rightarrow C \rightarrow A: -450 000 J	

(not AP[®]) Unit: Thermodynamics

Details

Big Ideas

honors

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-6

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): N/A

Mastery Objective(s): (Students will be able to ...)

• Calculate the energy produced or used by a heat engine.

Success Criteria:

- Correct equation is chosen.
- Solutions have the correct quantities substituted for the correct variables.
- Sign is correct for work (positive vs. negative).
- Algebra is correct.

Language Objectives:

• Explain what is happening to a gas through each of the steps of a heat engine cycle.

Tier 2 Vocabulary: internal, energy, heat, engine, work

Labs, Activities & Demonstrations:

• Stirling engine

Notes:

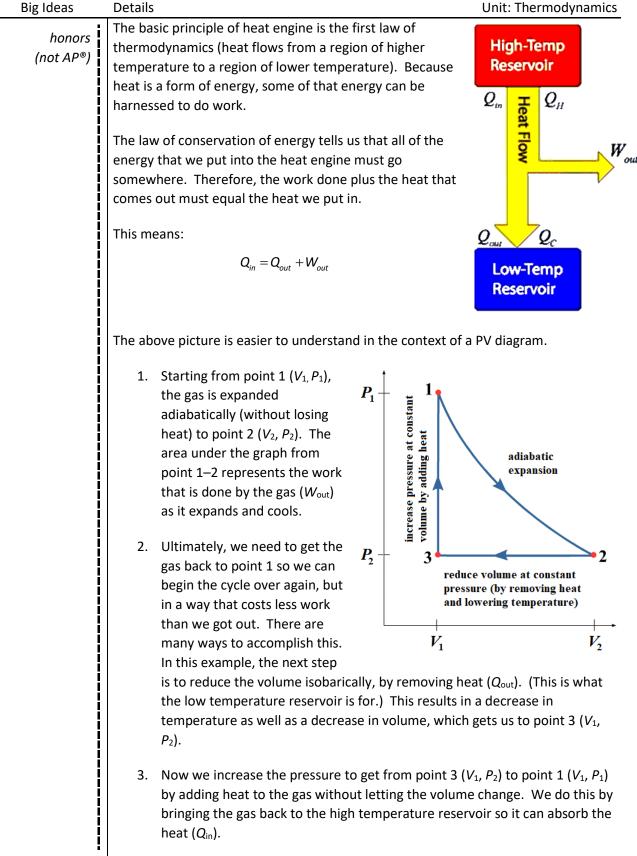
heat engine: a device that turns heat energy into mechanical work.

A heat engine operates by taking heat from a hot place (heat source), converting some of that heat into work, and dumping the rest of the heat into a cooler reservoir (heat sink).

A large number of the machines we use—most notably cars—employ heat engines.

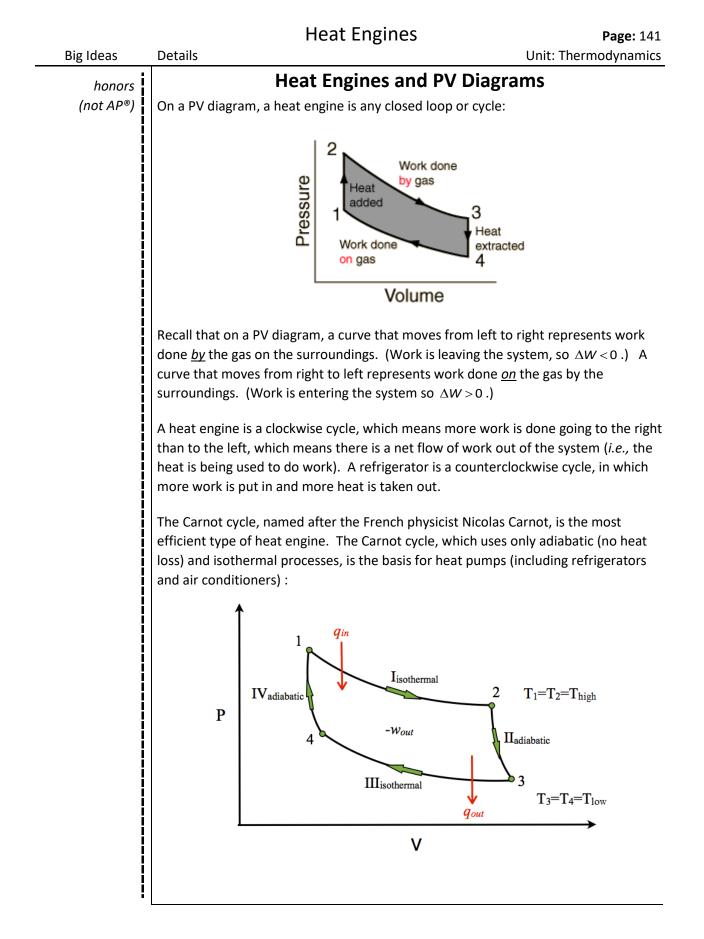
Heat Engines

Page: 139 Unit: Thermodynamics



Heat Engines

	neat Lingines	Page: 140		
Big Ideas	Details	Jnit: Thermodynamics		
honors	Heat Pumps			
(not AP®)	A heat pump is a device, similar to a heat engine, that "pumps" heat from one place to another. A refrigerator and an air conditioner are examples of heat pumps. A refrigerator uses a fluid ("refrigerant") to transfer (or "pump") heat from the inside of the refrigerator to the outside of the refrigerator (and into your kitchen).			
	This is why you can't cool off the kitchen by leaving the refriger even if you had a 100 % efficient refrigerator (most refrigerator 20–40 % efficient), all of the heat that you pumped out of the r the kitchen!	rs are actually only		
	A refrigerator works by the following process.			
	 Work is put in to compress a refrigerant (gas). In most of compressed until it turns into a liquid, which means add stored in the phase change. This increases the tempera to about 70 °C. 	litional energy is		
	 The refrigerant (now a liquid) passes through cooling co refrigerator. The liquid is cooled through convection by to about 25 °C 			
	 The refrigerant (still a liquid) is pumped to the inside of allowed to expand to a gas adiabatically. Work comes o temperature drops to about −20 °C. 	-		
	 Heat is transferred via convection from the contents (th refrigerant. 	e food) to the		
	 The refrigerant (still a gas) is pumped out of the refriger back to step 1. 	ator, which brings us		
	5 1 compressor 4 Refrigerator compartment 3			
	A heater can operate under the same principle, by putting the the room and having the expansion (which cools the refrigeran Individual rooms in homes are sometimes heated and cooled b pumps called "mini-splits".	t) occur outside.		



Big Ideas	Details	Unit: Thermodynamic
honors (not AP®)	The internal combustion engine in a car is also a typ called a "four-stroke" engine, because the piston ma motion) in one complete cycle. The four strokes are	akes four strokes (a back or fort
	 The piston moves down (intake), sucking a mathe cylinder. The piston moves up (compression), compressing the gases in the cylinder. The spark plug creates a spark, which combusts the gases. This increases the temperature in the cylinder to approximately 250°C. The gas expands (power stroke), which is the work that the engine provides to make the car go. The piston raises again, forcing the exhaust g (exhaust). Note that, at the end of the cycle, the gas is hotter the hot gas from the cylinder is dumped out the exhaust g is added. This is why the blue intake arrow the intake is at a lower temperature (lower isotherm). The energy to move the piston for the intake and expower strokes of the other pistons. This cycle—constant temperature compression, con constant temperature expansion (power), and const (exhaust) is called the Otto cycle, named after Nikolitype of heat engine to build the first commercially significant. 	power stroke ssion exhaust intake v sases out of the cylinder than its original temperature. haust pipe, and fresh (cool) gas on the right moves downward n). thaust strokes is provided by the stant volume heating (spark), tant volume gas exchange aus August Otto, who used this

Heat Engines

(not AP[®]) Unit: Thermodynamics

Details

Big Ideas

honors

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-6

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): N/A

Mastery Objective(s): (Students will be able to ...)

• Calculate the efficiency of a thermodynamic process.

Success Criteria:

- Correct equation is chosen.
- Solutions have the correct quantities substituted for the correct variables.
- Sign is correct for work (positive vs. negative).
- Algebra is correct.

Language Objectives:

• Explain how the efficiency of a process relates to the energy it uses and the work it produces.

Tier 2 Vocabulary: energy, heat, work

Notes:

<u>efficiency</u> (η): the ratio of the energy consumed by a device or process to the energy output by the device or process.

Assume that a heat engine starts with a certain temperature, which means a certain internal energy (U). The engine takes heat from a heat source at the incoming temperature T_{in} , does work (W), and exhausts heat at the higher temperature T_{out} . Assuming the internal energy of the machine itself stays constant, this means $\Delta U = 0$. Therefore, from the First law:

$$\Delta U = 0 = \Delta Q - \Delta W$$
$$0 = Q_{in} - Q_{out} - \Delta W$$
$$\Delta W = Q_{in} - Q_{out}$$

A 100% efficient heat engine would turn all of the heat into work, and would exhaust no heat ($Q_{out} = 0$, which would mean $\Delta W = Q_{in}$). Of course, real engines cannot do this, so we define efficiency, e, as the ratio of work out to heat in, *i.e.*:

$$e = \frac{\Delta W}{\Delta Q_{in}} = \frac{\Delta Q_{in} - \Delta Q_{out}}{\Delta Q_{in}} = \frac{\Delta Q_{in}}{\Delta Q_{in}} - \frac{\Delta Q_{out}}{\Delta Q_{in}} = 1 - \frac{\Delta Q_{out}}{\Delta Q_{in}}$$

Because the engine is doing work, $\Delta W > 0$, which means $0 \le e \le 1$. Furthermore, a consequence of the Second law is that some energy is always lost to the surroundings (entropy), which means $Q_{out} > 0$ and therefore $0 \le e < 1$.

Page: 1		Efficiency		Dotaile	
Unit: Thermodynam			oblem	Details	Big Ideas
Sample Problem Q: 80. J of heat is injected into a heat engine, causing it to do work. The engine the exhausts 20. J of heat into a cool reservoir. What is the efficiency of the engine?				honors (not AP®)	
A: $Q_{in} = 80 \text{ J}$ and $Q_{out} = 20 \text{ J}$. Therefore:					
$e = 1 - \frac{\Delta Q_{out}}{\Delta Q_{in}} = 1 - \frac{20}{80} = 1 - 0.25 = 0.75$					
would say that the	rcent	y is usually expressed as a pe efficient.	ciency is usua 75% efficient		
ed to heat that is giver	rgy is	-	n all of these rroundings.		
-	1	Energy Conversio			
fficiency		evice/Process			
9 40%		sgenerator			
5%		al/gas-fired power plant			
)%		mbined cycle power plant			i
90%		droelectric power plant	-		İ
o 59%			wind turbi		
		lar cell	solar cell		i
sually 15%	6-				
sually 15% 9 85%	6-	drogen fuel cell	hydrogen f		
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9 85% 5% 90% 99% 0 6% 27%		rdrogen fuel cell ternal combustion engine ectric motor, small (10–200 W ectric motor, large (> 200 W) notosynthesis in plants iman muscle frigerator	internal co electric mo electric mo photosynth human mu refrigerato refrigerato		
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9 85% 5% 90% 99% 0 6% 27% 0% 50% -5%		rdrogen fuel cell ternal combustion engine ectric motor, small (10–200 W ectric motor, large (> 200 W) notosynthesis in plants iman muscle frigerator frigerator, energy-saving ht bulb, incandescent	internal co electric mo electric mo photosyntl human mu refrigerato refrigerato light bulb, light bulb,		
9 85% 5% 90% 99% 0 6% 27% 27% 50% 50% -5%		rdrogen fuel cell ternal combustion engine ectric motor, small (10–200 W ectric motor, large (> 200 W) notosynthesis in plants iman muscle frigerator frigerator, energy-saving tht bulb, incandescent ht bulb, fluorescent	internal co electric mo photosynth human mu refrigerato light bulb, light bulb,		

Efficiency

honors (not AP®) Details

Big Ideas

You may notice that an electric heater is 100% efficient, because all of its energy is converted to heat. However, this does not mean that electric heat is necessarily the best choice for your home, because the power plant that generated the electricity is probably only 45% efficient.

Heating Efficiency

Heating efficiency is calculated in a similar way. The difference is that the energy produced by the heater *is* Q_{out} , which means:

 $\eta = \frac{Q_{out}}{Q_{in}} = \frac{\text{usable heat out}}{\text{total energy in}}$

"Usable heat out" means heat that is not lost to the environment. For example, if the boiler or furnace in your house is 70% efficient, that means 70% of the energy from the gas or oil that it burned was used to heat the steam, hot water or hot air that was used to heat your house. The other 30% of the energy heated the air in the boiler or furnace, and that heat was lost to the surroundings when the hot air went up the chimney.

Older boilers and furnaces (pre-1990s) were typically 70% efficient. Newer boilers and furnaces are around 80% efficient, and high-efficiency boilers and furnaces that use heat exchangers to collect the heat from the exhaust air before it goes up the chimney can be 90–97% efficient.

Efficiency of a Heat Pump

Carnot's theorem states that the maximum possible efficiency of a heat pump is related to the ratio of the temperature of the heat transfer fluid (liquid or gas) when it enters the heat pump to the temperature when it exits:

$$\eta \le 1 - \frac{T_{in}}{T_{out}}$$

Note that the Carnot equation is really the same as the efficiency equation in the previous section. Recall that for heating or cooling a substance:

$$Q = mC\Delta T = mC(T_{out} - T_{in})$$

The refrigerant is the same substance, which means mC is the same for the input as for the output, and it drops out of the equation.

Efficiency

Big Ideas	Details Unit: Thermodynamics
honors (not AP®)	It is a little counter-intuitive that a higher temperature difference means the heat pump is more efficient, but you should think about this in terms of heat transfer. (See the section on Heat Transfer starting on page 43.) Recall from Fourier's Law of Conduction that a higher temperature difference means a higher rate of heat transfer from one side to the other. In other words, the more heat you pump into the refrigerant, the higher its temperature will be when it leaves the system, and therefore the more efficiently the pump is moving heat. Conversely, if $T_{out} = T_{in}$, then the heat pump cannot transfer any heat, and the efficiency is zero.
	Sample Problem
	Q: Refrigerant enters a heat pump at 20. °C (293 K) and exits at 300. °C (573 K). What is the Carnot efficiency of this heat pump?
	A: Carnot's equation states that:
	$\eta = 1 - \frac{T_{in}}{T_{out}} = 1 - \frac{293}{573}$
	$\eta = 1 - 0.51 = 0.49$
	<i>I.e.,</i> this heat pump is 49% efficient.
ļ	

5	Introduction: Electric Force, Field & Potential Page: 147
Big Ideas	Details Unit: Electric Force, Field & Potential
	Introduction: Electric Force, Field & Potential
	Unit: Electric Force, Field & Potential
	Topics covered in this chapter:
	Electric Charge153
	Electric Permittivity159
	Coulomb's Law161
	Electric Fields and Electric Potential167
	Electric Field Vectors179
	Equipotential Lines & Maps182
	This chapter discusses static electric charges, how they behave, and how they relate to each other.
	• <i>Electric Charge</i> and <i>Coulomb's Law</i> describe the behavior of individual charged particles and their effects on each other.
	• <i>Electric Fields</i> describes the behavior of an electric force field on charged particles.
	• <i>Electric Field Vectors</i> and <i>Equipotential Lines & Maps</i> describe ways of representing electric fields in two dimensions.
	Standards addressed in this chapter:
	NGSS Standards/MA Curriculum Frameworks (2016):
	HS-PS2-4. Use mathematical representations of Newton's Law of Gravitation and Coulomb's Law to describe and predict the gravitational and electrostatic forces between objects.
	HS-PS3-1. Use algebraic expressions and the principle of energy conservation to calculate the change in energy of one component of a system when the change in energy of the other component(s) of the system, as well as the total energy of the system including any energy entering or leaving the system, is known. Identify any transformations from one form of energy to another, including thermal, kinetic, gravitational, magnetic, or electrical energy, in the system.
	HS-PS3-2. Develop and use a model to illustrate that energy at the macroscopic scale can be accounted for as either motions of particles and objects or energy stored in fields.

Big Ideas	Details	Unit: Electric Force, Field & Potential
	HS-PS	3-5. Develop and use a model of magnetic or electric fields to illustrate the
		prces and changes in energy between two magnetically or electrically
		narged objects changing relative position in a magnetic or electric field, espectively.
AP [®] only	AP [®] Phy	ysics 2 Learning Objectives/Essential Knowledge (2024):
		A: Describe the electric force that results from the interactions between narged objects or systems.
	10.:	1.A.1 : Charge is a fundamental property of all matter.
	10	0.1.A.1.i : Charge is described as positive or negative.
	1(0.1.A.1.ii : The magnitude of the charge of a single electron or proton, the elementary charge <i>e</i> , can be considered to be the smallest indivisible amount of charge.
	10	0.1.A.1.iii: The charge of an electron is −e, the charge of a proton is +e, and a neutron has no electric charge.
	10	0.1.A.1.iv : A point charge is a model in which the physical size of a charged object or system is negligible in the context of the situation being analyzed.
	10.:	1.A.2 : Coulomb's law describes the electrostatic force between two charged objects as directly proportional to the magnitude of each of the charges and inversely proportional to the square of the distance between the objects.
	10.:	1.A.3 : The direction of the electrostatic force depends on the signs of the charges of the interacting objects and is parallel to the line of separation between the objects.
	10	0.1.A.3.i : Two objects with charges of the same sign exert repulsive forces on each other.
	10	0.1.A.3.ii : Two objects with charges of opposite signs exert attractive forces on each other.
	10.3	1.A.4 : Electric forces are responsible for some of the macroscopic properties of objects in everyday experiences. However, the large number of particle interactions that occur make it more convenient to treat everyday forces in terms of nonfundamental forces called contact forces, such as normal force, friction, and tension.
		B: Describe the electric and gravitational forces that result from iteractions between charged objects with mass.
	10.:	1.B.1 : Electrostatic forces can be attractive or repulsive, while gravitational forces are always attractive.

	Introduction: Electric Force, Field & Potential Page: 149
Big Ideas	Details Unit: Electric Force, Field & Potential
AP® only	10.1.B.2 : For any two objects that have mass and electric charge, the magnitude of the gravitational force is usually much smaller than the magnitude of the electrostatic force.
	10.1.B.3: Gravitational forces dominate at larger scales even though they are weaker than electrostatic forces, because systems at large scales tend to be electrically neutral.
	10.1.C : Describe the electric permittivity of a material or medium.
	10.1.C.1 : Electric permittivity is a measurement of the degree to which a material or medium is polarized in the presence of an electric field.
	10.1.C.2 : Electric polarization can be modeled as the induced rearrangement of electrons by an external electric field, resulting in a separation of positive and negative charges within a material or medium.
	10.1.C.3 : Free space has a constant value of electric permittivity, ε_0 , that appears in physical relationships.
	10.1.C.4 : The permittivity of matter has a value different from that of free space that arises from the matter's composition and arrangement.
	10.1.C.4.i: In a given material, electric permittivity is determined by the ease with which electrons can change configurations within the material.
	10.1.C.4.ii: Conductors are made from electrically conducting materials in which charge carriers move easily; insulators are made from electrically nonconducting materials in which charge carriers cannot move easily.
	10.2.A : Describe the behavior of a system using conservation of charge.
	10.2.A.1 : The net charge or charge distribution of a system can change in response to the presence of, or changes in, the net charge or charge distribution of other systems.
	10.2.A.1.i : The net charge of a system can change due to friction or contact between systems.
	10.2.A.1.ii: Induced charge separation occurs when the electrostatic force between two systems alters the distribution of charges within the systems, resulting in the polarization of one or both systems.
	10.2.A.1.iii : Induced charge separation can occur in neutral systems.
	10.2.A.2 : Any change to a system's net charge is due to a transfer of charge between the system and its surroundings.
	10.2.A.2.i : The charging of a system typically involves the transfer of electrons to and from the system.
	10.2.A.2.ii : The net charge of a system will be constant unless there is a transfer of charge to or from the system.

-	Introduction. Lieutric roice, rieu & Potential Page: 150
Big Ideas	Details Unit: Electric Force, Field & Potential
AP [®] only	10.2.A.3 : Grounding involves electrically connecting a charged system to a much larger and approximately neutral system (<i>e.g.,</i> Earth).
	10.3.A : Describe the electric field produced by a charged object or configuration of point charges.
	10.3.A.1 : Electric fields may originate from charged objects.
	10.3.A.2 : The electric field at a given point is the ratio of the electric force exerted on a test charge at that point to the charge of the test charge.
	10.3.A.2.i: A test charge is a point charge of small enough magnitude such that its presence does not significantly affect an electric field in its vicinity.
	10.3.A.2.ii: An electric field points away from isolated positive charges and toward isolated negative charges.
	10.3.A.2.iii : The electric force exerted on a positive test charge by an electric field is in the same direction as the electric field.
	10.3.A.3: The electric field is a vector quantity and can be represented in space using vector field maps
	10.3.A.3.i: The net electric field at a given location is the vector sum of individual electric fields created by nearby charged objects.
	10.3.A.3.ii: Electric field maps use vectors to depict the magnitude and direction of the electric field at many locations within a given region.
	10.3.A.3.iii: Electric field line diagrams are simplified models of electric field maps and can be used to determine the relative magnitude and direction of the electric field at any position in the diagram.
	10.3.B : Describe the electric field generated by charged conductors or insulators.
	10.3.B.1: While in electrostatic equilibrium, the excess charge of a solid conductor is distributed on the surface of the conductor, and the electric field within the conductor is zero.
	10.3.B.1.i : At the surface of a charged conductor, the electric field is perpendicular to the surface.
	10.3.B.1.ii: The electric field outside an isolated sphere with spherically symmetric charge distribution is the same as the electric field due to a point charge with the same net charge as the sphere located at the center of the sphere.
	10.3.B.2: While in electrostatic equilibrium, the excess charge of an insulator is distributed throughout the interior of the insulator as well as at the surface, and the electric field within the insulator may have a nonzero value.

Big Ideas	Details Unit: Electric Force, Field & Potential Page: 151
	10.4.A : Describe the electric potential energy of a system.
AP® only	10.4.A.1 : The electric potential energy of a system of two point charges equals the amount of work required for an external force to bring the point charges to their current positions from infinitely far away.
	10.4.A.2 : The general form for the electric potential energy of two charged objects is given by the equation $U_E = \frac{1}{4\pi\varepsilon_0} \cdot \frac{q_1q_2}{r} = k \frac{q_1q_2}{r}$.
	10.4.A.3 : The total electric potential energy of a system can be determined by finding the sum of the electric potential energies of the individual interactions between each pair of charged objects in the system.
	10.5.A : Describe the electric potential due to a configuration of charged objects.
	10.5.A.1 : Electric potential describes the electric potential energy per unit charge at a point in space.
	10.5.A.2: The electric potential due to multiple point charges can be determined by the principle of scalar superposition of the electric potential due to each of the point charges.
	10.5.A.3: The electric potential difference between two points is the change in electric potential energy per unit charge when a test charge is moved between the two points.
	10.5.A.3.i: Electric potential difference may also result from chemical processes that cause positive and negative charges to separate, such as in a battery.
	10.5.A.4: When conductors are in electrical contact, electrons will be redistributed such that the surfaces of the conductors are at the same electric potential.
	10.5.B : Describe the relationship between electric potential and electric field.
	10.5.B.1: The average electric field between two points in space is equal to the electric potential difference between the two points divided by the distance between the two points.
	10.5.B.2: Electric field vector maps and equipotential lines are tools to describe the field produced by a charge or configuration of charges and can be used to predict the motion of charged objects in the field.
	10.5.B.2.i : Equipotential lines represent lines of equal electric potential in space. These lines are also referred to as isolines of electric potential.
	10.5.B.2.ii: Isolines are perpendicular to electric field vectors. An isoline map of electric potential can be constructed from an electric field vector map, and an electric field map may be constructed from an isoline map.
	10.5.B.2.iii : An electric field vector points in the direction of decreasing potential.

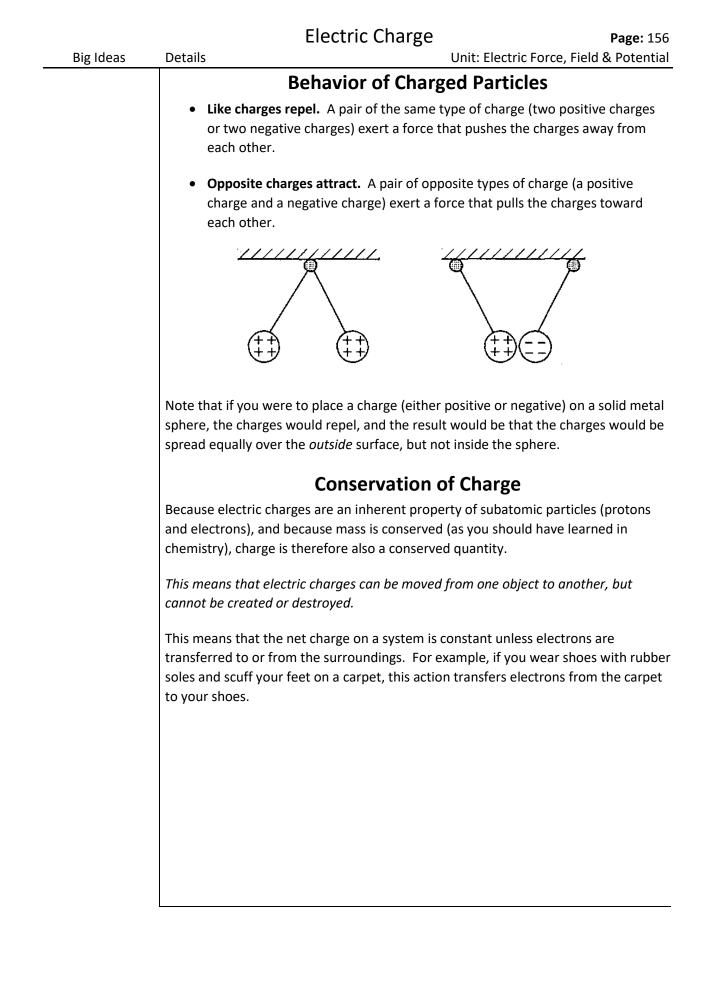
Big Ideas Details Unit: Electric Force, Field & Potential AP* only 10.5.8.2.iv: There is no component of an electric field along an isoline. 10.7.A. Describe changes in energy in a system due to a difference in electric potential between two locations. 10.7.A.1: When a charged object moves between two locations with different electric potentials, the resulting change in the electric potential energy of the object-field system is given by the following equation. 10.7.A.2: The movement of a charged object between two points with different electric potentials results in a change in Kinetic energy of the object consistent with the conservation of energy. Skills learned & applied in this chapter: • Working with isolines.	D : 11	Introduction: Electric Force, Field & Potential Page: 152	
 10.7.A: Describe changes in energy in a system due to a difference in electric potential between two locations. 10.7.A.1: When a charged object moves between two locations with different electric potentials, the resulting change in the electric potential energy of the object-field system is given by the following equation. 10.7.A.2: The movement of a charged object between two points with different electric potentials results in a change in kinetic energy of the object consistent with the conservation of energy. Skills learned & applied in this chapter: 	Big Ideas		
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object consistent with the conservation of energy. Skills learned & applied in this chapter:		10.7.A.2 : The movement of a charged object between two points with	
Skills learned & applied in this chapter:			
		object consistent with the conservation of energy.	
Working with isolines.		Skills learned & applied in this chapter:	
		Working with isolines.	

as Details	Electric Charge	Page: 1 it: Electric Force, Field & Potenti			
	Electric Cha	·			
Unit: Electric Force, Field & Potential NGSS Standards/MA Curriculum Frameworks (2016): HS-PS3-5					
				AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 10.1.A 10.1.A.1.i, 10.1.A.1.ii, 10.1.A.1.iii, 10.1.A.iv, 10.2.A, 10.2.A.1, 10. 10.2.A.1.ii, 10.2.A.1.iii, 10.2.A.2, 10.2.A.2.i, 10.2.A.2.ii, 10.2.A.3 Mastery Objective(s): (Students will be able to)	
• [Describe properties of positive and negative	electric charges.			
• [Describe properties of conductors and insula	tors.			
Succes	s Criteria:				
	/ariables are correctly identified and substite part of the correct equation.	uted correctly into the correct			
	Algebra is correct and rounding to appropria easonable.	te number of significant figures			
Langua	ge Objectives:				
•	Explain why the mass of the pendulum doe	es not affect its period.			
Tier 2	/ocabulary: charge				
Labs,	Activities & Demonstrations:				
•	charged balloon making hairs repel, attracti	ng water molecules.			
•	charged balloon sticking to wall (draw on or charges do not move)	ne side of balloon to show that			
•	charged balloon pulling meter stick				
•	build & demonstrate electroscope				
•	Wimshurst machine				
•	Van de Graaff generator				
	0				
Notes	:				
<u>charge</u>	<u>:</u>				
1.	A physical property of matter which causes near other electrically charged matter. (So charge".) Measured in coulombs (C).	•			
2.	A single microscopic object (such as a proto electric charge. (Sometimes called a "poin variable <i>q</i> .				
3.	The total amount of electric charge on a m accumulation of microscopic charged object				

Electric Charge

Big Ideas	Details Unit: Electric Force, Field & Potential
	4. (verb) To cause an object to acquire an electric charge.
	<u>positive charge</u> : the charge of a proton. Originally defined as the charge left on a piece of glass when rubbed with silk. The glass becomes positively charged because the silk pulls electrons off the glass.
	<u>negative charge</u> : the charge of an electron. Originally defined as the charge left on a piece of amber (or rubber) when rubbed with fur (or wool). The amber becomes negatively charged because the amber pulls the electrons off the fur.
	static electricity: stationary electric charge, such as the charge left on silk or amber in the above definitions.
	<u>elementary charge</u> : the magnitude (amount) of charge on one proton or one electron. One elementary charge equals 1.60×10^{-19} C. Because ordinary matter is made of protons and electrons, the amount of charge carried by any object must be an integer multiple of the elementary charge.
	Note however that quarks, which protons and neutrons are made of, carry fractional charges; up-type quarks carry a charge of $+\frac{1}{3}$ of an elementary charge, and down-type quarks carry a charge of $-\frac{1}{3}$ of an elementary charge. A proton is made of two up quarks and one down quark and carries a charge of $+1$ elementary charge. A neutron is made of one up quark and two down quarks and carries no charge.

		tric Charge Page: 155
Big Ideas	Detailselectric current(sometimes calledelectricity): themovement of electronsthrough a medium(substance) from onelocation to another.Note, however, thatelectric current isdefined as thedirection a positivelycharged particle wouldmove. Thus, electriccurrent "flows" in theopposite directionfrom the actualelectrons.	Unit: Electric Force, Field & Potential BENJAMIN FRANKLIN? / YES? I BRING A MESSAGE FROM THE FUTURE! I DON'T HAVE MUCH TIME. WHAT IS IT? I THE CONVENTION YOU'RE SETTING FOR ELECTRIC CHARGE IS BACKWARD. THE ONE LEFT ON GLASS BY SILK SHOULD BE THE NEGATIVE CHARGE.
		WE WERE GOING TO USE THE TIME MACHINE TO PREVENT THE ROBOT APOCALYPSE, BUT THE GUY WHO BUILT IT WAS AN ELECTRICAL ENGINEER. © xkcd.com. Used with permission.
	Some Devices t	hat Produce, Use or Store Charge
	capacitor: a device that store	s electric charge.
	battery: a device that uses ch	emical reactions to produce an electric current.
	generator: a device that conv current.	erts mechanical energy (motion) into an electric
	motor: a device that converts	an electric current into mechanical energy.
	Con	ductors vs. Insulators
	conductors include metal in them (such as salt wate	ows charges to move freely through it. Examples of s and liquids with positive and negative ions dissolved er). When charges are transferred to a conductor, the elves evenly throughout the substance.
	Examples of insulators inc	s not allow charges to move freely through it. clude nonmetals and most pure chemical compounds When charges are transferred to an insulator, they where they are placed.



Physics 2 In Plain English

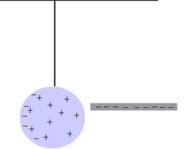
Big Ideas

Details

Charging by Induction

induction: when an electrical charge on one object causes a charge in a second object.

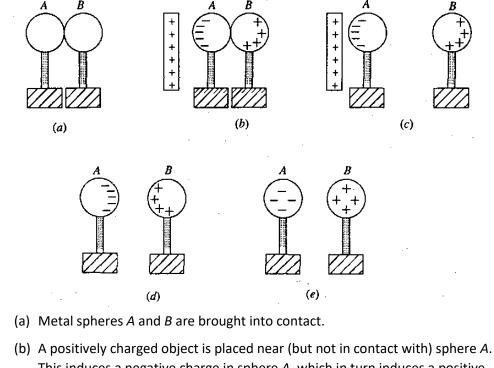
When a charged rod is brought near a neutral object, the charge on the rod attracts opposite charges and repels like charges that are near it. The diagram to the right shows a negatively charged rod repelling negative charges.



If the negatively charged rod were touched to the sphere, some of the charges from the rod

would be transferred to the sphere at the point of contact. This would cause the sphere to have an overall negative charge.

A procedure for inducing charges in a pair of metal spheres is shown below:



This induces a negative charge in sphere *A*, which in turn induces a positive charge in sphere *B*.

- (c) Sphere *B* (which is now positively charged) is moved away.
- (d) The positively charged object is removed.
- (e) The charges distribute themselves throughout the metal spheres.

Electric Charge

honors (not AP®)

Details

Big Ideas

Charge Density

The amount of electric charge on a surface is called the charge density. As with density (in the mass/volume sense), the variable used is usually the Greek letter rho with a subscript *q* indicating charge (ρ_q). Charge density can be expressed in terms of length, area, or volume, which means, the units for charge density can be $\frac{C}{m}, \frac{C}{m^2}, \text{ or } \frac{C}{m^3}.$

Grounding

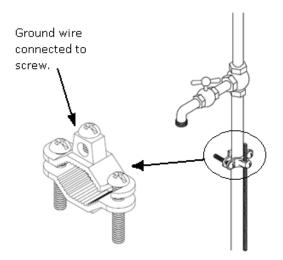
For the purposes of our use of electric charges, the ground (Earth) is effectively an endless supply of both positive and negative charges. Under normal circumstances, if a charged object is touched to the ground, electrons will move to neutralize the charge, either by flowing from the object to the ground or from the ground to the object.

Grounding a charged object or circuit means neutralizing the electrical charge on an object or portion of the circuit by connecting it to a much larger and approximately neutral system, such as the Earth.

The charge of any object that is connected to ground is zero, by definition.

The term "grounding" comes from the fact that this is often accomplished by connecting the system via a wire to a metal pipe or stake that is partially or fully buried in the ground.

In buildings, the metal pipes that bring water into the building are often used to ground the electrical circuits. The metal pipe is a good conductor of electricity and carries the unwanted charge out of the building and into the ground outside.



Electric Permittivity

Unit: Electric Force, Field & Potential

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-4

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): 10.1.A, 10.1.A.2, ,

10.1.A.3, 10.1.A.3.i, 10.1.A.3.ii, 10.1.A.4, 10.1.B, 10.1.B.1, 10.1.B.2, 10.1.B.3 Mastery Objective(s): (Students will be able to...)

- Solve problems using Coulomb's Law
- Quantitatively predict the effects on the electrostatic force when one of the variables (amount of electric charge or distance) in Coulomb's Law is changed.

Success Criteria:

Details

Big Ideas

- Variables are correctly identified and substituted correctly into the correct part of the correct equation.
- Algebra is correct and rounding to appropriate number of significant figures is reasonable.

Language Objectives:

• Explain how force and distance both affect the amount of force between two charged objects.

Tier 2 Vocabulary: charge

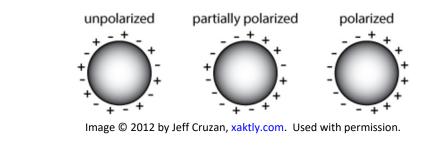
Notes:

<u>force field</u>: a region in which objects experience a force that is proportional to the amount that the object has of the property that the field acts upon.

electric field: a force field that acts upon objects with a nonzero electrical charge.

For example, in physics 1, you learned about the gravitational force field, which acts upon objects with mass. In the *Electric Fields* topic, starting on page 167, you will learn more about electric fields, which act upon objects with charge.

<u>polarized</u>: an object or region that has opposite values of some property at each end. An object is electrically polarized if one end is charged more positively or less negatively than the other.



Electric Permittivity

<u>electric permittivity</u>: the degree to which a material or medium is polarized in the presence of an electric field.

permittivity of free space (ε_{\circ}): the degree to which empty space (a vacuum) can support an electric field. The permittivity of free space is defined in terms of two constants: the magnetic permeability of a vacuum (μ_{\circ} ; see *Magnetism*, starting on page 280) and the speed of light (*c*).)

$$\varepsilon_o = \frac{1}{\mu_o c^2} = 8.85 \times 10^{-12} \frac{F}{m}$$

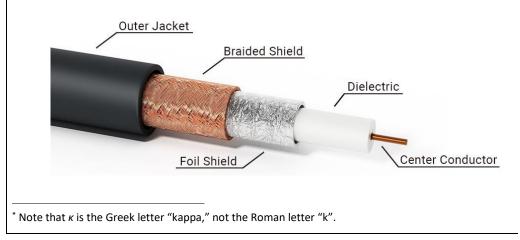
<u>relative permittivity</u> (dielectric constant) (κ^* or ε_r): the ratio of the electric permittivity of a substance to the electric permittivity of empty space.

A vacuum (empty space) has a relative permittivity of 1.

Relative permittivity is most often used to determine the ability of an insulating material to prevent electric charges from moving through itself. The lower the relative permittivity, the better the insulator.

Substance	к	Substance	к
vacuum	1	rubber	~7
air	1.0006	ethanol @ 25 °C	24.3
paper	1.4	methanol @ 25 °C	32.7
polyethylene	2.25	water @ 25 °C	78.4
silicon dioxide	3.9	calcium copper titanate	>250 000

Polyethylene is often used as a dielectric (insulator) between the center conductor and the outside shield in coaxial cables.



Big Ideas

Details

Unit: Electric Force, Field & Potential

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-4

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 10.1.A, 10.1.A.2, ,

10.1.A.3, 10.1.A.3.i, 10.1.A.3.ii, 10.1.A.4, 10.1.B, 10.1.B.1, 10.1.B.2, 10.1.B.3 Mastery Objective(s): (Students will be able to...)

- Solve problems using Coulomb's Law
- Quantitatively predict the effects on the electrostatic force when one of the variables (amount of electric charge or distance) in Coulomb's Law is changed.

Success Criteria:

Details

Big Ideas

- Variables are correctly identified and substituted correctly into the correct part of the correct equation.
- Algebra is correct and rounding to appropriate number of significant figures is reasonable.

Language Objectives:

• Explain how force and distance both affect the amount of force between two charged objects.

Tier 2 Vocabulary: charge

Labs, Activities & Demonstrations:

- Charged balloon or Styrofoam sticking to wall.
- Charged balloon pushing meter stick.
- Van de Graaff generator with negative electrode attached to inertia balance pan.

Notes:

Electric charge is measured in Coulombs (abbreviation "C"). One Coulomb is the amount of electric charge transferred by a current of 1 ampere for a duration of 1 second.

+1 C is the charge of 6.2415×10^{18} protons.

-1 C is the charge of 6.2415×10^{18} electrons.

A single proton or electron therefore has a charge of $\pm 1.6022 \times 10^{-19}$ C. This amount of charge is called the <u>elementary charge</u>, because it is the charge of one elementary particle.

An object can only have an integer multiple of this amount of charge, because it is impossible^{*} to have a charge that is a fraction of a proton or electron.

Because charged particles attract or repel each other, that attraction or repulsion must be a force, which can be measured and quantified. The force is directly proportional to the strengths of the charges, and inversely proportional to the square of the distance. The formula is:

$$F_e = \frac{1}{4\pi\varepsilon_o} \cdot \frac{q_1 q_2}{r^2} = k \frac{q_1 q_2}{r^2}$$

where:

Details

Big Ideas

- F_e = electrostatic force of repulsion between electric charges. A positive value of F_e denotes that the charges are repelling (pushing away from) each other; a negative value of F_e denotes that the charges are attracting (pulling towards) each other.[†]
- ε_{o} = electric permittivity of free space $\approx 8.85 \times 10^{-12} \frac{F}{m}$.

$$k = \text{electrostatic constant} = = \frac{1}{4\pi\varepsilon_o} \approx 9.0 \times 10^9 \frac{\text{N} \cdot \text{m}^2}{\text{C}^2}.$$

 q_1 , q_2 = the charges on objects #1 and #2 respectively

r = distance (radius, because it goes outward in every direction) between the centers of the two charges

This formula is Coulomb's Law, named for its discoverer, the French physicist Charles-Augustin de Coulomb.

Coulomb's Law has several parallels with Newton's Law of Universal Gravitation:

$$F_g = G \frac{m_1 m_2}{r^2} \qquad \qquad F_e = k \frac{q_1 q_2}{r^2}$$

gravitational force

electrostatic force

The situations are similar in that there are two objects, each exerting a force on the other separated by some distance, r. With the gravitational force, masses can only attract, which means F_g is always attractive. However, F_e can be either attractive or repulsive, because charges attract or repel, depending on whether they have opposite or like signs. If the charges have the same sign (repulsive), the value of F_e will be positive; if the charges have opposite signs (attractive), the value of F_e will be negative.

^{*} This is true for macroscopic objects. Certain quarks, which are the particles that protons and neutrons are made of, have charges of $\frac{1}{3}$ or $\frac{2}{3}$ of an elementary charge.

⁺ It is unfortunate that a positive value for force denotes attraction in the gravitational force equation, but repulsion in the electrostatic force equation.

Big Ideas	Details	Unit: Electric Force, Field & Potential
	Sample problems:	
	Q: Find the force of electrostat hydrogen atom if the radius	c attraction between the proton and electron in a of the atom is 37.1 pm
	 A: The charge of a single proto is −1.60 × 10⁻¹⁹ C. 	n is 1.60 $ imes$ 10 ⁻¹⁹ C, and the charge of a single electron
	$37.1 \mathrm{pm} = 3.71 \times 10^{-11} \mathrm{m}$	
	$F_e = \frac{kq_1q_2}{r^2} = \frac{(8.99 \times 10^9)(1.6)}{(3.99)(1.6)}$	$\frac{0 \times 10^{-19})(-1.60 \times 10^{-19})}{71 \times 10^{-11})^2} = -1.67 \times 10^{-7} \mathrm{N}$
	However, rather than memory attraction or repulsion, it's e	ative, which signifies that the force is attractive. rize whether a positive or negative indicates asier to reason that the charges are opposite, so the prize what you can understand!
	separated by distance d. If the separated by distance d.	with charge $+q$ (which means $q_1 = q_2 = q$) are he amount of charge on one of the particles is halved what will be the effect on the force between them?
	A: To solve this problem, we fin	st set up Coulomb's Law:
	$F_e = \frac{kq_1q_2}{r^2}$	
	•	charges with half of itself—let's say q_1 will become e the distance r with (2 r). This gives:
	$F_e = \frac{k(0.5q_1)q_2}{(2r)^2}$	
	Simplifying and rearranging	this expression gives:
	$F_e = \frac{0.5kq_1q_2}{4r^2} = \frac{0.5}{4} \cdot \frac{kq_1q_2}{r^2} =$	$\frac{1}{8} \cdot \frac{kq_1q_2}{r^2}$
	Therefore, the new F_e will b	$\frac{1}{8}$ of the old F_e .
	L	

Details

Big Ideas

An easier way to solve this problem is to do a "before and after" calculation. Set the value of every quantity in the "before" equation to 1:

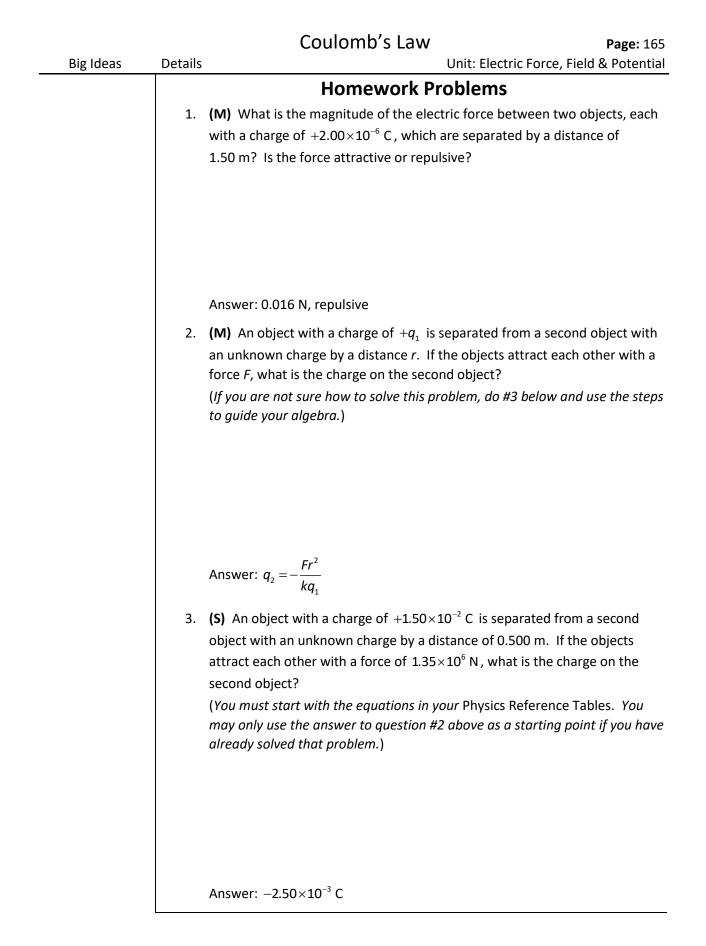
$$F_e = \frac{kq_1q_2}{r^2} \rightarrow \frac{1\cdot 1\cdot 1}{1^2} = 1$$

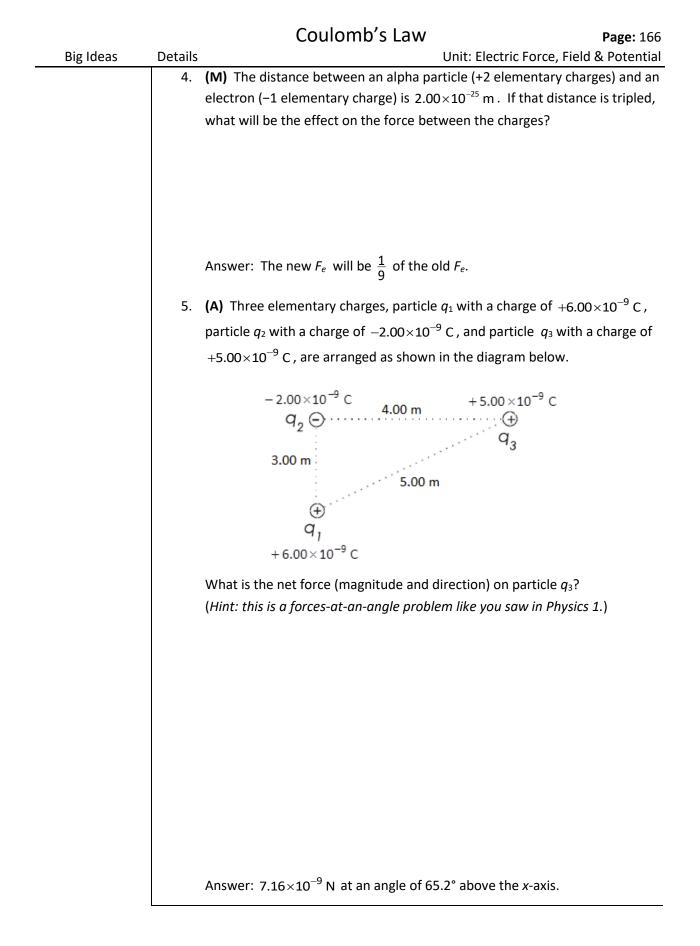
For the "after" equation, replace quantities that change with their multipliers:

$$F_e = \frac{kq_1q_2}{r^2} \rightarrow \frac{1 \cdot 1 \cdot 0.5}{2^2} = \frac{0.5}{4} = \frac{1}{8}$$

The "before" value for F_e was 1, and the "after" value was $\frac{1}{8}$, which means the new force will be $\frac{1}{8}$ of the original force.

This method is sometimes called "Bertha's Rule of Ones," or the "factor of change" method.





Electric Fields and Electric Potential

Unit: Electric Force, Field & Potential

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS3-1, HS-PS3-2, HS-PS3-5

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): 10.3.A, 10.3.A.1, 10.3.A.2, 10.3.A.2.i, 10.3.A.2.ii, 10.3.A.2.iii, 10.3.A.3, 10.3.A.3.i, 10.3.A.3.ii, 10.3.A.3.iii, 10.3.B, 10.3.B.1, 10.3.B.1.ii, 10.3.B.1.ii, 10.3.B.2, 10.4.A, 10.4.A.1, 10.4.A.2, 10.4.A.3, 10.5.A, 10.5.A.1, 10.5.A.2, 10.5.A.3, 10.5.A.3.i, 10.5.A.4

Mastery Objective(s): (Students will be able to ...)

- Sketch electric field lines and vectors around charged particles or objects.
- Solve problems involving the forces on a charge due to an electric field.

Success Criteria:

- Sketches show arrows pointing from positive charges to negative charges.
- Variables are correctly identified and substituted correctly into the correct part of the correct equation.
- Algebra is correct and rounding to appropriate number of significant figures is reasonable.

Language Objectives:

• Explain how the electric force on a charged particle changes as you get closer to or farther away from another charged object.

Tier 2 Vocabulary: charge, field

Labs, Activities & Demonstrations:

• students holding copper pipe in one hand and zinc-coated steel pipe in other—measure with voltmeter. (Can chain students together.)

Notes:

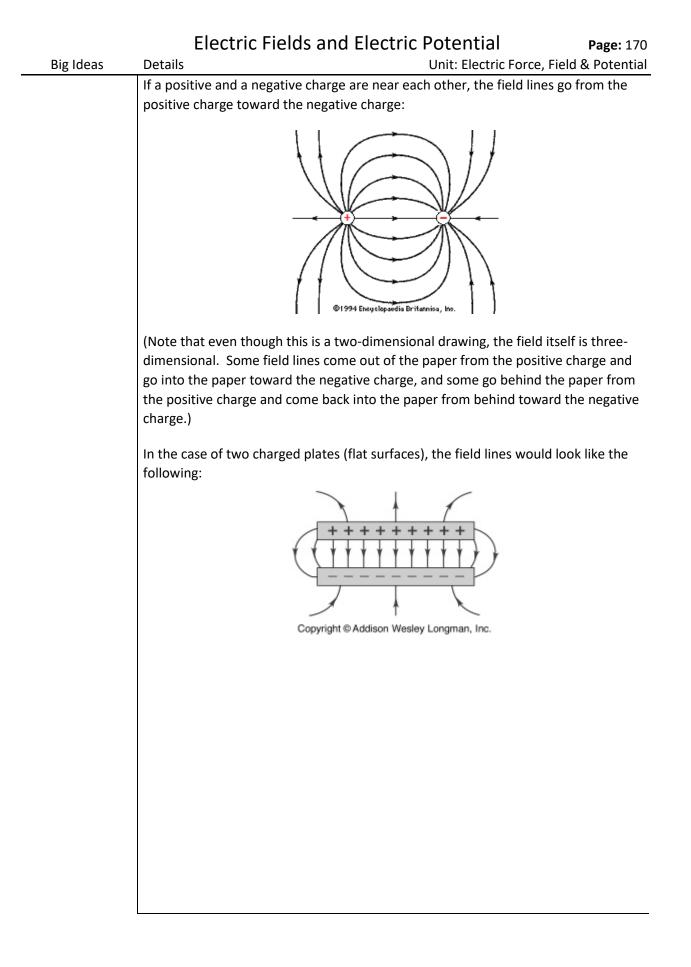
<u>force field</u>: a region in which an object experiences a force because of some intrinsic property of the object that enables the force to act on it. Force fields are vectors, which means they have both a magnitude and a direction.

<u>electric field</u> (\vec{E}) : an electrically charged region (force field) that exerts a force on any charged particle within the region.

An electric field applies a force to an object based on its electrical charge. $\vec{F}_{e} = q\vec{E}$, where \vec{E} represents the magnitude and direction of the electric field.

	Electric Fields and Electric Potential Page: 168
Big Ideas	Details Unit: Electric Force, Field & Potential
	Because gravity is a familiar concept, it is useful to use gravitational fields as a way to explain force fields, and thus electric fields.
	Recall that a gravitational field applies a force to an object based on its mass.
	$\vec{F}_g = m\vec{g}$, where \vec{g} represents the magnitude and direction of the gravitational field.
	Just as a gravitational field applies a force to an object that has mass, an electric field applies a force to an object that has charge:
	Gravitational Field
	force force
	A key difference between the two situations is that there are two kinds of charges—positive and negative—whereas there is only one kind of mass.
	The force on an object with mass is always in the direction of the gravitational field. However, the direction of the force on an object with charge depends on whether the charge is positive or negative. <i>The force on an object with positive charge is in the same direction as the electric field; the force on an object with negative charge is always in the opposite direction from the electric field.</i>
	For any force field, the amount of force is the amount of the quantity that the
	field acts on times the strength of the field:
	$\vec{F}_g = m \vec{g}$
	amount
	force of quantity strength that the of field field acts on
	$ec{m{ extbf{F}}}_{e} = egin{array}{ccc} egin{array} egin{array}{ccc} egin{ar$

Big Ideas	Electric Fields and Electric PotentialPage: 169DetailsUnit: Electric Force, Field & Potential
	field lines: lines with arrows that show the direction of an electric field. In the above diagrams, the arrows are the field lines.
	Field lines are lines that show the directions of force on an object. As described above, for an electric field, the object is assumed to be a positively charged particle. This means that <i>the direction of the electric field is from positive to negative</i> . This means that field lines go outward in all directions from a positively charged particle, and inward from all directions toward a negatively-charged particle.
	This means that a positively-charged particle (such as a proton) would move in the direction of the arrows, and a negatively charged particle (such as an electron) would move in the opposite direction.
	The simplest electric field is the region around a single charged particle:
	field lines field lines <t< th=""></t<>
	As stated in the <i>Electric Charge</i> topic (starting on page 153), the charges in a solid conductor repel one another, resulting in the charges moving to the outside of the conductor. This means that <i>the electric field inside of a conductor is zero</i> .
	However, the same is not true for insulators. If you have an insulator (such as a dielectric) in an electric field, the excess electric charge is spread throughout the insulator, and the electric field can have a nonzero value.
	If you have a hollow conducting sphere (such as a hollow metal ball), the sphere will conduct the charges to the outside, and the electric field inside of the sphere will be zero. In this situation, the sphere may be considered as a point charge, as if all of the charge were placed at its center.



Electric Field Strength

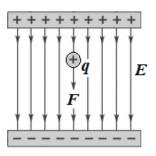
We can measure the strength of an electric field by placing a particle with a positive charge (q) in the field and measuring the force (\vec{F}) on the particle.

Details

Big Ideas

Coulomb's Law tells us that the force on the charge is due to the charges from the electric field:

$$F_e = \frac{kq_1q_2}{r^2}$$



If the plates have equal charge densities, the repulsive force from the like-charged plate decreases as the particle moves away from it, but the attractive force from the oppositely charged plate increases by the same amount as the particle moves toward it.

This means that if the positive and negative charges on the two surfaces that make the electric field have equal charge densities, *the force is the same everywhere in between the two surfaces*. The force on the particle is related only to the strength of the electric field and the charge of the particle.

This results in the equation that defines the electric field (\vec{E}) as the force between the electric field and our particle, divided by the charge of our particle:

$$\vec{E} = \frac{\vec{F}}{q}$$
 or $\vec{F} = q\vec{E}$

Big Ideas	Electric Fields and Electric Potential Page: 17 Details Unit: Electric Force, Field & Potential
0	Electric Potential Energy and Electric Potential
	Recall from the work-energy theorem that work equals a change in energy. Becaus an electric field can do work on a charged particle, an electric field must therefore apply energy to the particle.
	electric potential energy (U_e) : the amount of energy required to either bring two opposite charges together, or drive two like charges apart to a distance of infinity (<i>i.e.</i> , a distance at which they would no longer exert a force on each other).
	Note that potential energy of any kind (including electric potential energy) is a property of a system. Objects within a system can only have potential energy with respect to each other.
	Recall from physics 1 that energy added or released is work (by definition). Thi means that the potential energy of an object with respect to another object in system is the force required to bring the objects together times the distance over which that force would need to act:
	$U_e = \vec{F}_e \cdot \vec{d}$
	Because the distance can be in any direction, it makes sense to think of the distance as a radius <i>r</i> , using spherical coordinates. This means, according to Coulomb's Law:
	$U_e = F_e \cdot r = \frac{kq_1q_2}{r^2} \cdot r = \frac{kq_1q_2}{r}$
	<u>electric potential</u> (<i>V</i>): the electric potential of a location in space is the amount of work that would be required to bring a unit positive charge (<i>i.e.</i> , an object with charge of +1 C) from "infinity" (which really means from some location that has an electric potential of zero) to that location. <i>I.e.</i> , if $q = 1$ C, then $V = U_e$.
	For a charge of any other amount, q , its electric potential would be U_e divided b q:
	$V = \frac{U_e}{q} = \frac{kq}{r}$
	Therefore, the electric potential at a point due to multiple charges would be:
	$V = k \sum_{i} \frac{q_{i}}{r_{i}}$ or, because $k = \frac{1}{4\pi\varepsilon_{o}}$, $V = \frac{1}{4\pi\varepsilon_{o}} \cdot \sum_{i} \frac{q_{i}}{r_{i}}$
	Electric potential is measured in volts (V).
	$1 V \equiv 1 \frac{J}{C} \equiv 1 \frac{N \cdot m}{C}$

Electric Fields and Electric Potential Page: 173 **Big Ideas** Details Unit: Electric Force, Field & Potential Electric potential energy is analogous to gravitational potential energy. In a gravitational field, a particle has gravitational potential energy because gravity can make it move. In an electric field, a particle has electric potential (energy) because the electric field can make it move. For example, if we had a 1 kg mass and we placed it at a height of 4 m above the ground, its gravitational potential would be $U_q = mgh = (1)(10)(4) = 40$ J. Similarly, if we put an object with a charge of 1 C at a location that has an electric potential of 40 V, that object would have 40 J of potential energy due to the electric field. Gravitational **Electric Potential** Potential energy (Electric Potential Energy per kg of mass per coulomb of charge) charge mass • $40 \frac{J}{kg}$ • $40 \frac{J}{C} = 40 V$ $-20 \frac{J}{kg}$ $-20 \frac{J}{C} = 20 V$ $- 0 \frac{J}{kg} - 0 \frac{J}{C} = 0 V$ $V = \frac{U_e}{q} = \frac{W}{q} = \vec{E} \bullet \vec{d}$ gravitational potential energy electric potential per unit of mass (already per unit of charge)

Big Ideas Details

Work Done on a Charge by an Electric Field

Recall from physics 1 that work is the dot product of force and displacement:

$$W = \vec{F} \cdot \vec{d} = Fd \cos \theta$$

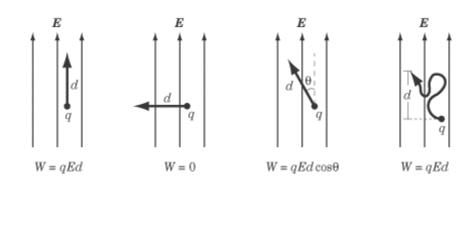
Because $W = \Delta U$, the potential energy of a charge in an electric field is the work that the field is able to do on the charge. This means:

$$U_e = \vec{F}_e \cdot \vec{d} = \frac{kq_1q_2}{r^2} \cdot r = \frac{kq_1q_2}{r}$$

Because $\vec{F} = q\vec{E}$, we can substitute:

$$W = \vec{F} \cdot \vec{d} = q \vec{E} \cdot \vec{d} = qEd \cos\theta$$

Note that the electric field can only cause displacement in the direction of the field. Therefore, the work caused by the electric field depends only on the displacement in the direction of the field. (This is where the $\cos\theta$ term comes from.)



	Electric Fields and Electric Potential Page: 175
Big Ideas	Details Unit: Electric Force, Field & Potential
	A more familiar term in electricity is voltage.
	<u>voltage = potential difference</u> (ΔV): the difference in electric potential between two points in space. This difference is caused by the action of an electric field at a distance:
	$\Delta V = \frac{\Delta U_e}{q} = \frac{W}{q} = \vec{E} \bullet \vec{d} = Ed \cos \theta$
	Note that many physics texts use the variable V for both electric potential and voltage (potential difference), and the reader needs to figure out which one is meant from context. To eliminate (or at least reduce) the confusion that this causes, these notes will use V for electric potential and ΔV for potential difference (voltage).
	Because voltage is simply a difference between two electric potentials, potential difference (voltage) is measured in volts (V).
	Because the work done by an electric field is $W = qEd\cos\theta$ and potential difference is $\Delta V = Ed\cos\theta$, we can substitute ΔV for $Ed\cos\theta$, which gives:
	$W = q \Delta V$

•	Redistribution of Charges
Big Ideas	Details

When conductors are placed in electrical contact, electrons will redistribute themselves so that the surfaces of the conductors have the same electric potential. This makes sense—because electrons repel each other, if they are able to move (*i.e.,* in a conductor), they will spread out to minimize the repulsion.

This is why birds can sit on power lines, even if those power lines are made of bare copper wire. Because the wire conducts the charges freely, the electrons spread out to equalize the distance, which means the potential difference between any one point on the wire and another is the same. This means there is no potential difference between the part of the wire where one of a bird's legs contacts it and part of the wire where the other touches. Because the wire conducts electricity much better than the bird does, virtually no electric charge goes through the bird.



Image © 2011 by Paul Anderson. Used with permission.

ntial Page: 177 Electric Force, Field & Potential

Big Ideas	Details	Unit: Electric Force, Field & Potential
	Sample Problem:	
	Q: A proton has a velocity of $1 \times 10^5 \frac{\text{m}}{\text{s}}$ when it	tisat † † † † † † † ^E
	point <i>P</i> in a uniform electric field that has a	an an an an an an an an an an an an an a
	intensity of $1 \times 10^4 \frac{N}{C}$. Calculate the force	Paky
	(magnitude and direction) on the proton and sketch its path.	an P a ∳ ∽
	A: The force on the proton is given by:	
	$\vec{F}_e = q\vec{E} = (1.6 \times 10^{-19})(1 \times 10^4) = 1.6 \times 10^{-15}$	N ↑ ↑ ↑ ↑ ↑ ↓ [■]
	The direction of the force is the same direction the electric field, which in this problem is u	
	An upward force causes acceleration upwa Because the proton starts with a velocity o right, upward acceleration means that its v will have a continuously increasing vertical component.	ards. Define the selection of the select

		Electric Fields and Electric Potential Page: 178
Big Ideas	Details	Unit: Electric Force, Field & Potential
		Homework Problems
	1.	(M) Sketch the electric field in all directions around each of the following charged particles. (Assume that each particle has the same amount of charge.)
		a. 🕒
		b. (+) (-)
		с. \bigcirc \bigcirc
	2.	(M) An electron is placed exactly halfway between two charged parallel plates, as shown in the diagram at the right. The electric field strength between the plates is $4.8 \times 10^{-11} \frac{N}{C}$. a. Sketch field lines to represent the electric field between the plates. b. Which direction does the electron move? c. As the electron moves, does the force acting on it increase, decrease, or remain the same?
		d. What is the net force on the electron?
		Answer: -7.68×10 ⁻³⁰ N
		(Negative means the opposite direction of the electric field.)

Electric Field Vectors

Unit: Electric Force, Field & Potential

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): 10.5.B, 10.5.B. 1, 10.5.B.2, 10.5.B.2.i, 10.5.B.2.ii, 10.5.B.2.iii, 10.5.B.2.iv

Mastery Objective(s): (Students will be able to...)

• Sketch & interpret electric field vector diagrams.

Success Criteria:

Details

Big Ideas

- Sketches show arrows pointing from positive charges toward negative charges.
- Electric field vectors show longer arrows where charges are larger and shorter arrows where charges are smaller.

Language Objectives:

• Explain how the electric force on a charged particle changes as you get closer to or farther away from another charged object.

Tier 2 Vocabulary: charge, field

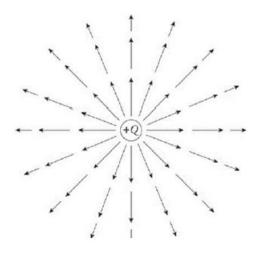
Notes:

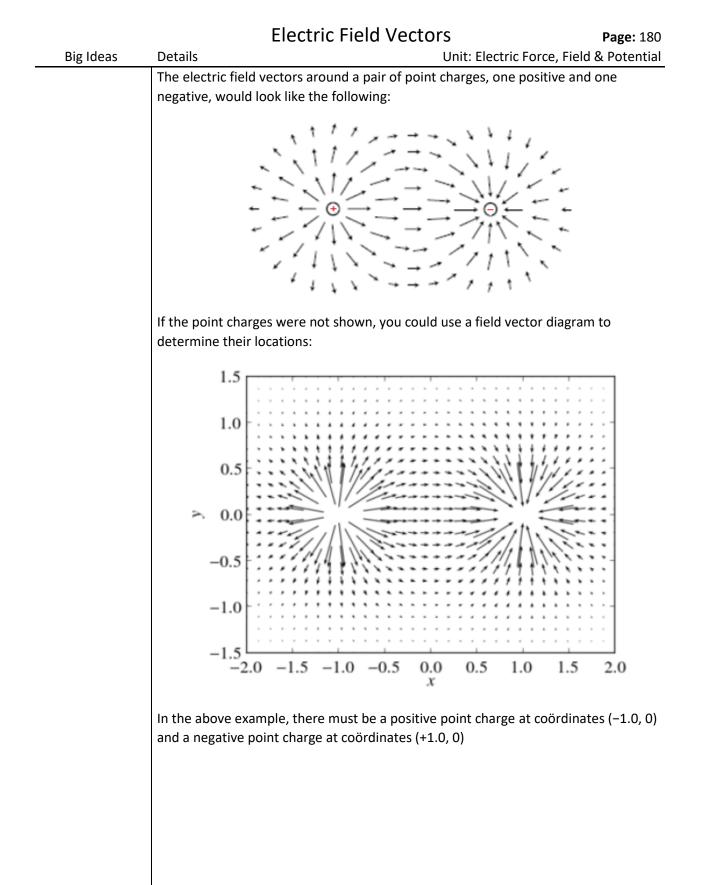
<u>electric field vector</u>: an arrow representing the strength and direction of an electric field at a point represented on a map.

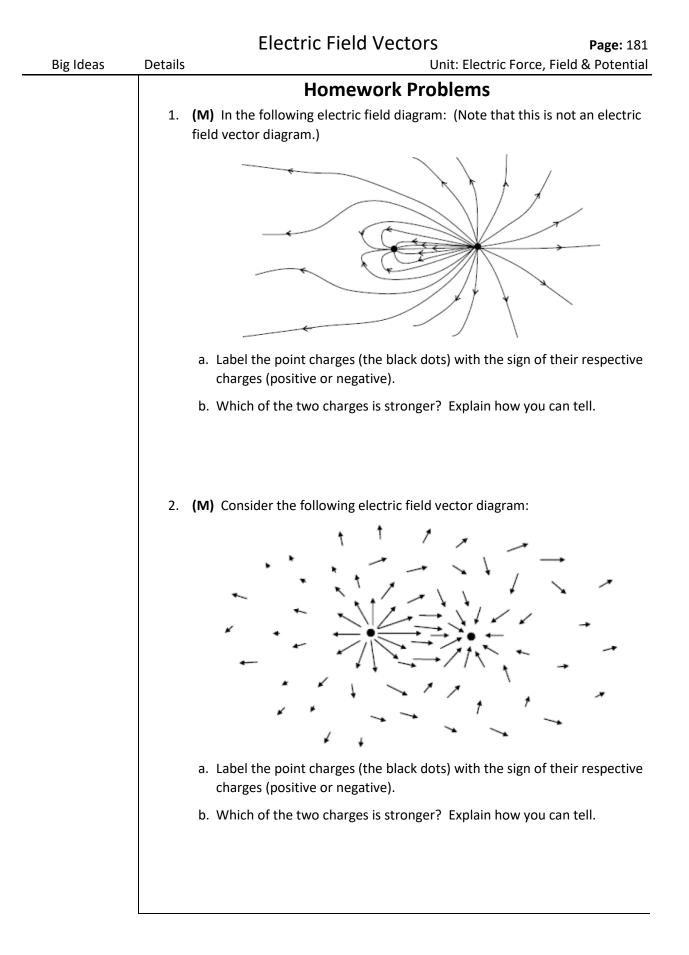
A map of an electric field can be drawn using field vectors instead of field lines.

Electric field vectors are preferred, because in addition to showing the direction of the electric field at a given location, they also show the relative strength. For example, this diagram shows the electric field around a positive charge. Notice that:

- The vectors point in the direction of the electric field (from positive to negative).
- The vectors are longer where the electric field is stronger and shorter where the electric field is weaker.







Unit: Electric Force, Field & Potential

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 10.5.B, 10.5.B. 1,

10.5.B.2, 10.5.B.2.i, 10.5.B.2.ii, 10.5.B.2.iii, 10.5.B.2.iv

Mastery Objective(s): (Students will be able to ...)

• Sketch & interpret equipotential ("isoline") maps.

Success Criteria:

- Isolines are perpendicular to electric field lines.
- Isolines connect regions of equal electric potential.

Language Objectives:

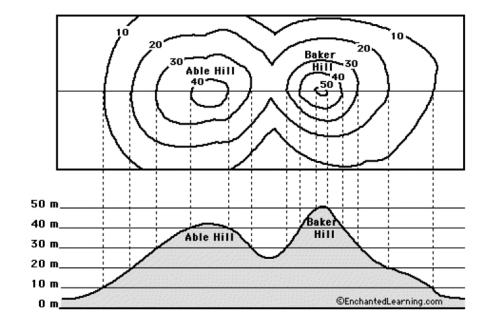
• Explain how isolines are like geographical contour maps.

Tier 2 Vocabulary: isoline, field, map

Notes:

isoline or equipotential line: a line on a map that connects regions of equal electric potential.

Isolines are the equivalent of elevation lines on a contour map. Below is an example of a contour map (top), and a side view of the same landscape (bottom):

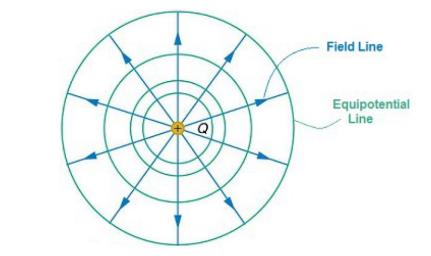


The contour map (top) is a view from above. Notice that each contour line connects points that have the same elevation.

Equipotential Lines & Maps

Similar to contour lines, equipotential lines connect regions of the same electric potential.

For example, the electric field direction is away from a positive point charge. The electric field strength decreases as you get farther away from the point charge. The equipotential lines (isolines) are therefore circles around the point charge; circles closer to the charge have higher electric potential, and circles farther away have lower electric potential.



Notice that the equipotential lines must be perpendicular to the field lines. (This makes sense: the field lines show the direction in which electric potential is decreasing, and equipotential lines are lines along with the electric potential is the same.)

As you travel along a field line, the electric potential becomes continuously less positive or more negative. The equipotential lines are the mileposts that show what the electric potential is at that point.

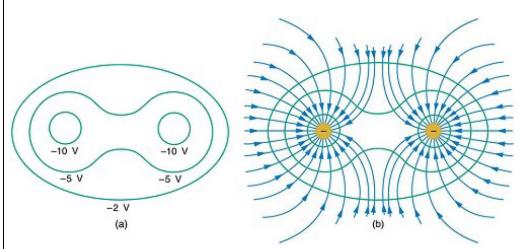
Big Ideas

Details

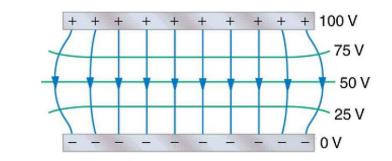
Equipotential Lines & Maps

If you were given only the equipotential lines, you could determine what the resulting field lines looked like. For example, in the illustration below, if you were given the isolines in diagram (a), you would infer that the regions inside each of the smaller isolines must be negative point charges, and that the electric field becomes more and more negative as you approach those points.

Because the electric field lines go from positive to negative, the field lines must therefore point into the points, resulting in diagram (b). Notice again that the field lines are always perpendicular to the isolines.



The electric field lines and isolines for the region between two parallel plates would look like the following:

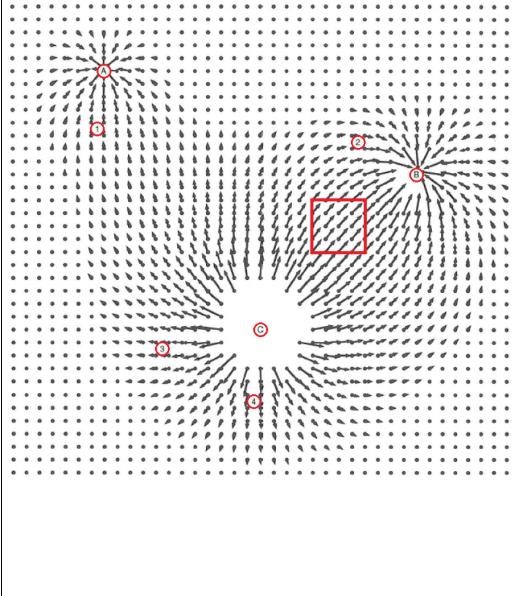


This is the procedure for mapping an electric field. Because electric potential can be measured using a voltmeter, you can use the voltmeter to determine where the isolines are and then draw the field lines so they are perpendicular to the isolines.

Big Ideas

Details

	Equ	ipotential Lines & Maps	Page: 185
Big Ideas	Details	Unit: Electric For	ce, Field & Potential
		Homework Problems	
	vector arrow repres location. Empty spa the electric field is e In the diagram belo	ow, there are three point charges, labeled A, B ations, 1, 2, 3, and 4, and a region of interest s	tric field in that ents regions where 3, and C. There are



Equipotential Lines & Maps

Big Ideas	Details Unit: Electric Force, Field & Potential
	 (M) On the diagram on the previous page, indicate the sign (positive or negative) of charges A, B, and C.
	2. (M) Rank the charges from strongest to weakest (regardless of sign).
	 (M) Indicate the direction of the force that would act on a proton placed at point 1 and point 2.
	 (M) Indicate the direction of the force that would act on an electron placed at point 3 and point 4.
	5. (M) At which numbered point is the electric field strongest in magnitude?
	6. (M) Circle the diagram that could represent isolines in the boxed region between charges B and C.
	$\begin{array}{c} \begin{array}{c} -30 \ V \\ -30 \ V \\ -20 \ V \\ -20 \ V \\ -10 \ V \\ 0 \ V \end{array} + \begin{array}{c} 0 \ V \\ +10 \ V \\ +20 \ V \\ +30 \ V \\ +10 \ V \\ 0 \ V \end{array} + \begin{array}{c} 0 \ V \\ -10 \ V \\ -20 \ V \\ -30 \ V \\ -30 \ V \\ -30 \ V \end{array} + \begin{array}{c} 0 \ V \\ -10 \ V \\ -20 \ V \\ -30 \ V \\ -30 \ V \\ -30 \ V \end{array} + \begin{array}{c} 0 \ V \\ +20 \ V \\ +20 \ V \\ +20 \ V \\ +30 \ V \\ -20 \ V \\ -20 \ V \\ -30 \ V \end{array} + \begin{array}{c} 0 \ V \\ -20 \ V \\ -30 \ V \\ -30 \ V \\ -30 \ V \end{array} + \begin{array}{c} 0 \ V \\ +20 \ V \\ +30 \ V \\ +30 \ V \\ -10 \ V $

Big Ideas	Details	Unit: DC Circuits
	Introduction: DC Circuits	
	Unit: DC Circuits	
	Topics covered in this chapter:	
	Electric Current & Ohm's Law	
	Electrical Components	205
	Voltaic Cells (Batteries)	208
	EMF & Internal Resistance of a Battery	211
	Circuits	214
	Kirchhoff's Rules	219
	Series Circuits (Resistance Only)	224
	Parallel Circuits (Resistance Only)	230
	Mixed Series & Parallel Circuits (Resistance Only)	240
	Measuring Voltage, Current & Resistance	248
	Capacitance	252
	Capacitors in Series and Parallel Circuits	258
	DC Resistor-Capacitor (RC) Circuits	
	This chapter discusses DC Circuits, particularly those containing batt and/or capacitors., how they behave, and how they relate to each o	
	• <i>Electric Current & Ohm's Law</i> describes equations and calcul the flow of charged particles (electric current).	ations involving
	 Electrical Components shows pictures of and circuit diagram common electrical components. 	symbols for
	• EMF & Internal Resistance of a Battery explains the difference voltage supplied by the chemical cells in a battery and the vo battery is actually able to supply in a circuit.	
	 Circuits, Series Circuits, Parallel Circuits, and Mixed Series & describe arrangements of circuits that contain batteries and other components that have resistance) and the equations t them. 	resistors (or
	• <i>Measuring Voltage, Current & Resistance</i> describes how to measure those quantities for components in a circuit.	correctly
	• Capacitance and Capacitors in Series & Parallel Circuits descurated and how they behave in circuits.	ribes capacitors

Big Ideas	Details Unit: DC Circuits
	• DC Resistor-Capacitor (RC) Circuits describes calculations for time-varying circuits that contain a resistor and a capacitor.
	One of the new challenges encountered in this chapter is interpreting and simplifying circuit diagrams, in which different equations may apply to different parts of the circuit.
	Standards addressed in this chapter:
	NGSS Standards/MA Curriculum Frameworks (2016):
	HS-PS2-4. Use mathematical representations of Newton's Law of Gravitation and Coulomb's Law to describe and predict the gravitational and electrostatic forces between objects.
	HS-PS3-1. Use algebraic expressions and the principle of energy conservation to calculate the change in energy of one component of a system when the change in energy of the other component(s) of the system, as well as the total energy of the system including any energy entering or leaving the system, is known. Identify any transformations from one form of energy to another, including thermal, kinetic, gravitational, magnetic, or electrical energy, in the system.
	HS-PS3-2. Develop and use a model to illustrate that energy at the macroscopic scale can be accounted for as either motions of particles and objects or energy stored in fields.
	HS-PS3-5. Develop and use a model of magnetic or electric fields to illustrate the forces and changes in energy between two magnetically or electrically charged objects changing relative position in a magnetic or electric field, respectively.
AP [®] only	AP [®] Physics 2 Learning Objectives/Essential Knowledge (2024):
	10.6.A : Describe the physical properties of a parallel-plate capacitor.
	10.6.A.1: A parallel-plate capacitor consists of two separated parallel conducting surfaces that can hold equal amounts of charge with opposite signs.
	10.6.A.2: Capacitance relates the magnitude of the charge stored on each plate to the electric potential difference created by the separation of those charges.
	10.6.A.2.i: The capacitance of a capacitor depends only on the physical properties of the capacitor, such as the capacitor's shape and the material used to separate the plates.

Big Ideas	Details Unit: DC Circuits
AP® only	10.6.A.2.ii : The capacitance of a parallel-plate capacitor is proportional to the area of one of its plates and inversely proportional to the distance between its plates. The constant of proportionality is the product of the dielectric constant, κ (ε_r), of the material between the plates and the electric permittivity of free space, ε_0 .
	10.6.A.3 : The electric field between two charged parallel plates with uniformly distributed electric charge, such as in a parallel-plate capacitor, is constant in both magnitude and direction, except near the edges of the plates.
	10.6.A.3.i : The magnitude of the electric field between two charged parallel plates, where the plate separation is much smaller than the dimensions
	of the plates, can be described with the equation $E_c = \frac{Q}{\kappa \varepsilon_o A}$.
	10.6.A.3.ii: A charged particle between two oppositely charged parallel plates undergoes constant acceleration and therefore its motion shares characteristics with the projectile motion of an object with mass in the gravitational field near Earth's surface.
	10.6.A.4 : The electric potential energy stored in a capacitor is equal to the work done by an external force to separate that amount of charge on the capacitor.
	10.6.A.5 : The electric potential energy stored in a capacitor is described by the equation $U_c = \frac{1}{2}Q\Delta V$
	10.6.A.6 : Adding a dielectric between two plates of a capacitor changes the capacitance of the capacitor and induces an electric field in the dielectric in the opposite direction to the field between the plates.
	11.1.A : Describe the movement of electric charges through a medium.
	11.1.A.1 : Current is the rate at which charge passes through a cross-sectional area of a wire.
	11.1.A.1.i: Electric charge moves in a circuit in response to an electric potential difference, sometimes referred to as electromotive force, or emf (ε).
	11.1.A.1.ii: If the current is zero in a section of wire, the net motion of charge carriers in the wire is also zero, although individual charge carriers will not have zero speed.
	11.1.A.2: Although current is not a vector quantity, it does have a direction. The direction of current is associated with what the motion of positive charge would be but not with any coordinate system in space.
	11.1.A.2.i : The direction of conventional current is chosen to be the direction in which positive charge would move.

Big Ideas	Details Unit: DC Circuits
AP [®] only	11.1.A.2.ii : In common circuits, current is actually due to the movement of electrons (negative charge carriers).
	11.2.A : Describe the behavior of a circuit.
	11.2.A.1: A circuit is composed of electrical loops, which may include circuit elements such as wires, batteries, resistors, lightbulbs, capacitors, switches, ammeters, and voltmeters.
	11.2.A.2 : A closed electrical loop is a closed path through which charges may flow.
	11.2.A.2.i : A closed circuit is one in which charges would be able to flow.
	11.2.A.2.ii : An open circuit is one in which charges would not be able to flow.
	11.2.A.2.iii : A short circuit is one in which charges would be able to flow with no change in potential difference.
	11.2.A.3 : A single circuit element may be part of multiple electrical loops.
	11.2.A.4 : Circuit schematics are representations used to describe and analyze electric circuits.
	11.2.A.4.i: The properties of an electric circuit are dependent on the physical arrangement of its constituent elements.
	11.2.A.4.ii: Circuit elements have common symbols that are used to create schematic diagrams. Variable elements are indicated by a diagonal strikethrough arrow across the standard symbol for that element.
	11.3.A : Describe the resistance of an object using physical properties of that object.
	11.3.A.1 : Resistance is a measure of the degree to which an object opposes the movement of electric charge.
	11.3.A.2: The resistance of a resistor with uniform geometry is proportional to its resistivity and length and is inversely proportional to its cross- sectional area.
	11.3.A.2.i: Resistivity is a fundamental property of a material that depends on its atomic and molecular structure and quantifies how strongly the material opposes the motion of electric charge.
	11.3.A.2.ii : The resistivity of a conductor typically increases with temperature.
	11.3.B : Describe the electrical characteristics of elements of a circuit.
	11.3.B.1 : Ohm's law relates current, resistance, and potential difference across a conductive element of a circuit.
	11.3.B.1.i : Materials that obey Ohm's law have constant resistance for all currents and are called ohmic materials.
l	

Big Ideas	Details Unit: DC Circuits
AP [®] only	11.3.B.1.ii : The resistivity of an ohmic material is constant regardless of temperature.
	11.3.B.1.iii: Resistors can also convert electrical energy to thermal energy, which may change the temperature of both the resistor and the resistor's environment.
	11.3.B.1.iv : The resistance of an ohmic circuit element can be determined from the slope of a graph of the current in the element as a function of the potential difference across the element.
	11.4.A : Describe the transfer of energy into, out of, or within an electric circuit, in terms of power.
	11.4.A.1: The rate at which energy is transferred, converted, or dissipated by a circuit element depends on the current in the element and the electric potential difference across it.
	11.4.A.2 : The brightness of a bulb increases with power, so power can be used to qualitatively predict the brightness of bulbs in a circuit.
	11.5.A : Describe the equivalent resistance of multiple resistors connected in a circuit.
	11.5.A.1 : Circuit elements may be connected in series and/or in parallel.
	11.5.A.1.i: A series connection is one in which any charge passing through one circuit element must proceed through all elements in that connection and has no other path available. The current in each element in series must be the same.
	11.5.A.1.ii : A parallel connection is one in which charges may flow through one of two or more paths. Across each path, the potential difference is the same.
	11.5.A.2 : A collection of resistors in a circuit may be analyzed as though it were a single resistor with an equivalent resistance R_{eq} .
	11.5.A.2.i : The equivalent resistance of a set of resistors in series is the sum of the individual resistances.
	11.5.A.2.ii: The inverse of the equivalent resistance of a set of resistors connected in parallel is equal to the sum of the inverses of the individual resistances.
	11.5.A.2.iii: When resistors are connected in parallel, the number of paths available to charges increases, and the equivalent resistance of the group of resistors decreases.
l	

Big Ideas	Details Unit: DC Circu
AP® only	11.5.B : Describe a circuit with resistive wires and a battery with internal resistance.
	11.5.B.1 : Ideal batteries have negligible internal resistance. Ideal wires have negligible resistance.
	11.5.B.1.i : The resistance of wires that are good conductors may normally be neglected, because their resistance is much smaller than that of other elements of a circuit.
	11.5.B.1.ii : The resistance of wires may only be neglected if the circuit contains other elements that do have resistance.
	11.5.B.1.iii: The potential difference a battery would supply if it were idea is the potential difference measured across the terminals when there i no current in the battery and is sometimes referred to as its emf (ε).
	11.5.B.2 : The internal resistance of a nonideal battery may be treated as the resistance of a resistor in series with an ideal battery and the remainder the circuit.
	11.5.B.3 : When there is current in a nonideal battery with internal resistanc r, the potential difference across the terminals of the battery is reduced relative to the potential difference when there is no current in the batter
	11.5.C : Describe the measurement of current and potential difference in a circuit.
	11.5.C.1 : Ammeters are used to measure current at a specific point in a circuit.
	11.5.C.1.i : Ammeters must be connected in series with the element in which current is being measured.
	11.5.C.1.ii: Ideal ammeters have zero resistance so that they do not affect the current in the element that they are in series with.
	11.5.C.2 : Voltmeters are used to measure electric potential difference between two points in a circuit.
	11.5.C.2.i : Voltmeters must be connected in parallel with the element across which potential difference is being measured.
	11.5.C.2.ii : Ideal voltmeters have an infinite resistance so that no charge flows through them.
	11.5.C.3 : Nonideal ammeters and voltmeters will change the properties of t circuit being measured.
	11.6.A : Describe a circuit or elements of a circuit by applying Kirchhoff's loop rule.
	11.6.A.1 : Energy changes in simple electrical circuits may be represented in terms of charges moving through electric potential differences within circuit elements.

		S
Big Ideas	Details Unit: DC Circuits	S
AP [®] only	11.6.A.2 : Kirchhoff's loop rule is a consequence of the conservation of energy	1.
,	11.6.A.3 : Kirchhoff's loop rule states that the sum of potential differences across all circuit elements in a single closed loop must equal zero.	
	11.6.A.4 : The values of electric potential at points in a circuit can be	
	represented by a graph of electric potential as a function of position within a loop.	
	11.7.A : Describe a circuit or elements of a circuit by applying Kirchhoff's junction rule.	
	11.7.A.1 : Kirchhoff's junction rule is a consequence of the conservation of electric charge.	
	11.7.A.2: Kirchhoff's junction rule states that the total amount of charge entering a junction per unit time must equal the total amount of charge exiting that junction per unit time.	
	11.8.A : Describe the equivalent capacitance of multiple capacitors.	
	11.8.A.1 : A collection of capacitors in a circuit may be analyzed as though it were a single capacitor with an equivalent capacitance <i>C</i> _{eq} .	
	11.8.A.1.i : The inverse of the equivalent capacitance of a set of capacitors connected in series is equal to the sum of the inverses of the individual capacitances.	
	11.8.A.1.ii: The equivalent capacitance of a set of capacitors in series is less than the capacitance of the smallest capacitor.	
	11.8.A.1.iii: The equivalent capacitance of a set of capacitors in parallel is the sum of the individual capacitances.	
	11.8.A.2: As a result of conservation of charge, each of the capacitors in series must have the same magnitude of charge on each plate.	S
	11.8.B : Describe the behavior of a circuit containing combinations of resistors and capacitors.	
	11.8.B.1 : The time constant is a significant feature of an RC circuit.	
	11.8.B.1.i : The time constant of an RC circuit is a measure of how quickly the capacitor will charge or discharge and is defined as $\tau = R_{eq}C_{eq}$.	
	11.8.B.1.ii : For a charging capacitor, the time constant represents the time required for the capacitor's charge to increase from zero to approximately 63 percent of its final asymptotic value.	
	11.8.B.1.iii : For a discharging capacitor, the time constant represents the time required for the capacitor's charge to decrease from fully charged to approximately 37 percent of its initial value.	

Big Ideas	Details Unit: DC Circuits
A₽® only	11.8.B.2: The potential difference across a capacitor and the current in the branch of the circuit containing the capacitor each change over time as the capacitor charges and discharges, but both will reach a steady state after a long time interval.
	11.8.B.2.i: Immediately after being placed in a circuit, an uncharged capacitor acts like a wire, and charge can easily flow to or from the plates of the capacitor.
	11.8.B.2.ii: As a capacitor charges, changes to the potential difference across the capacitor affect the charge on the plates of the capacitor, the current circuit branch in which the capacitor is located, and the electric potential energy stored in the capacitor.
	11.8.B.2.iii: The potential difference across a capacitor, the current in the circuit branch in which the capacitor is located, and the electric potential energy stored in the capacitor all change with respect to time and asymptotically approach steady state conditions.
	11.8.B.2.iv: After a long time, a charging capacitor approaches a state of being fully charged, reaching a maximum potential difference at which there is zero current in the circuit branch in which the capacitor is located.
	11.8.8.2.v: Immediately after a charged capacitor begins discharging, the amount of charge on the capacitor plates and the energy stored in the capacitor begin to decrease.
	11.8.B.2.vi: As a capacitor discharges, the amount of charge on the capacitor, the potential difference across the capacitor, and the current in the circuit branch in which the capacitor is located all decrease until a steady state is reached.
	11.8.B.2.vii : After either charging or discharging for times much greater than the time constant, the capacitor and the relevant circuit branch may be modeled using steady-state conditions.
	Skills learned & applied in this chapter:
	 Working with material-specific constants from a table.
	 Identifying electric circuit components.
	 Simplifying circuit diagrams.

Page: 195 **Big Ideas** Details Electric Current & Ohm's Law Unit: DC Circuits NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-9(MA) AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 11.3.A, 11.3.A.1, 11.3.A.2, 11.3.A.2.i, 11.3.A.2.ii, 11.3.B, 11.3.B.1, 11.3.B.1.i, 11.3.B.1.ii, 11.3.B.1.iii, 11.3.B.1.iv, 11.4.A, 11.4.A.1 Mastery Objective(s): (Students will be able to...) • Solve problems involving relationships between voltage, current, resistance and power. **Success Criteria:** Variables are correctly identified and substituted correctly into the correct equation. Algebra is correct and rounding to appropriate number of significant figures is reasonable. Language Objectives: • Describe the relationships between voltage, current, resistance, and power. Tier 2 Vocabulary: current, resistance, power Labs, Activities & Demonstrations: modeling resistivity with straws make a light bulb out of a pencil "lead" (graphite) Notes: electric current (*I*): the flow of charged current particles through a conductor, caused by a difference in electric potential. The electrons direction of the electric current is defined as the direction that a positively-charged particle would move. Note, however, that the particles that are actually moving are electrons, which are negatively charged. This means that electric current "travels" in the opposite direction from the electrons. We will use conventional current (pretending that positive particles are flowing through the circuit) throughout this course. Electric current (\vec{I}) is a vector quantity and is measured in amperes $I = \frac{\Delta Q}{t}$ (A), often abbreviated as "amps". One ampere is one coulomb per

second.

	Electric Current & Onin's Law	Page: 196
Big Ideas	Details Unit:	DC Circuits
	Note that when electric current is flowing, charged particles move from	n where
	they are along the circuit. For example, when a light bulb is illuminate	d, the
	electrons that do the work for the first few minutes are already in the	
	voltage (potential difference) $(\Delta V)^*$: the difference in electric potential	W/
	energy between two locations, per unit of charge.	$\Delta V = \frac{W}{q}$
	chergy between two locations, per unit of charge.	Ч
	Potential difference is the work (<i>W</i>) done on a charge per unit of charge	ze (a).
	Potential difference (ΔV) is a scalar quantity (in DC circuits) and is mea	
		Surcum
	volts (V), which are equal to joules per coulomb.	
	The total voltage in a circuit is usually determined by the power supply	/ that is
		, that is
	used for the circuit (usually a battery in DC circuits).	
	resistance (<i>R</i>): the amount of electromotive force (electric potential)	A1/
	needed to force a given amount of current through an object in a DC	$R = \frac{\Delta V}{I}$
		1
	circuit.	
	Resistance (<i>R</i>) is a scalar quantity and is measured in ohms (Ω). One of	hm is ono
		TITLIS ONE
	volt per ampere.	
	This relationship is Ohm's Law, named for the German physicist Georg	Ohm
		Onn.
	Ohm's Law is more commonly written:	
	$I = \frac{\Delta V}{R}$ or $\Delta V = IR$	
	Simply put, Ohm's Law states that	Þ
	an object has an ability to resist	
	electric current flowing through it.	
	The more resistance an object	
	has, the more voltage you need to	
	force electric current through it.	_ ;
	Or, for a given voltage, the more	F.
	resistance an object has, the less voltage	-0
	current will flow through it.	\leq
		3
	Resistance is an intrinsic property	m _
	of a substance. In this course, we	
	will limit problems that involve calculations to ohmic resistors, which r	neans
	their resistance does not change with temperature.	
	* Note that most physics texts (and most physicists and electricians) use V for both electric	potential and
	voltage, and students have to rely on context to tell the difference. In these notes, to ma	
	distinction clear (and to be consistent with the AP® Physics 2 exam), we will use V for ele	
	potential, and ΔV for voltage (potential difference).	

Big Ideas	Details Unit: DC Circuits
	Choosing the voltage and the arrangement of objects in the circuit (which determines the resistance) is what determines how much current will flow.
	Electrical engineers use resistors in circuits to reduce the amount of current that flows through the components.
	Every physical object has resistance.
	• Substances that are good conductors have minimal resistance. The resistance of wires is small enough that it can be ignored, unless the wire is the only element of the circuit.
	 Substances that are good insulators have very large resistance. Air, for
	example, has a resistance of 10^{12} to $10^{16} rac{\Omega}{cm}$; it takes about 21 100 V to
	create a spark that can bridge a gap of 1 cm of air. This means that an air gap is considered to be an open circuit, in which no current flows.
honors (not AP®)	<u>impedance</u> (<i>Z</i>): the opposition that a circuit presents to a current when a voltage is applied. In a DC circuit, impedance and resistance are equivalent. In an AC circuit, the oscillating voltage creates changing electric and magnetic fields, which themselves resist the changes caused by the alternating current. This means the opposition to current is constantly changing at the same frequency as the oscillation of the current.
	Mathematically, impedance is represented as a complex number, in which the real part is resistance and the imaginary part is reactance, a quantity that takes into account the effects of the oscillating electric and magnetic fields.
	<u>resistivity (ρ)</u> : the innate ability of a substance to offer electrical resistance. The resistance of an object is therefore a function of the resistivity of the substance (ρ), and of the length (L) and cross- sectional area (A) of the object. In MKS units, resistivity is measured in ohm- meters (Ω ·m).
	Resistivity changes with temperature. For small temperature differences (less than 100°C), resistivity is given by:
	$\rho = \rho_o (1 + \alpha \Delta T)$

Big Ideas	Details Unit: DC Circuits					
	where $ ho_{_{o}}$ is the resistivity at some reference temperature and $lpha$ is the					
	temperature coëfficient of resistivity for that substance. For conductors, $lpha$ is					
	positive (which means their resistivity					
	increases with temperature). For metals 0.150 –					
	at room temperature, resistivity typically varies from +0.003 to +0.006 K^{-1} . 0.125 – Hg					
	0.100 -					
	Some materials become superconductors					
	temperatures. The temperature below 0.050 – which a material becomes a					
	superconductor is called the critical $0.025 - T_{c}$					
	temperature (T_c). For example, the critical 0					
	temperature for mercury is 4.2 K, as shown 4.0 4.1 4.2 4.3 4.4					
	in the graph to the right. T(K)					
hanara İ	<u>conductivity</u> (σ): the innate ability of a substance to conduct electricity. 1					
honors (not AP®)	Conductivity (σ) is the inverse of resistivity, and is measured in $\sigma = \frac{1}{\rho}$					
(//////////////////////////////////////	siemens (S). Siemens used to be called mhos (symbol U).					
Ī	(Note that "mho" is "ohm" spelled backwards.)					
	ohmic resistor: a resistor whose resistance is the same regardless of voltage and					
	current. The filament of an incandescent light bulb is an example of a non-					
	ohmic resistor, because the current heats up the filament, which increases its					
	resistance. (This is necessary in order for the filament to also produce light.)					
	<u>capacitance</u> (<i>C</i>): the ability of an object to hold an electric charge. $C = \frac{Q}{Q}$					
	Capacitance (C) is a scalar quantity and is measured in farads (F). One ΔV					
	farad equals one coulomb per volt.					
	power (P): as discussed in the mechanics section of this course, power (P) is the					
	work done per unit of time and is measured in watts (W).					
	In electric circuits:					
	$P = \frac{W}{t} = I\Delta V = I^2 R = \frac{(\Delta V)^2}{R}$					
	t R					
	work (W): recall from mechanics that work (W) equals power times time, and is					
	measured in either newton-meters (N·m) or joules (J):					
	$(\Delta V)^2 t$					
	$W = Pt = I\Delta Vt = I^2Rt = \frac{(\Delta V)^2 t}{R} = Vq$					
	Electrical work or energy is often measured in kilowatt-hours (kW·h).					
	$1 \text{kW} \cdot \text{h} = 3.6 \times 10^6 \text{ J} = 3.6 \text{ MJ}$					

Big Ideas

Details

Summary	v of Terms.	Units and Variables	
Samuary	, 01 101113,		

Term	Variable	Unit	Term	Variable	Unit
point charge	q	coulomb (C)	resistance	R	ohm (Ω)
charge	Q	coulomb (C)	capacitance	С	farad (F)
current	Ι	ampere (A)	power	Р	watt (W)
voltage	ΔV	volt (V)	work	W	joule (J)

honors (not AP®)

Alternating Current vs. Direct Current

Electric current can move in two ways.

<u>direct current</u>: electric current flows through the circuit, starting at the positive terminal of the battery or power supply, and ending at the negative terminal. Batteries supply direct current. A typical AAA, AA, C, or D battery supplies 1.5 volts DC.

However, the net flow of charged particles through a wire is very slow. Electrons continually collide with one another in all directions as they drift slowly through the circuit. Individual electrons in a DC circuit have a net velocity of about one meter per hour.



<u>alternating current</u>: electric current flows back and forth in one direction and then the other, like a wave. The current alternates at a particular frequency. In the U.S., household current is 110 – 120 volts AC with a frequency of 60 Hz. In most of the rest of the world, household current is 230 volts AC with a frequency of 50 Hz.

Alternating current requires higher voltages in order to operate devices, but has the advantage that the voltage drop is much less over a length of wire than with direct current.

Big Ideas	Details	Unit: DC Circuits
	Sample Problems:	
	Q: A simple electrical device uses 1.5 A of household electrical outlet. How much were plugged into a 12 V outlet in a ca	h current would the same device draw if it
	A: Resistance is a property of a specific of we assume the device is ohmic and the current.	bject. Because we are not told otherwise, e resistance is the same regardless of the
		formation about the device plugged into a vice's resistance, then use the resistance ws in the car.
	In the household outlet:	In the car:
	$R = \frac{\Delta V}{I} = \frac{110}{1.5} = 73.\overline{3}\Omega$	$I = \frac{\Delta V}{R} = \frac{12}{73.\overline{3}} = 0.163 \mathrm{A}$
	much current would the computer dra	r. The laptop's power supply adjusts the regardless of the voltage supplied. How w from a 110 V household outlet? How computer need to draw from a 12 V car
	A: The strategy for this problem is the sa	me as the previous one.
	Household outlet:	Car outlet:
	$P = I\Delta V$ $I = \frac{P}{\Delta V} = \frac{10}{110} = 0.091 \text{ A}$	$I = \frac{P}{\Delta V} = \frac{10}{12} = 0.8\overline{3} \text{ A}$

	Electric Current & Onm's Law	Page: 201
Big Ideas	Details	Unit: DC Circuits
	Q: A 100 Ω resistor is 0.70 mm in diameter and 6.0 mm long. If you make a 470 Ω resistor out of the same material (with the same would the length need to be? If, instead, you wanted to make a same length, what would the new diameter need to be?	diameter), what
	A: In both cases, $R = \frac{\rho L}{A}$.	
	For a resistor of the same diameter (same cross-sectional area), the same, which means:	ho and A are
	$\frac{R'}{R} = \frac{L'}{L}$ $L' = \frac{R'L}{R} = \frac{(470)(6.0)}{100} = 28.2 \mathrm{mm}$	
	For a resistor of the same length, $ ho$ and L are the same, which	means:
	$\frac{R'}{R} = \frac{A}{A'} = \frac{\pi r^2}{\pi (r')^2} = \frac{\pi (\frac{d}{2})^2}{\pi (\frac{d}{2})^2} = \frac{d^2}{(d')^2}$ $d' = \sqrt{\frac{Rd^2}{R'}} = d\sqrt{\frac{R}{R'}} = 0.70\sqrt{\frac{100}{470}} = 0.70\sqrt{0.213} = 0.32$	3mm
	V K V K V 470	

Big Ideas	Details	Unit: DC Circuits
		Homework Problems
	1.	(S) An MP3 player uses a standard 1.5 V battery. How much resistance is in the circuit if it uses a current of 0.010 A?
		Answer: 150 Ω
	2.	(M) How much current flows through a hair dryer plugged into a 110 V circuit if it has a resistance of 25 Ω ?
		Answer: 4.4 A
	3.	(S) A battery pushes 1.2 A of charge through the headlights in a car, which has a resistance of 10 Ω . What is the potential difference across the headlights?
		Answer: 12 V
	4.	(M) A circuit used for electroplating copper applies a current of 3.0 A for 16 hours. How much charge is transferred?
		Answer: 172 800 C
	F	
	5.	(S) What is the power when a voltage of 120 V drives a 2.0 A current through a device?
		Answer: 240W

Big Ideas	Details	Unit: DC Circuits
	6.	(S) What is the resistance of a 40. W light bulb connected to a 120 V circuit?
		Answer: 360 Ω
	7.	(M) If a component in an electric circuit dissipates 6.0 W of power when it draws a current of 3.0 A, what is the resistance of the component?
		Answer: 0.67 Ω
	8.	(S) A 0.7 mm diameter by 60 mm long pencil "lead" is made of graphite, which has a resistivity of approximately $1.0 \times 10^{-4} \Omega \cdot m$. What is its resistance? Hints:
		 You will need to convert mm to m. You will need to convert the diameter to a radius before using A = πr² to find the area.
		Answer: 15.6 Ω
	9.	(M) A cylindrical object has radius <i>r</i> and length <i>L</i> and is made from a substance with resistivity ρ . A potential difference of ΔV is applied to the object. Derive an expression for the current that flows through it. <i>Hint: this is a two-step problem.</i>
		Answer: $I = \frac{(\Delta V)A}{\rho L}$

Big Ideas	Details	Unit: DC Circuits
	10.	(S) Some children are afraid of the dark and ask their parents to leave the
		hall light on all night. Suppose the hall light in a child's house has two 75. W
		incandescent light bulbs (150 W total), the voltage is 120 V, and the light is
		left on for 8.0 hours.
		a. How much current flows through the light fixture?
		Answer: 1.25 A
		b.How many kilowatt-hours of energy would be used in one night?
		Answer: 1.2 kW·h
		c. If the power company charges 22 ø per kilowatt-hour, how much does it
		cost to leave the light on overnight?
		Answer: 26.4 ¢
		d.If the two incandescent bulbs are replaced by LED bulbs that use 12.2 W
		each (24.4 W total) how much would it cost to leave the light on
		overnight?
		Answer: 4.3 ¢

Electrical Components

Unit: DC Circuits

Details

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-9(MA)

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): 11.2.A, 11.2.A.4.ii

Mastery Objective(s): (Students will be able to...)

- Identify electrical components using the components themselves and/or the symbols used in circuit diagrams.
- Describe the purpose of various electrical components and how they are used in circuits.

Success Criteria:

- Descriptions correctly identify the component.
- Purpose and use of component is correct.

Language Objectives:

• Explain the components in an actual circuit or a circuit diagram and describe what each one does.

Tier 2 Vocabulary: component, resistor, fuse

Labs, Activities & Demonstrations:

- Show & tell with actual components.
- How a fuse works.

Notes:

<u>electrical component</u>: an object that performs a specific task in an electric circuit. A circuit is a collection of components connected together so that the tasks performed by the individual components combine in some useful way.

<u>circuit diagram</u>: a picture that represents a circuit, with different symbols representing the different components.

Electrical Components

Pigldoog		Electrical C	omponents	Page: 206		
<u> </u>	Details Unit: DC Circuits The following table describes some of the common components of electrical circuits					
	what they do, and the symbols that are used to represent them in circuit diagrams.					
	Component	Symbol	Picture	Description		
	wire			Carries current in a circuit.		
	junction	+	X	Connection between two or more wires.		
	unconnected wires			Wires pass by each other but are not connected.		
	battery	Ť		Supplies current at a fixed voltage.		
	resistor	-~~~-		Resists flow of current.		
	potentiometer (rheostat, dimmer)			Provides variable (adjustable) resistance.		
	capacitor	$\dashv \vdash$		Stores charge.		
	diode	* H -	-	Allows current to flow in only one direction (from + to –).		
	light-emitting diode (LED)		+	Diode that gives off light when current flows through it.		
	switch	~~		Opens / closes circuit.		
	incandescent lamp (light)			Provides light (and resistance).		

Electrical Components

	Component	Symbol	Picture	Description
	inductor (transformer)	<u> 1000</u>		Increases or decreases voltage in an AC circuit.
	voltmeter	-(V)-		Measures voltage (volts).
	ammeter	-(A)-		Measures current (amperes).
	ohmmeter	-R- -Ω-		Measures resistance (ohms).
	fuse			Opens circuit if too much current flows through it.
	ground		(clamps to water pipe)	Neutralizes charge.
AP® only	symbol. The diago resistance). The di the same manner.	nal arrow indic agonal arrow c	use of the diagonal arrow ates that the resistance ca an be used with other syr will use just a diagonal sl	an be adjusted (variable nbols (<i>e.g.,</i> capacitors) i

Voltaic Cells (Batteries)

	voltaic Cells (Battelles) Page 20	8
Big Ideas	Details Unit: DC Circui	ts
honors	Voltaic Cells (Batteries)*	
(not AP®)	Unit: DC Circuits	
İ	NGSS Standards/MA Curriculum Frameworks (2016): N/A	
	AP [®] Physics 2 Learning Objectives/Essential Knowledge (2024): N/A	
	Mastery Objective(s): (Students will be able to)	
	 Explain how a battery works. 	
	 Identify the components of a battery and their function. 	
	Success Criteria:	
	 Descriptions are accurate and components are identified correctly. 	
	Language Objectives:	
	 Explain how a battery works. (Domains: speaking, writing) 	
	 Identify the components of a battery and their function (Domains: speaking, writing) 	
	Tier 2 Vocabulary: battery, current	
	Labs, Activities & Demonstrations: building a voltaic cell 	
	Notes:	
	<u>voltaic cell</u> : (also called a galvanic cell) a chemical apparatus that uses an electrochemical reaction to produce electricity. (A battery is a type of galvanic cell.)	
	<u>electrochemistry</u> : using chemical oxidation & reduction (redox) reactions to produce electricity or vice-versa. In an electrochemical reaction, oxidation and reduction reactions occur in separate containers, and electrons travel from one container to the other. In physics, the chemical energy from the combination of the two reactions is the potential difference (voltage) that moves those electrons through an electric circuit.	è
	<u>electrolytic cell</u> : a cell similar to a galvanic cell, except that the reaction is nonspontaneous, and electricity is used to add the energy needed to make the reaction occur. (Electrolysis of water is an example.)	
	<u>electrode</u> : a solid metal strip where either oxidation or reduction occurs. The meta strips also conduct the electrons into or out of the electric circuit.	əl
	* Voltaic cells are taught in AP [®] Chemistry as part of the topic of electrochemistry. The topic is presented here in order to explain where the electric potential in a battery comes from.	

Voltaic Cells (Batteries)

Big Ideas	Details Unit: DC Circuits
honors	anode: the negatively (-) charged electrode. At the anode:
(not AP®)	• Oxidation occurs. (Atoms from the anode are oxidized into positive ions.)
	• These positive ions are released into the solution. (<i>I.e.</i> , the anode loses mass.)
	• The electrons produced by oxidation are forced through the wire toward the
	cathode via the electric circuit.
	cathode: the positively (+) charged electrode. At the cathode:
	• Reduction occurs. (Ions from the solution are reduced to neutral metal
	atoms.)
	 These metal atoms are deposited onto the cathode. (<i>I.e.</i>, the cathode gains mass.)
	• The electrons needed for reduction are brought in through the wire from the anode via the electric circuit.
	salt bridge: a salt solution that is connected to both half-cells. The salt bridge
	provides ions for the two half-cells in order to keep the charges balanced. (If the
	charges are not allowed to balance, opposite charges would build up in both cells and the reaction would stop.) The salt solution must be made of ions that
	do not take part in the reactions at the cathode or anode. (KNO ₃ is commonly
	used.)
	e e
	electric circuit
	anode salt bridge cathode
	(oxidation)
	$\begin{bmatrix} & & \\ & & \end{bmatrix}$ $\begin{bmatrix} Zn & \begin{bmatrix} & KCl \\ & & \end{bmatrix}$ $\begin{bmatrix} Cu & \end{bmatrix}$
	7 + 2 + 0
	Zn
	$\begin{bmatrix} Zn^{2+} \\ SO_4^{2-} \end{bmatrix}$ $\begin{bmatrix} Cu^{2+} \\ SO_4^{2-} \end{bmatrix}$
	$Zn(s) + 2e^- \longrightarrow Zn^{2+}$ $Cu^{2+} + 2e^- \longrightarrow Cu(s)$
i	

Voltaic Cells (Batteries)

		. 210
Big Ideas	Details Unit: DC Cir	
honors (not AP®)	standard voltage (<i>E</i> °): the voltage (electric potential) of an electrochemical reac under "standard conditions".	tion
	• "Standard conditions" means temperature is 25 °C, all ion concentrations	s are
	$1\frac{mol}{L}$, and all gas pressures are 1 atm. [*]	
	 The actual voltage of the cell, V, depends on the temperature, ion concentrations and gas pressures. At standard conditions, V = E°. 	
	• <i>E</i> ° values for reduction reactions are published in tables of Standard Reduction Potentials.	
	• <i>E</i> ° for an oxidation reaction is the negative of the <i>E</i> ° for the reverse (reduction) reaction. <i>(I.e.,</i> if you reverse the reaction, change the sign of	<i>E</i> °.)
	• The standard voltage of a cell is the sum of the standard voltages for the oxidation and reduction half-cells:	
	• $E^o = E^o_{reduction} + E^o_{oxidation}$	
	 If E^o > 0, then the reaction happens spontaneously. This is what happen when a battery is used to power a circuit. 	IS
	 If E^o <0, the reaction does not occur spontaneously, and energy is required to force the reaction to occur. This is what happens while a battery is charging. 	
	* You can tall that "standard conditions" were defined by showists. If they were defined by showist	sists
ļ	* You can tell that "standard conditions" were defined by chemists. If they were defined by physic standard pressure would be 1 bar rather than 1 atm.	lists,

EMF & Internal Resistance of a Battery

Unit: DC Circuits

Details

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): 11.5.B, 11.5.B.1.iii, 11.5.B.2, 11.5.B.3

Mastery Objective(s): (Students will be able to ...)

• Solve problems involving relationships between voltage, current, resistance and power.

Success Criteria:

- Variables are correctly identified and substituted correctly into the correct equation.
- Algebra is correct and rounding to appropriate number of significant figures is reasonable.

Language Objectives:

• Describe the relationships between voltage, current, resistance, and power.

Tier 2 Vocabulary: current, resistance, power

Labs, Activities & Demonstrations:

• batteries and resistors (< 10 Ω) to measure emf in a low-resistance circuit

Notes:

An ideal battery always supplies current at the voltage of the electrochemical cells inside of it. In a real battery, the voltage is a little less when the battery is "under load" (supplying current to a circuit) than when it is tested with no load. This difference is caused by real-world limitations of the chemical and physical processes that occur inside of the battery.

<u>electromotive force (emf)</u>: the potential difference (voltage) supplied by a battery without load. This is the stated voltage of the battery. The term "electromotive force" literally means "electron-moving force". EMF is often represented by the variable ε .

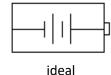
<u>voltage</u>: the observed potential difference between two points in a circuit. The voltage of a battery usually means the voltage under load.

<u>internal resistance</u> (r): a model that explains the difference between the emf of a battery and the voltage (potential difference) it can supply as if the drop in voltage were caused by a resistor inside of the battery. In this course, we will use the variable R for the resistance of components in a circuit, and r for internal resistance. ideal battery: a battery that has no internal resistance.

Big Ideas

Details

To account for internal resistance, we model a battery as if it were a power supply with the ideal voltage, plus a resistor that is physically inside of the battery.





model

Note that this is a model; the actual situation is more complex, because in addition to the resistivity of the battery's component materials, the difference between the internal voltage and the supplied voltage also depends on factors such as electrolyte conductivity, ion mobility, and electrode surface area.

The following table shows the nominal voltage and internal resistance of common Duracell (coppertop) dry cell batteries of different sizes. These numbers are given by the manufacturer for a new battery at room temperature (25°C):

Size	AAA	AA	С	D	9V
V _{NL} (V)	1.5	1.5	1.5	1.5	9
<i>R_{int}</i> (mΩ)	250	120	150	137	1700

The internal resistance can be used to calculate the maximum current that a battery could theoretically supply. If you were to connect a wire from the positive terminal of a battery to the negative terminal, the only resistance in the circuit should be the battery's internal resistance.

The theoretical maximum current that the battery can supply is therefore the current that would be supplied when the only resistance is the battery's internal resistance, and can be calculated from Ohm's Law:

$$I_{\max} = \frac{\Delta V}{r}$$

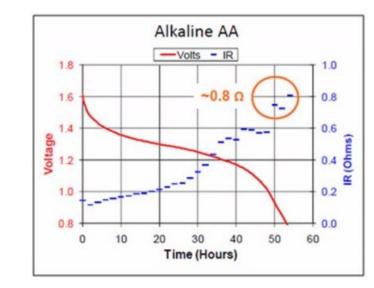
This concept can be used in circuit analysis by using the following equation:

$$\Delta V_{terminal} = \mathcal{E} - Ir$$

This equation states that the voltage (potential difference) across the terminals of the battery is the battery's emf minus the potential difference that is "used up" by the internal resistance.

EMF & Internal Resistance of a Battery

Note also that the factors that affect a battery's internal resistance change as the battery ages. The following graph shows the changes in voltage and internal resistance of an alkaline AA battery as it supplied a current of 50 mA over a duration of about 52 hours.



honors (not AP®) Internal resistance can be calculated by measuring the voltage with no "load" on the battery (*i.e.,* the voltmeter is connected directly to the battery with nothing else in the circuit) and the voltage with "load" (*i.e.,* the battery is connected to a circuit with measurable resistance):

$$R_{\rm int} = \left(\frac{\Delta V_{NL}}{\Delta V_{FL}} - 1\right) R_L$$

where:

Details

Big Ideas

 R_{int} = internal resistance of battery

 ΔV_{FL} = voltage measured with full load (resistor with resistance R_L in circuit)

- $\Delta V_{\scriptscriptstyle NL}$ = voltage measured with no load (voltmeter connected directly to battery)
- *R_L* = resistance of the load (resistor) that is used to experimentally determine the internal resistance of the battery

ig Ideas	Circuits Page: 22 Details Unit: DC Circu
ueas	
	Circuits
	Unit: DC Circuits
	NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-9(MA)
	AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 11.2.A, 11.2.A.1, 11.2.A.2, 11.2.A.2.i, 11.2.A.2.ii, 11.2.A.2.iii, 11.2.A.3, 11.2.A.4, 11.2.A.4.i, 11.2.A.4.ii
	Mastery Objective(s): (Students will be able to)
	 Identify electrical circuits or sections of circuits as series or parallel.
	Success Criteria:
	• Descriptions correctly identify the component.
	 Descriptions correctly describe which type of circuit (series or parallel) the component is in.
	Language Objectives:
	 Identify which components are in series vs. parallel in a mixed circuit.
	Tier 2 Vocabulary: series, parallel
	Labs, Activities & Demonstrations:
	Example circuit with light bulbs & switches.
	 Fuse demo using a single strand from a multi-strand wire.
	• Fuse demo using a single strand norm a multi-strand wire.
	Notes:
	circuit: an arrangement of electrical components that allows electric current to pa through them so that the tasks performed by the individual components combine in some useful way.
	<u>closed circuit</u> : a circuit that has a complete path for current to flow from the positiv terminal of the battery or power supply through the components and back to the negative terminal.
	open circuit: a circuit that has a gap such that current cannot flow from the positive terminal to the negative terminal.
	short circuit: a circuit in which the positive terminal is connected directly to the negative terminal with no load (resistance) in between.
	If we assume that wires have essentially no resistance, then a short circuit draw essentially infinite current. In a household with 110 V wiring, a short circuit ca quickly produce enough heat to start a fire. This is why circuits need to be protected with fuses or circuit breakers.

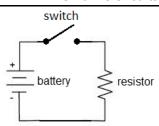
Circuits

A diagram of a simple electric circuit might look like the diagram to the right.

Big Ideas

Details

When the switch is closed, the electric current flows from the positive terminal of the battery through the switch, through the resistor, and back to the negative terminal of the battery.



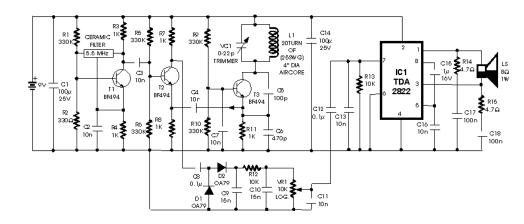
An electric circuit needs a power supply (often a battery) that provides current at a specific voltage (electric potential difference), and one or more components that use the energy provided.

The battery or power supply continues to supply current, provided that:

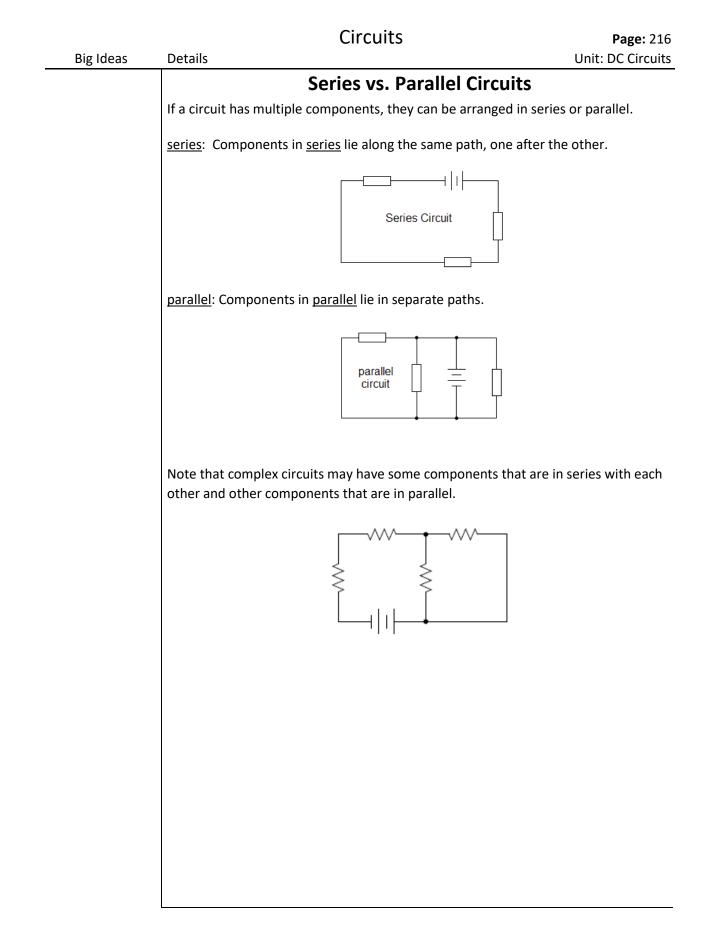
- 1. There is a path for the current to flow from the positive terminal to the negative terminal, and
- 2. The total resistance of the circuit is small enough to allow the current to flow.

If the circuit is broken, current cannot flow and the chemical reactions inside the battery stop.

As circuits become more complex, the diagrams reflect this increasing complexity. The following is a circuit diagram for a metal detector:



Analyzing an electrical circuit means figuring out the potential difference (voltage), current, and/or resistance contributed by each component of a circuit.

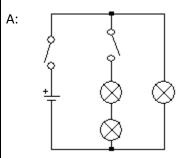


Sample Problem:

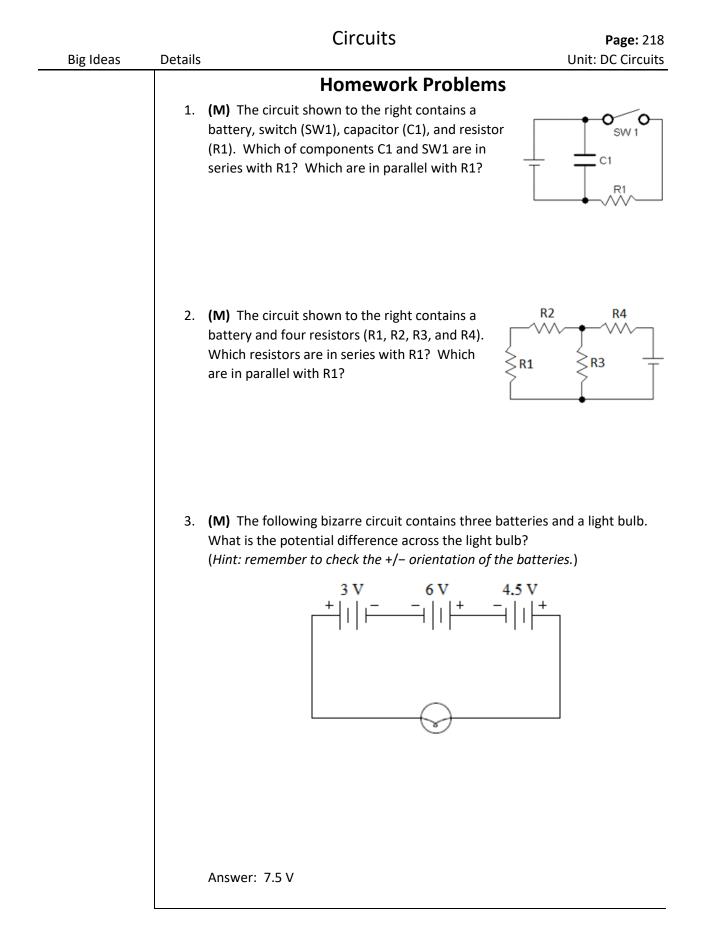
Details

Big Ideas

Q: A circuit consists of a battery, two switches, and three light bulbs. Two of the bulbs are in series with each other, and the third bulb is in parallel with the others. One of the switches turns off the two light bulbs that are in series with each other, and the other switch turns off the entire circuit. Draw a schematic diagram of the circuit, using the correct symbol for each component.



Note that no sensible person would intentionally wire a circuit this way. It would make much more sense to have the second switch on the branch with the one light bulb, so you could turn off either branch separately or both branches by opening both switches. This is an example of a strange circuit that a physics teacher would use to make sure you really can follow exactly what the question is asking!



Big Ideas	Details	Unit: DC Circuit
	Kirchhoff's Rules	
	Unit: DC Circuits	
	NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-9	(MA)
	AP [®] Physics 2 Learning Objectives/Essential Knowledge (2024): 11.6.A.2, 11.6.A.3, 11.6.A.4, 11.7.A, 11.7.A.1, 11.7.A.2	11.6.A, 11.6.A.1,
	Mastery Objective(s): (Students will be able to)	
	 Apply Kirchhoff's junction and loop rules to determine vol- circuits. 	tages and currents i
	Success Criteria:	
	Loop rule correctly applied (electric potential differences a	add to zero).
	 Junction rule correctly applied (total current into a junctio current out). 	n equals total
	Language Objectives:	
	• Explain why electric potential has to add to zero around a current into a junction has to add up to current out.	loop and why
	Tier 2 Vocabulary: loop, junction	
	Labs, Activities & Demonstrations:	
	 model a circuit by walking up & down stairs 	
	Notes:	
	In 1845, the German physicist Gustav Kirchhoff came up with tw describe the behavior of current in complex circuits. Those rules	
	Kirchhoff's junction rule: the total current coming into a junctio total current coming out of the junction.	n must equal the
	The junction rule is based on the concept of conservation of Current is simply the flow of electric charge, so any charges junction must also come out of it.	-
	Kirchhoff's loop rule: the sum of the voltages around a closed lo zero.	oop must add up to
	The loop rule is based on the concept that voltage is the diff potential between one location in the circuit and another. If the same point in the circuit, the difference in electric poten you started and where you ended (the same place) must be any increases and decreases in voltage around the loop must	f you come back to tial between where zero. Therefore,

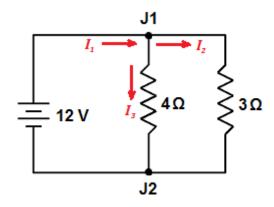
Kirchhoff's Rules

Junction Rule Example:

Details

Big Ideas

As an example of the junction rule, consider the following circuit:



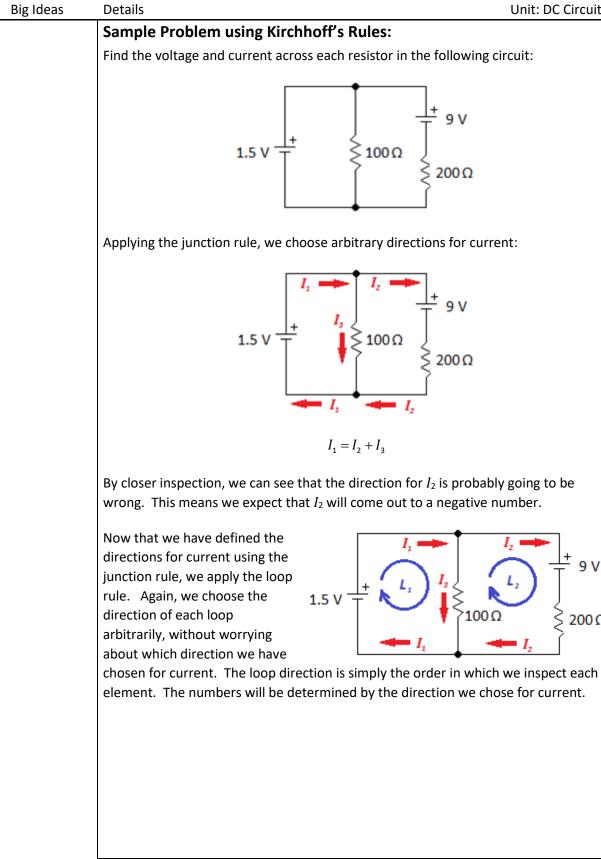
The junction rule tells us that the current flowing into junction J1 must equal the current flowing out. If we assume current I_1 flows into the junction, and currents I_2 and I_3 flow out of it, then $I_1 = I_2 + I_3$.

We know that the voltage across both resistors is 12 V. From Ohm's Law we can determine that the current through the 3 Ω resistor is $I_2 = 4$ A, and the current through the 4 Ω resistor is $I_3 = 3$ A. The junction rule tells us that the total current must therefore be:

$$I_1 = I_2 + I_3 = 4A + 3A = 7A$$

	Kirchhoff's Rules	Page: 221
Big Ideas	Details	Unit: DC Circuits
	Loop Rule Example:	
	For the loop rule, consider the circuit to the right:]
	If we start at point A and move counterclockwise around the loop (in the direction of the arrow), the voltage should be zero when we get back to point A. $\frac{-1}{+} 6V$	
	For this example, we are moving around the	}
	circuit in the same direction that the current flows, because that makes the most intuitive sense. However, it we we moved clockwise instead—just as with vector quantities, we cho direction and assign each quantity to a positive or negative number the math tells us what is actually happening.	oose a positive
	Starting from point A, we first move through the 6 V battery. We ar the negative pole to the positive pole of the battery, so the voltage +6 V. When we move through the second battery, the voltage incre	increases by
	Next, we move through the 15Ω resistor. When we move through positive direction (of current flow), the voltage drops, so we assign voltage of $-15I$ (based on $V = IR$, where I is the current through the Similarly, the voltage across the 10Ω resistor is $-10I$. Applying the	the resistor a resistor).
	6+3+(-15I)+(-10I)=0	
	9-25I=0	
	9 = 25I	
	$I = \frac{9}{25} = 0.36 \text{ A}$	
	Now that we know the total current, we can use it to find the voltage difference) across the two resistors.	ge drop (potential
	$\Delta V_{10\Omega} = IR = (0.36)(10) = 3.6 \text{ V}$ $\Delta V_{15\Omega} = IR = (0.36)(15)$	=5.4 V

Kirchhoff's Rules



9 V

200 Ω

Kirchhoff's Rules

As we inspect our way around the loop, there are two rules for determining the
voltage across each component:

 Voltage across a battery is *positive* if the loop direction is *from negative to positive* (the "forward" direction).
 Voltage across a battery is *negative* if the loop direction is *from positive to*

Voltage across a battery is *negative* if the loop direction is from positive to *negative* (the "backward" direction).

Voltage across a resistor is *negative* if the loop direction is *with the current* (the resistor is "using up" voltage).
 Voltage across a resistor is *positive* if the loop direction is *against the current* (we are traveling from a place where the electric potential is lower to a place where it is higher).

Now we inspect our way around each loop, writing the equations for the voltages:

L1:
$$+1.5 - 100I_3 = 0 \rightarrow I_3 = 0.015 \text{ A}$$

Big Ideas

Details

L2:
$$-9 - 200I_2 + 100I_3 = 0$$

 $-9 - 200I_2 + 1.5 = 0$
 $-7.5 = 200I_2$
 $I_2 = -0.0375 \text{ A}$
 $I_1 = I_2 + I_3 = -0.0375 + 0.015 = -0.0225 \text{ A}$

 I_3 came out to a positive number, meaning that the current is flowing in the direction that we chose initially. However, I_1 and I_2 both came out negative, meaning that the current in those two segments of the circuit is actually flowing in the opposite direction from the arbitrary direction that we chose at the beginning of the problem.

Now that we know the current and resistance, we can find the voltage drop across each resistor using Ohm's Law.

100 Ω : $V = I_3 R = (0.015)(100) = 1.5 V$

200 Ω : $V = I_2 R = (-0.0375)(200) = -7.5 V$

Again, the negative sign shows that the voltage drop (from positive to negative) is in the opposite direction from what we originally chose.

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-9(MA)

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 11.5.A, 11.5.A.1, 11.5.A.1.i, 11.5.A.2, 11.5.A.2.i, 11.5.B, 11.5.B.1, 11.5.B.1.i, 11.5.B.1.ii

Mastery Objective(s): (Students will be able to...)

• Calculate voltage, current, resistance and power in series circuits.

Success Criteria:

- Correct relationships are applied for voltage, current, resistance and power in series circuits.
- Variables are correctly identified and substituted correctly into the correct equations.
- Algebra is correct and rounding to appropriate number of significant figures is reasonable.

Language Objectives:

• Explain the relationships for voltages, current, resistance and power in series circuits.

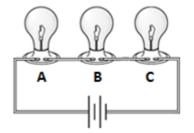
Tier 2 Vocabulary: series, circuit

Labs, Activities & Demonstrations:

• Circuit with light bulbs wired in series.

Notes:

series: Components in series lie along the same path, one after the other.



In a series circuit, all of the current flows through every component, one after another. If the current is interrupted anywhere in the circuit, no current will flow. For example, in the following series circuit, if any of the light bulbs A, B, or C is removed, no current can flow and none of the light bulbs will be illuminated.

Because some of the electric potential energy (voltage) is "used up" by each bulb in the circuit, each additional bulb means the voltage is divided among more bulbs and is therefore less for each bulb. This is why light bulbs get dimmer as you add more bulbs in series.

Christmas tree lights used to be wired in series. This caused a lot of frustration, because if one bulb burned out, the entire string went out, and it could take several tries to find which bulb was burned out.

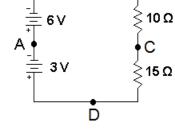
The diagram to the right shows two batteries and two resistors in series.

Current

Details

Big Ideas

Because there is only one path, all of the current flows through every component. This means the current is the same through every component in the circuit:



в

Voltage

In a series circuit, if there are multiple voltage sources (*e.g.*, batteries), the voltages add:

 $I_{total} = I_1 = I_2 = I_3 = \dots$

$$\Delta V_{total} = \Delta V_1 + \Delta V_2 + \Delta V_3 + \dots$$

In the above circuit, there are two batteries, one that supplies 6V and one that supplies 3V. The voltage from A to B is +6V, the voltage from A to D is -3V (note that A to D means measuring from negative to positive), and the voltage from D to B is (+3V) + (+6V) = +9V.

Resistance

If there are multiple resistors, each one contributes to the total resistance and the resistances add:

$$R_{total} = R_1 + R_2 + R_3 + \dots$$

In the above circuit, the resistance between points B and D is $10\Omega + 15\Omega = 25\Omega$.

Power

In all circuits (series and parallel), any component that has resistance dissipates power whenever current passes through it. The total power consumed by the circuit is the sum of the power dissipated by each component:

$$P_{total} = P_1 + P_2 + P_3 + \dots$$

Calculations

Details

Big Ideas

You can calculate the voltage, current, resistance, and power of each component separately, any subset of the circuit, or entire circuit, using the equations:

 $\Delta V = IR \qquad P = I\Delta V = I^2 R = \frac{(\Delta V)^2}{R}$

"Solving" the circuit for these quantities is much like solving a Sudoku puzzle. You systematically decide which variables (for each component and/or the entire circuit) you have enough information to solve for. Each result enables you to determine more and more of them, until you have found all of the quantities you need.

Sample Problem:

Suppose we are given the following series circuit:

	〕		Var.	R ₁	R ₂	Total
	\gtrsim R1 = 10 Ω	Voltage (V)	ΔV			9
¥9 ۷	Ĵ	Current (A)	Ι			
-	R2 = 15 Ω	Resistance (Ω)	R	10	15	
		Power (W)	Р			

and we are asked to fill in the following table:

First, we recognize that resistances in series add, which gives us:

	Var.	R ₁	R ₂	Total
Voltage (V)	ΔV			9
Current (A)	Ι			
Resistance (Ω)	R	10	15	25
Power (W)	Р			

Now, we know two variables in the "Total" column, so we use $\Delta V = IR$ to find the current.

$$\Delta V = IR$$

9 = (I)(25)
$$I = \frac{9}{25} = 0.36 \text{ A}$$

Big Ideas Details

Because this is a series circuit, the total current is also the current through R_1 and R_2 .

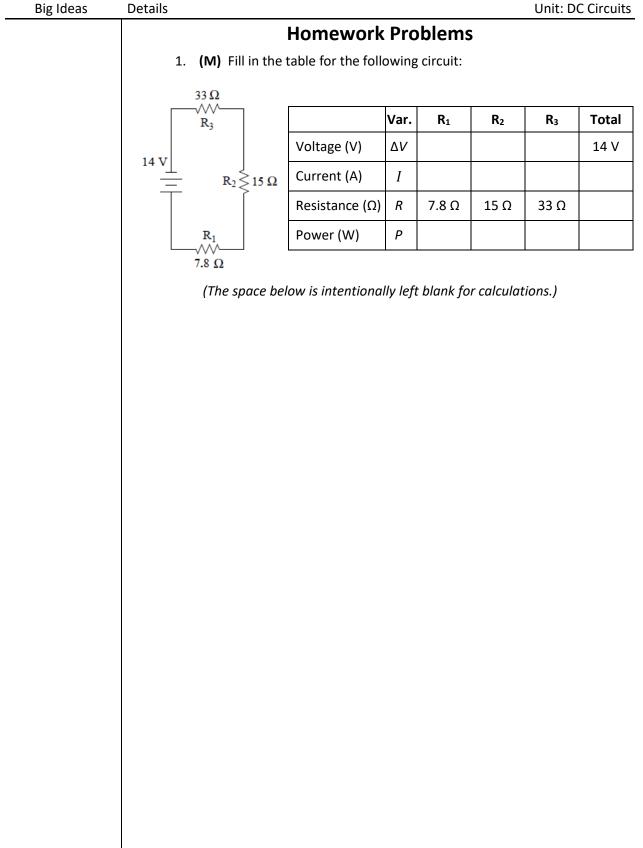
	Var.	R ₁	R ₂	Total
Voltage (V)	ΔV			9
Current (A)	Ι	0.36	0.36	0.36
Resistance (Ω)	R	10	15	25
Power (W)	Р			

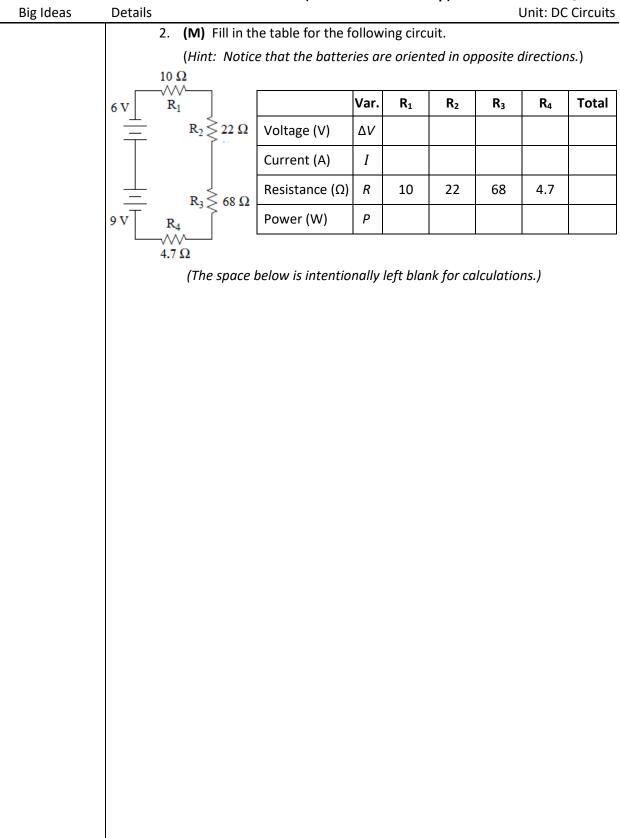
As soon as we know the current, we can find the voltage across R_1 and R_2 , again using $\Delta V = IR$.

	Var.	R ₁	R ₂	Total
Voltage (V)	ΔV	3.6	5.4	9
Current (A)	Ι	0.36	0.36	0.36
Resistance (Ω)	R	10	15	25
Power (W)	Р			

Finally, we can fill in the power, using $P = I \Delta V$:

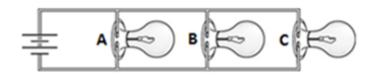
	Var.	R ₁	R ₂	Total
Voltage (V)	ΔV	3.6	5.4	9
Current (A)	Ι	0.36	0.36	0.36
Resistance (Ω)	R	10	15	25
Power (W)	Р	1.30	1.94	3.24





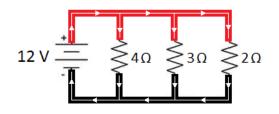
Details Unit: DC Circuits
Parallel Circuits (Resistance Only)
Unit: DC Circuits
NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-9(MA)
AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 11.5.A, 11.5.A.1,
11.5.A.1.ii, 11.5.A.2, 11.5.A.2.ii, 11.5.A.2.iii
Mastery Objective(s): (Students will be able to)
 Calculate voltage, current, resistance and power in parallel circuits.
Success Criteria:
 Correct relationships are applied for voltage, current, resistance and power in parallel circuits.
 Variables are correctly identified and substituted correctly into the correct equations.
 Algebra is correct and rounding to appropriate number of significant figures is reasonable.
Language Objectives:
• Explain the relationships for voltages, current, resistance and power in paralle
circuits.
Tier 2 Vocabulary: parallel
Labs, Activities & Demonstrations:
• Circuit with light bulbs wired in parallel.
Notes:
parallel: Components in parallel lie in separate paths.
parallel
In a parallel circuit, the current divides at each junction, with some of the current flowing through each path. If the current is interrupted in one path, current can still flow through the other paths.

For example, in the parallel circuit below, if any of light bulbs A, B, or C is removed, current still flows through the remaining bulbs.



Because the voltage across each branch is equal to the total voltage, all of the bulbs will light up with full brightness, regardless of how many bulbs are in the circuit. (However, each separate light bulb draws the same amount of current as if it were the only thing in the circuit, so **the total current in the circuit increases with each new branch**. This is why you trip a circuit breaker or blow a fuse if you have too many high-power components plugged into the same circuit.)

The following circuit shows a battery and three resistors in parallel:



Current

Big Ideas

Details

The current divides at each junction (as indicated by the arrows). This means the current through each path must add up to the total current:

$$I_{total} = I_1 + I_2 + I_3 + \dots$$

Voltage

In a parallel circuit, the potential difference (voltage) across the battery is always the same (12 V in the above example). Therefore, the potential difference between *any point* on the top wire and *any point* on the bottom wire must be the same. This means the voltage is the same across each path:

$$V_{total} = V_1 = V_2 = V_3 = \dots$$

Resistance

If there are multiple resistors, the effective resistance of each path becomes less as there are more paths for the current to flow through. The total resistance is given by the formula:

$$\frac{1}{R_{total}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$$

/)

Big Ideas Details Unit: DC Circuits Some students find it confusing that the combined resistance of a group of resistors in series is always less than any single resistor by itself. Power Just as with series circuits, in a parallel circuit, any component that has resistance dissipates power whenever current passes through it. The total power consumed by the circuit is the sum of the power dissipated by each component: $P_{total} = P_1 + P_2 + P_3 + \dots$ Electric current is analogous to water in a pipe: • The current corresponds to the flow rate. • The voltage corresponds to the pressure between one side and the other. The resistance would correspond to how small the pipe is (i.e., how hard it is to push water through the pipes). A smaller pipe has more resistance; a larger pipe will let water flow through more easily than a smaller pipe. The voltage (pressure) drop is the same between one side and the other because less water flows through the smaller pipes and more water flows through the larger ones until the pressure is completely balanced. The same is true for electrons in a parallel circuit. The water will flow through the *set* of pipes more easily than it would through any one pipe by itself. The same is true for resistors. As you add more resistors, you add more pathways for the current, which means less total resistance. Another common analogy is to compare resistors with toll booths on a highway. Influencing the Flow Rate on a Tollway One toll booth slows cars down while the drivers pay the toll. Multiple toll booths in a row would slow traffic down more. This is analogous to resistors in series. Multiple toll booths next to each other (in parallel) make traffic flow faster because there are more paths for the Placed in Paralle cars to follow. Each toll booth further reduces the resistance to the flow of traffic.

Calculations

Details

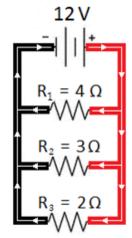
Big Ideas

Just as with series circuits, you can calculate the voltage, current, resistance, and power of each component and the entire circuit using the equations:

$$\Delta V = IR \qquad P = I\Delta V = I^2 R = \frac{(\Delta V)^2}{R}$$

Sample Problem

Suppose we are given the following parallel circuit:



and we are asked to fill in the following table:						
	Var.	R1	R ₂	R ₃	Total	
Voltage (V)	ΔV				12	
Current (A)	Ι					
Resistance (Ω)	R	4	3	2		
Power (W)	Р					

Because this is a parallel circuit, the total voltage equals the voltage across all three branches, so we can fill in 12 V for each resistor.

The next thing we can do is use $\Delta V = IR$ to find the current through each resistor:

	Var.	R1	R ₂	R₃	Total
Voltage (V)	ΔV	12	12	12	12
Current (A)	Ι	3	4	6	13
Resistance (Ω)	R	4	3	2	
Power (W)	Р				

In a parallel circuit, the current adds, so the total current is 3 + 4 + 6 = 13 A.

Now, we have two ways of finding the total resistance. We can use $\Delta V = IR$ with the total voltage and current:

$$\Delta V = IR$$

$$12 = 13R$$

$$R = \frac{12}{13} = 0.923 \Omega$$

Physics 2 In Plain English

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Big Ideas	Details			-			Unit: DC Circ
		an use the formu	la for	resistances	in 💦	71 04 Di	us Silver Edition
	$\frac{1}{R_{total}} =$ Instead it is usua function calculate the pictor	$\frac{1}{R_{total}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_2} + \frac{1}{R_1} + \frac{1}{R_2} $	$\frac{4}{12} + \frac{6}{12}$ 3 Ω mon d e the 1 On a n wou	enominato L/x or x ^{−1} TI-84 Ild look like	r,	Ф Техая 4 ⁻¹ +3 ⁻¹ +3 1. Ans ⁻¹	5 INSTRUMENTS 2 ⁻¹ 0833333333 230769231
		n the picture.)				LOG 7 LN 4 STO) LN 0 STO) DN 0 0	
	circled in					IN LA REL 4 STOT ON CATALOG	1 Constraints of the second se
			Var.	R ₁	R ₂	IN LA REL 4 STOT ON CATALOG	1 Constraints of the second se
			Var. ΔV	R 1 12 V	U	LN 4 STOP ON CANADA	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
		have:			R ₂	LN 4 STOD ON 0 Radia 4 STOD ON 0 Radia 4 Control 1 ON 0 Radia 4 Control 1 ON 0 Control 1 Control	5 6 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
		have: Voltage (V)	ΔV	12 V	R ₂ 12 V	R ₃ 12 V	5 6 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7

	Var.	R ₁	R ₂	R₃	Total
Voltage (V)	ΔV	12	12	12	12
Current (A)	Ι	3	4	6	13
Resistance (Ω)	R	4	3	2	0.923
Power (W)	Ρ	36	48	72	156

	Parallel	Lircuits (Resista	ince (Jnly)		Page: 23			
Big Ideas	Details					Unit: DC Circuit			
	Batteries in Paralle	:I							
	One question that has connected in parallel.	not been answered ye	et is wh	at happe	ens when	batteries are			
		the batteries have the same voltage, the potential difference (voltage) remains the me, but the total current is the combined current from the two batteries.							
	However, if the batter battery attempts to ma terminals. This results battery.	aintain a constant pot	ential d	ifferenc	e (voltage	e) between its			
	Remember that physic chemical reactors with overcharges the other, the cathode becomes battery bursts, and the	redox reactions takin , material is deposited physically too large fo	g place on the	in each cathode	cell. If or e (positive	ne battery e terminal) unti			
	Light Bulbs								
	Electric light bulbs, wh	ich were commercializ	zed by T	homas	Edison				
	in 1880, use electrical	energy to produce ligh	nt. For a	about					
	100 years, most light b				-	((M))			
	electricity through a tu	ingsten filament until	it glows	white-h	not.	• 1			
	Newer light bulbs, such	h as fluorescent bulbs	or light	-emittin	g diode	一个			
	(LED) bulbs, produce s	•	t but m	uch less	heat,				
	making them much mo	ore energy efficient.							
	The S.I. unit for light in	tensity is the lumen (l	m).						
		Intensity (lm)	560	800	1100	1600			
	Incandesco	ent Bulb Power (W) [*]	40	60	75	100			
	Incandescent	Bulb Resistance (Ω) ⁺	360	240	192	144			
	L	ED Bulb Power (W) [*]	2–3	7–10	10–15	15–20			
	LED	Bulb Resistance (Ω)	5760	1700	1150	820			

* Assuming a 120 V household circuit.

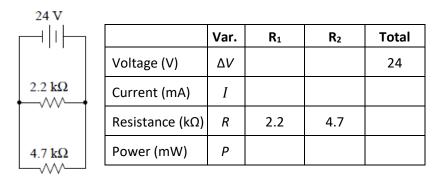
⁺ Note that incandescent light bulbs are not ohmic resistors, meaning their resistance changes as the current changes because the heat generated affects the resistivity of the tungsten filament.

	Parallel Circuits (Resistance Only)	Page: 236
Big Ideas	Details	Unit: DC Circuits
	The amount of light that a light bulb produces is proportional to the power it consumes. For over 100 years, incandescent bulbs were so their power rating (in watts), and people developed an understand light a typical incandescent bulb would produce in a 120 V househow that the power consumed by a light bulb is a function of both the covoltage: $P = I \Delta V$.	old according to ing of how much old circuit. Note
	 In a parallel circuit (such as you would find in your house), to constant. The resistance of a component determines how draws. A component with lower resistance (<i>e.g.</i>, a light bu "wattage" rating) draws more current and therefore uses no means a bulb with a higher "wattage" rating will be <u>brighter</u> circuit. 	much current it lb with a higher nore power. This
	 circuit. In a series circuit, the current through each bulb is constant is only one path). The voltage across the entire circuit is fix voltage across each component splits according to the com resistance. A component with less resistance (<i>e.g.</i>, a light t "wattage" rating) "uses up" less of the total voltage and the power. This means a bulb with a higher "wattage" rating v a series circuit. 	ed, but the ponent's pulb with a higher erefore uses less



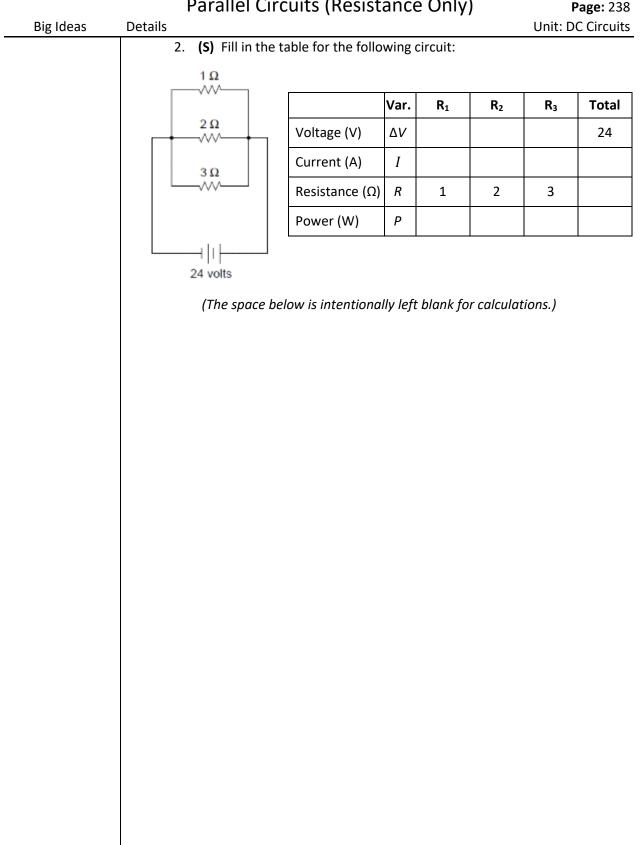
Homework Problems

1. (M) Fill in the table for the following circuit:



Note: the above units can be used directly with $\Delta V = IR$ and $P = I\Delta V$ without converting. (Because volts = milliamps × kiloöhms and milliwatts = milliamps × volts.)

(The space below is intentionally left blank for calculations.)



	Parallel (Circu	its (Re	sistance	e Only)		Page: 2
Big Ideas	Details					I	Unit: DC Circ
	3. (M) Fill in $1 k\Omega \leq R_1^{2.2}$	kΩ	4 vol	•	circuit: 6.8 kΩ	47 ≷R₃	$0 \Omega $
		Var.	R ₁	R ₂	R ₃	R4	Total
	Voltage (V)	ΔV					4
	Current (mA)	Ι					
	Resistance (kΩ)	R	1	2.2	6.8	0.47	
	Power (mW)	Р					
	without co milliwatts	onvertii = millio	ng. (Beca amps × vo	use volts = lts.)	milliamps		

Unit: DC Circuits

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-9(MA)

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 11.5.A, 11.5.A.1,

11.5.A.1.i, 11.5.A.1.ii, 11.5.A.2, 11.5.A.2.i, 11.5.A.2.ii, 11.5.A.2.iii

Mastery Objective(s): (Students will be able to...)

• Calculate voltage, current, resistance and power in mixed series & parallel circuits.

Success Criteria:

- Correct relationships are applied for voltage, current, resistance and power in mixed series & parallel circuits.
- Variables are correctly identified and substituted correctly into the correct equations.
- Algebra is correct and rounding to appropriate number of significant figures is reasonable.

Language Objectives:

• Explain the relationships for voltages, current, resistance and power in mixed series & parallel circuits.

Tier 2 Vocabulary: series, parallel

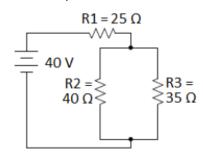
Labs, Activities & Demonstrations:

• light bulb mystery circuits

Notes:

If a circuit has mixed series and parallel sections, you can determine the various voltages, currents and resistances by applying Kirchhoff's Rules and/or by "simplifying the circuit." Simplifying the circuit, in this case, means replacing groups of resistors that are in series or parallel with a single resistor of equivalent resistance.

For example, suppose we need to solve the following mixed series & parallel circuit for voltage, current, resistance and power for each resistor:



Because the circuit has series and parallel sections, we cannot simply use the series and parallel rules across the entire table.

	Var.	R ₁	R ₂	R₃	Total
Voltage (V)	ΔV				40
Current (A)	Ι				
Resistance (Ω)	R	25	40	35	
Power (W)	Р				

We can use Ohm's Law ($\Delta V = IR$) and the power equation ($P = I \Delta V$) on each individual resistor and the totals for the circuit (columns), but we need two pieces of information for each resistor in order to do this.

Our strategy will be:

Big Ideas

Details

- 1. Simplify the resistor network until all resistances are combined into one equivalent resistor to find the total resistance.
- 2. Use $\Delta V = IR$ to find the total current.
- 3. Work backwards through your simplification, using the equations for series and parallel circuits in the appropriate sections of the circuit until you have all of the information.

Step 1: If we follow the current through the circuit, we see that it goes through resistor R1 first. Then it splits into two parallel pathways. One path goes through R2 and R3, and the other goes through R4 and R5.

There is no universal shorthand for representing series and parallel components, so let's define the symbols "—" to show resistors in series, and " \parallel " to show resistors in parallel. The above network of resistors could be represented as:

R1 − (R2 || R3)

Now, we simplify the network just like a math problem—start with the innermost parentheses and work your way out.

Unit: DC Circuits

Details **Big Ideas**

Step 2: Combine the parallel 40 Ω and 35 Ω resistors into a single equivalent resistance:

$$25 \Omega - (40 \Omega \parallel 35 \Omega) \longrightarrow 25 \Omega - (R_{eq.,||})$$

$$\frac{1}{R_{total}} = \frac{1}{40} + \frac{1}{35}$$
$$\frac{1}{R_{total}} = 0.0250 + 0.0286 = 0.0536$$
$$R_{total} = \frac{1}{0.0526} = 18.\overline{6}\Omega$$

0.0536

Now our circuit is equivalent to:

Step 3: Add the two resistances in series to get the total combined resistance of the circuit:

$$25 \Omega - 18.\overline{6} \Omega \longrightarrow R_{total}$$

$$18.\overline{6} + 25 = 43.\overline{6} \Omega$$

This gives:

	Var.	R ₁	R ₂	R ₃	Total
Voltage (V)	ΔV				40
Current (A)	Ι				
Resistance (Ω)	R	25	40	35	43. 6
Power (W)	Ρ				

Unit: DC Circuits

Step 4: Now that we know the total voltage and resistance, we can use Ohm's Law to find the total current:

$$\Delta V = IR$$

$$40 = I(43.\overline{6})$$

$$I = \frac{40}{43.\overline{6}} = 0.916 \text{ A}$$

While we're at it, let's use $P = I\Delta V = (0.916)(40) = 36.6$ W to find the total power.

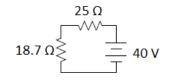
	Var.	R ₁	R ₂	R ₃	Total
Voltage (V)	ΔV				40 V
Current (A)	Ι				0.916
Resistance (Ω)	R	25	40	35	43.6
Power (W)	Р				36.6

Now we work backwards.

Big Ideas

Details

The next-to-last simplification step was:



The 25 Ω resistor is R1. All of the current goes through it, so the current through R1 must be 0.916 A. Using Ohm's Law, this means the voltage drop across R1 must be:

$$\Delta V = IR = (0.916)(25) = 22.9 V$$

and the power must be:

$$P = I \Delta V = (0.916)(22.9) = 21.0 \text{ W}$$

This means that the voltage across the parallel portion of the circuit (R2 \parallel R3) must be 40 – 22.9 = 17.1 V. Therefore, the voltage is 17.1 V across *both* parallel branches (because voltage is the same across parallel branches).

	Var.	R1	R ₂	R₃	Total
Voltage (V)	ΔV	22.9	17.1	17.1	40
Current (A)	Ι	0.916			0.916
Resistance (Ω)	R	25	40	35	43.6
Power (W)	Р	21.0			36.6

Unit: DC Circuits

We can use this and Ohm's Law to find the current through one branch:

$$\Delta V_{40\,\Omega} = \Delta V_{35\,\Omega} = 40 - \Delta V_1 = 40 - 22.9 = 17.1V$$
$$\Delta V_{40\,\Omega} = I_{40\,\Omega} R_{40\,\Omega}$$
$$I_{40\,\Omega} = \frac{\Delta V_{40\,\Omega}}{R_{40\,\Omega}} = \frac{17.1}{40} = 0.428 \text{ A}$$

We can use Kirchhoff's Junction Rule to find the current through the other branch:

$$I_{total} = I_{40 \Omega} + I_{35 \Omega}$$

0.916 = 0.428 + $I_{35 \Omega}$
 $I_{35 \Omega}$ = 0.488 A

This gives us:

Details

Big Ideas

	Var.	R1	R ₂	R₃	Total
Voltage (V)	ΔV	22.9	17.1	17.1	40
Current (A)	Ι	0.916	0.428	0.488	0.916
Resistance (Ω)	R	25	40	35	43.6
Power (W)	Р	21.0			36.6

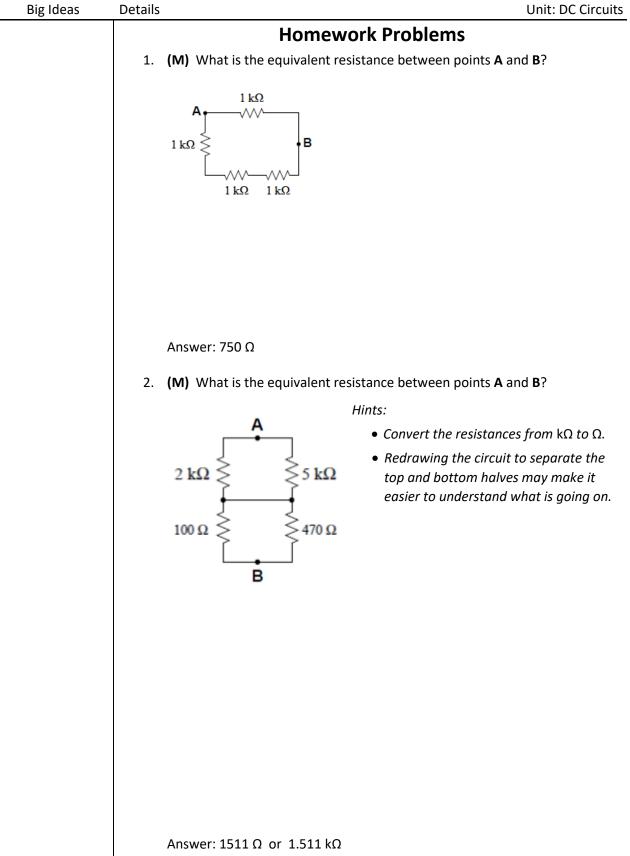
Finally, because we now have current and resistance for each of the resistors R_2 and R_3 , we can use $P = I\Delta V$ to find the power:

$$P_2 = I_2 \Delta V_2 = (0.428)(17.1) = 7.32 \text{ W}$$

$$P_3 = I_3 \Delta V_3 = (0.488)(17.1) = 8.34 \text{ W}$$

	Var.	R ₁	R ₂	R₃	Total
Voltage (V)	ΔV	22.9	17.1	17.1	40
Current (A)	Ι	0.916	0.428	0.488	0.916
Resistance (Ω)	R	25	40	35	43.6
Power (W)	Ρ	21.0	7.32	8.34	36.6

Alternately, because the total power is the sum of the power of each component, once we had the power in all but one resistor, we could have subtracted from the total to find the last one.



Big Ideas Details	ance Only) Page: 246 Unit: DC Circuits
	Unit: DC Circuits
Answer: 80.5 Ω	

Details						Unit: D	0 000
4. (N	/) Fill in the ta	ble for the circuit b	pelow:				
	12 V						
	┍──┤╎│┝───	1	Var.	R ₁	R ₂	R ₃	Tota
R3 \$	≷ 470 Ω	Voltage (V)	ΔV	-		5	12
	130 Ω	Current (A)	Ι				
		Resistance (Ω)	R	220	130	470	
R ₁	≥ 220 Ω	Power (W)	Р				
¹	> 220 32		1 1			I	1
l							
	The space b	alaw is intentiona		blank fo	radoulat	tionel	
	(The space b	oelow is intentional	lly left	blank fo	or calculat	tions.)	
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Measuring Voltage, Current & Resistance

Unit: DC Circuits

Details

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): 11.5.C, 11.5.C.1, 11.5.C.1.i, 11.5.C.2.ii, 11.5.C.2.ii, 11.5.C.2.ii, 11.5.C.3

Mastery Objective(s): (Students will be able to ...)

• Accurately measure voltage and current in a DC circuit.

Success Criteria:

- Multimeter wires are plugged in to the correct jacks and dial is set to the correct quantity.
- Measurements are taken at appropriate points in the circuit. (Voltage is measured in parallel and current is measured in series.)

Language Objectives:

- Explain how to set up the multimeter correctly.
- Explain where to take the measurements and why.

Tier 2 Vocabulary: meter

Labs, Activities & Demonstrations:

- Show & tell with digital multi-meter.
- Measurement of voltages and currents in a live DC circuit.

Notes:

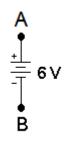
Analyzing an electrical circuit means figuring out the potential difference (voltage), current, and/or resistance in each component of a circuit. In order to analyze actual circuits, it is necessary to be able to measure these quantities.

Measuring Voltage

Voltage is measured with a voltmeter.

Suppose we want to measure the electric potential (voltage) across the terminals of a 6 V battery. The diagram would look like this:

The voltage between points A and B is either +6V or -6V, depending on the direction. The voltage from A to B (positive to negative) is +6V, and the voltage from B to A (negative to positive) is -6V.



Measuring Voltage, Current & Resistance

To measure voltage:

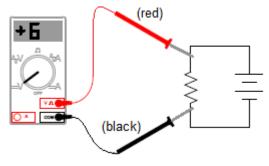
Details

Big Ideas

- 1. The circuit needs to be powered up with current flowing through it.
- 2. Make sure the red lead is plugged into the V Ω socket (for measuring volts or ohms).
- 3. Make sure that the voltmeter is set for volts (DC or AC, as appropriate).
- 4. Touch the two leads *in parallel* with the two points you want to measure the voltage across. (Remember that voltage is the same across all branches of a parallel circuit. You want the voltmeter to be one of the branches, and the circuit to be the other branch with the same voltage.)

On a voltmeter (a meter that measures volts or voltage), positive voltage means the

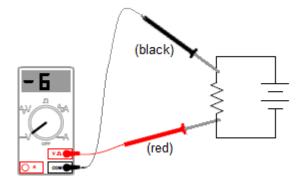
current is going from the red (+) lead to the black (-) lead. In the following circuit, if you put the red (+) lead on the end of a resistor that is closer to the positive terminal of the battery, and the black (-) lead on the end that is closer to the negative terminal, the voltage reading will be positive. In the circuit to the right, the voltmeter reads +6 V.



However, if you reverse the leads so that the black (-) lead is closer to the positive

terminal of the battery and the red (+) lead is closer to the negative terminal, the voltage reading will be negative. In the circuit to the right, the voltmeter reads -6 V.

The reading of -6 V indicates that the current is actually flowing in



the opposite direction from the way the voltmeter is measuring—from the black (-) lead to the red (+) lead.

Voltmeters have a high resistance (typically 200 k Ω for older analog voltmeters, and 10 M Ω or more for modern digital voltmeters), so that the presence of the meter has a minimal effect on the circuit under test. An "ideal voltmeter" would have infinite resistance.

	Measuring voltage, current & Resistance Page. 250
Big Ideas	Details Unit: DC Circuits
	Measuring Current
	Current (amperage) is measured with an ammeter.
	To measure current:
	 The circuit needs to be open between the two points where you want to measure the current.
	 Make sure the red lead is plugged into appropriate socket (10 A if the current is expected to be 0.5 A or greater; 1 A or mA/μA if the current is expected to be less than 0.5 A).
	3. Make sure the ammeter is set for amperes (A), milliamperes (mA) or microamperes (μ A) AC or DC, depending on what you expect the current in the circuit to be.
	4. Touch one lead to each of the two contact points, so that the ammeter is <i>in series</i> with the rest of the circuit. (Remember that current is the same through all components in a series circuit. You want to measure all of the current, so you want all of the current to flow through the meter.)
	On an ammeter (a meter that measures current), the current is measured assuming that it is flowing from the red (+) lead to the black (-) lead. In the following circuit, if you put the red (+) lead on the side that is connected to the positive terminal and the black (-) lead on the end that is connected to the negative terminal, the current reading would be positive. In the circuit to the right, the current is $+3A$.
	As with the voltage example above, if you switched the leads, the reading would be -3 A instead of $+3$ A.
	Ammeters have a low resistance, so that the presence of the meter has a minimal effect on the circuit under test. Because of the way the meter is designed resistance varies depending on the amount of current being measured. (One popular ammeter has a resistance of 0.03.0 when measuring currents in the $6 - 10.0$ range $1.8.0$

has a resistance of 0.03 Ω when measuring currents in the $\,6-10$ A range, 1.8 Ω when measuring current in the 60 – 400 mA range, and 100 Ω for currents in the $600 \ \mu\text{A} - 6 \ \text{mA}$ range.) An "ideal ammeter" would have zero resistance.

Measuring Voltage, Current & Resistance

Big Ideas	Details Unit: DC Circuit					
516 10203	Measuring Resistance	_				
	Resistance is measured with an ohmmeter.					
	Resistance does not have a direction. If you placed an ohmmeter across points A and B, it would read 10Ω regardless of which lead is on which point.	2				
	An ohmmeter supplies a voltage across the component and measures the current. Because the voltage supplied is constant, the Ohm's Law calculation is built into the meter and the readout displays the resistance.					
	To measure resistance:					
	1. The circuit needs to be open. Because the meter is applying a voltage and measuring current, you do not want other voltages or currents in the circuit					
	2. Make sure the red lead is plugged into the V Ω socket (for measuring volts o ohms).	r				
	3. Make sure that the voltmeter is set for Ω .					
	4. Touch one lead to each end of the resistor.					
	If you need to measure the resistance of a component that is in a circuit under power, it can be more reliable to measure the voltage and current and calculate resistance using Ohm's Law ($\Delta V = IR$).					

Big Ideas	Capacitance Details	Page: 252 Unit: DC Circuits					
0	Capacitance						
	 Unit: DC Circuits NGSS Standards/MA Curriculum Frameworks (2016): N/A AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 1 10.6.A.2, 10.6.A.2.i, 10.6.A.2.ii, 10.6.A.3, 10.6.A.3.i, 10.6.A.3. 10.6.A.5, 10.6.A.6 Mastery Objective(s): (Students will be able to) Solve problems involving relationships between capacitance, voltage. Success Criteria: Variables are correctly identified and substituted correctly in equation. Algebra is correct and rounding to appropriate number of sign reasonable. 	ii, 10.6.A.4, , charge and nto the correct					
	 Describe what a capacitor does. Tier 2 Vocabulary: charge, capacitance Labs, Activities & Demonstrations: build a capacitor 						
	Notes: <u>capacitor</u> : an electrical component that stores electrical charge but does not allow current to flow through. The simplest capacitors are made of metal plates that are separated by some fixed distance.	plates					
	The electrical symbol for a capacitor is a representation of the parallel plates.						

Capacitance

	capacitance	rage. 200
Big Ideas	Details	Unit: DC Circuits
	When an electric potential difference (voltage) is applied to a	circuit that contains a
	capacitor, one side of the capacitor will acquire a positive char	ge, and the other side
	will acquire an equal negative charge. This process is called ch	-
		99 capacite
	When a charged capacitor is placed in a circuit (perhaps it was	charged previously,
	and then the voltage source was switched off), charge flows of	
	the circuit. This process is called <i>discharging the capacitor</i> .	
	No current actually flows through the capacitor, but as it charge	zes, the positive
	charges that accumulate on one side of the capacitor repel po	• •
	other side into the rest of the circuit. (The same is true from t	-
	on the other side.) This means that <i>an uncharged capacitor a</i>	
	first begins to charge.	
	As charge builds up in the capacitor, its electric potential incre	ases on the nositive
	side, and decreases on the negative side. This means that the	•
	-	
	between the battery (or other voltage source) and the capacit	
	the charges repelling the additional charges that the battery is	trying to add.
	Eventually, the capacitor becomes fully charged, and the elect	ric notential
	difference in the circuit is unable to add any more charge. Wh	•
		••
	more charges flow into or out of the capacitor. This means the	
	capacitor in a circuit that has a power supply (e.g., a battery) c	icts like an open
	switch or a broken wire.	
	If you disconnect the battery and reconnect the fully-charged	capacitor to a circuit
	that allows the capacitor to discharge, charges will flow out of	•
	through the circuit. This means that <i>a fully charged capacitor</i>	
	separate power supply acts like a battery when it first begins	to discharge.
	Toys from joke shops that shock people use simple battery-and	d capacitor circuits
		-
	The battery charges the capacitor gradually over time until a si	-
	charge has built up. When the person grabs the object, the pe	
	circuit that discharges the capacitor, resulting in a sudden, unp	pleasant electric shock.

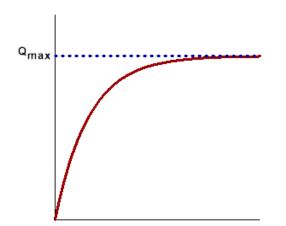
Capacitance

Big Ideas	Details Unit: DC Circuits
	The first capacitors were made independently in 1745 by
	the German cleric Ewald Georg von Kleist, and by the
	Dutch scientist Pieter van Musschenbroek. Both von
	Kleist and van Musschenbroek lined a glass jar with metal
	foil on the outside and filled the jar with water. (Recall
	that water with ions dissolved in it conducts electricity.)
	Both scientists charged the devices with electricity, and
	both received a severe shock when they accidentally
	discharged the jars through themselves.
	This type of capacitor is named after is called a Leyden
	jar, after the city of Leiden (Leyden) where van
	Musschenbroek lived.
	Modern Leyden jars are lined on the inside and outside with conductive metal foil.
	As a potential difference is applied between the inside and outside of the jar, charge
	builds up between them. The glass, which acts as an insulator (a substance that
	does not conduct electricity), keeps the two pieces of foil separated and does not
	allow the charge to flow through.
	Because the thickness of the jar is more or less constant, the Leyden jar behaves like
	a parallel plate capacitor.
	Shortly after the invention of the Leyden jar, Daniel Gralath discovered that he could connect several jars in parallel to increase the total possible stored charge. The American scientist and statesman Benjamin Franklin compared this idea with a "battery" of cannon. (The original meaning of the term "battery" was a collection of cannons for the purpose of battering the enemy.) The term is now used to describe a similar arrangement of electrochemical cells.
	Franklin's most famous experiment was to capture the charge from a lightning strike
	in Leyden jars, proving that lightning is an electric discharge.
	<u>capacitance</u> : a measure of the ability of a capacitor to store charge. Capacitance is
	measured in farads (F), named after the English physicist Michael Faraday.
	Capacitance is the ratio of the charge stored by a capacitor to the voltage applied:
	$C = \frac{Q}{\Delta V}$ which is often represented as $Q = C \Delta V$
	Thus, one farad is one coulomb per volt. Note, however, that one farad is a
	ridiculously large amount of capacitance. The capacitors in most electrical circuits
	are in the millifarad (mF) to picofarad (pF) range.

Capacitance

Capacitance is the theoretical limit of the charge that a capacitor could store at a given potential difference (voltage) if the charge were allowed to build up over an infinite amount of time.

As described above, as a capacitor is charged, the positive side increasingly repels additional positive charges coming from the voltage source, and the negative side increasingly repels additional negative charges. This means that the capacitor charges rapidly at first, but the amount of charge stored decreases exponentially as the charge builds up.



Note that Q_{max} is sometimes labeled Q_0 . Be careful—in this case, the subscript 0 does **not** necessarily mean at time = 0.

Energy Stored in a Capacitor

Recall that energy is the ability to do work, and that $W = \Delta U$. Because W = qV, if we keep the voltage constant and add charge to the capacitor:

$$W = \Delta U = \Delta V \Delta q$$

Applying calculus^{*} gives:

$$dU = \Delta V \, dq$$
 and therefore $U = \int_0^Q \Delta V \, dq = \int_0^Q \frac{q}{C} \, dq = \frac{1}{2} \frac{Q^2}{C}$

Because $Q = C\Delta V$, we can substitute $C\Delta V$ for Q, giving the equation for the stored (potential) energy in a capacitor:

$$U_C = \frac{Q^2}{2C} = \frac{1}{2}QV = \frac{1}{2}CV^2$$

* Because this is not a calculus-based course, you are not responsible for understanding this derivation. However, you do need to be able to use the resulting equations.

Big Ideas

Details

Parallel-Plate Capacitors and Dielectrics

The capacitance of a parallel plate capacitor is given by the following equation:

 $C = \kappa \varepsilon_0 \frac{A}{d}$

where:

C = capacitance

 $\kappa = \varepsilon_r$ = relative permittivity (dielectric constant), vacuum = 1

 $\varepsilon_o =$ electrical permittivity of free space = 8.85 × 10⁻¹² $\frac{F}{m}$

A = cross-sectional area

d = distance between the plates of the capacitor

When a capacitor is fully charged, the distance between the plates can be so small that a spark could jump from one plate to the other, shorting out and discharging the capacitor. In order to prevent this from happening, the space between the plates is often filled with a chemical (often a solid material or an oil) called a dielectric.

A dielectric is an electrical insulator (charges do not move, which reduces the possibility of the capacitor shorting out), but has a relatively high value of electric permittivity (ability to support an electric field). (See *Electric Permittivity*, starting on page 159.)

Dielectrics in capacitors serve the following purposes:

- Keep the conducting plates from coming into contact, allowing for smaller plate separations and therefore higher capacitances.
- Increase the effective capacitance by spreading out the charge, reducing the electric field strength and allowing the capacitor to hold same charge at a lower voltage.
- Reduce the possibility of the capacitor shorting out by sparking (more formally known as dielectric breakdown) during operation at high voltage.

Note that a higher value of κ^* and lower value of *d* both enable the capacitor to have a higher capacitance.

Commonly used solid dielectrics include porcelain, glass or plastic (such as polyethylene). Common liquid dielectrics include mineral oil or castor oil. Common gaseous dielectrics include air, nitrogen and sulfur hexafluoride.

^{*} Note that κ is the Greek letter "kappa," not the Roman letter "k".

From *Electric Fields and Electric Potential*, starting on page 167, $\Delta V = \vec{E} \cdot \vec{d}$.

Because
$$C = \frac{Q}{\Delta V}$$
, which means $\Delta V = \frac{Q}{C}$, we can substitute $C = \kappa \varepsilon_o \frac{A}{d}$ to give:
$$\Delta V = \frac{Q}{C} = \frac{Qd}{\kappa \varepsilon_o A} = \vec{E} \cdot \vec{d} = Ed \cos \theta$$

Assuming the electric field and displacement are in the same direction, $\cos\theta = 1$, which means the electric field between the plates of a capacitor is:

 $E_c = \frac{Q}{\kappa \varepsilon_o A}$

Details

Unit: DC Circuits

Details

Big Ideas

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 11.8.A, 11.8.A.1, 11.8.A.1.i, 11.8.A.1.ii, 11.8.A.1.iii, 11.8.A.2

Mastery Objective(s): (Students will be able to ...)

• Calculate voltage, capacitance, charge and potential energy in series and parallel circuits.

Success Criteria:

- Correct relationships are applied for each quantity.
- Variables are correctly identified and substituted correctly into the correct equations and algebra is correct.

Language Objectives:

• Explain how capacitors behave similarly to and different from resistors in series and parallel circuits.

Tier 2 Vocabulary: charge, capacitance

Notes:

Capacitors in Parallel

When capacitors are connected in parallel:

The voltage in a parallel circuit must be constant regardless of the path.

The total charge on multiple capacitors in parallel is $Q_{total} = Q_1 + Q_2 + \dots$, because charge can accumulate separately in the capacitors in each branch of the circuit.

The charge on capacitor C_1 must be $Q_1 = C_1 \Delta V$, and the charge on capacitor C_2 must be $Q_2 = C_2 \Delta V$.

This means:

This means:

$$Q_{total} = Q_1 + Q_2 = C_1 \Delta V + C_2 \Delta V = (C_1 + C_2) \Delta V.$$
Because $C_{eq} = \frac{Q_{total}}{Q_{total}}$, we have:
 $C_{eq} = \frac{Q_{total}}{Q_{total}} = \frac{Q_1 + Q_2}{Q_1 + Q_2} = \frac{(C_1 + C_2) \Delta V}{Q_1 + Q_2} = C_1 + C_2$

capacitance is the sum of the capacitances of the individual capacitors:

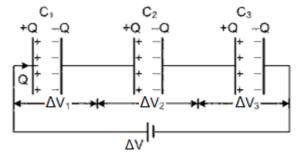
$$C_{eq} = C_1 + C_2 + C_3 + \cdots$$

Big Ideas

Details

Capacitors in Series

In a series circuit, the voltage from one end to the other is divided among the components.



Note that the segment of the circuit that goes from the right side of C_1 to the left side of C_2 is isolated from the rest of the circuit. Current does not flow through a capacitor, which means charges cannot enter or leave this segment. Because charge is conserved (electrical charges cannot be created or destroyed), this means the negative charge on C_1 (which is $-Q_1$) must equal the positive charge on C_2 (which is $+Q_2$).

By applying this same argument across each of the capacitors, all of the charges across capacitors in series must be equal to each other and equal to the total charge in that branch of the circuit. (Note that this is true regardless of whether C_1 , C_2 and C_3 have the same capacitance.)

Therefore, the charge distribution in capacitors in series is: $Q = Q_1 = Q_2 = Q_3$

Because the components are in series, we also know that $\Delta V = \Delta V_1 + \Delta V_2 + \Delta V_3$

Because $\Delta V = \frac{Q}{C}$:

$$\Delta V = \frac{Q_1}{C_1} + \frac{Q_2}{C_2} + \frac{Q_3}{C_3}$$

Because $Q = Q_1 = Q_2 = Q_3$:

$$\Delta V = \frac{Q}{C_1} + \frac{Q}{C_2} + \frac{Q}{C_3} = Q \left(\frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} \right)$$
$$\frac{\Delta V}{Q} = \frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$$

Generalizing this relationship, when capacitors are arranged in series, the reciprocal of the total capacitance is the sum of the reciprocals of the capacitances of the individual capacitors:

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \cdots$$

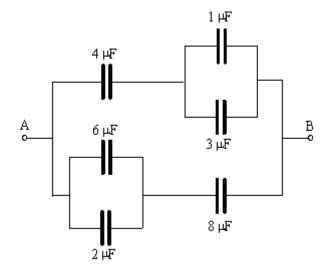
Big Ideas Details

Mixed Series and Parallel Circuits

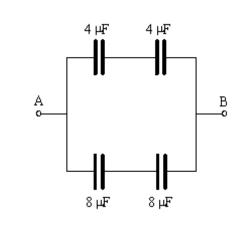
As with resistor networks, mixed circuits involving capacitors in series and in parallel can be simplified by replacing each set of capacitors with an equivalent capacitance, starting with the innermost set of capacitors and working outwards (much like simplifying an equation by starting with the innermost parentheses and working outwards).

Sample Problem:

Simplify the following circuit:



First, we would add the capacitances in parallel. On top, $3 \mu F + 1 \mu F = 4 \mu F$. On the bottom, $6 \mu F + 2 \mu F = 8 \mu F$. This gives the following equivalent circuit:



Big Ideas Details Next, we combine the capacitors in series on top: $\frac{1}{C_{eg}} = \frac{1}{C_1} + \frac{1}{C_2} = \frac{1}{4} + \frac{1}{4} = \frac{2}{4} = \frac{1}{2}$ $\frac{1}{C_{eq}} = \frac{1}{2}; \quad \therefore \ C_{eq} = 2 \ \mu F$ and the capacitors in series on the bottom: $\frac{1}{C_{eg}} = \frac{1}{C_1} + \frac{1}{C_2} = \frac{1}{8} + \frac{1}{8} = \frac{2}{8} = \frac{1}{4}$ $\frac{1}{C_{eq}} = \frac{1}{4}; \quad \therefore \ C_{eq} = 4 \ \mu F$ This gives the following equivalent circuit: 2 нҒ _____B A 0----o--4 μF Finally, we combine the last two capacitances in parallel, which gives: $C_{eq} = C_1 + C_2 = 2 + 4 = 6 \,\mu\text{F}$

ig Ideas	Details	Lapacitors in S		unu i	aranci v	chedits	Unit:	Page: 26 DC Circuit
-	-	le Problem						
	Q: Fil	l in the table for the	followi	ng circuit	t:			
		9 V _		: 3 µF		C3 = 4 µF		
			C4 =	2 µF	C2 = 1 ;	ιF		
		Quantity (unit)	Var.	2 μF	C2=1;	C3	C4	Total
		Quantity (unit) Voltage (V)					C4	Total 9
			Var.				C4	
		Voltage (V)	Var. ΔV	C1	C2	СЗ		

et's start by combining the two capacitors parallel (C2 & C3) to make a equivalent capacitor.

$$C_* = C_2 + C_3 = 1 \,\mu\text{F} + 4 \,\mu\text{F} = 5 \,\mu\text{F}$$

Now we have three capacitors in series: C_1 , C_* , and C_4 :

$$\frac{1}{C_{total}} = \frac{1}{C_1} + \frac{1}{C_*} + \frac{1}{C_4} = \frac{1}{3} + \frac{1}{5} + \frac{1}{2} = 0.\overline{3} + 0.2 + 0.5 = 1.0\overline{3}$$
$$C_{total} = \frac{1}{1.0\overline{3}} = 0.9677 \,\mu\text{F}$$

Now we can calculate Q for the total circuit from $Q = C\Delta V$:

$$Q = C\Delta V = (9)(0.9677) = 8.710 \,\mu C$$

Now we have:

Quantity (unit)	Var.	C1	C2	С3	C4	Total
Voltage (V)	ΔV					9
Capacitance (µF)	С	3	1	4	2	0.9677
Charge (µC)	Q					8.710
Energy (µJ)	U					

Big Ideas

Details

Next, because the charge is equal across all capacitors in series, we know that $Q_1 = Q_* = Q_4 = Q_{total}$, which gives:

Quantity (unit)	Var.	C1	C2	С3	C4	Total
Voltage (V)	ΔV					9
Capacitance (µF)	С	3	1	4	2	0.9677
Charge (µC)	Q	8.710			8.710	8.710
Energy (µJ)	U					

Now we can calculate V_1 and V_4 from $Q = C \Delta V$.

We can also calculate the energy from $U_C = \frac{1}{2}Q\Delta V = \frac{1}{2}C(\Delta V)^2$

Quantity (unit)	Var.	C1	C2	С3	C4	Total
Voltage (V)	ΔV	2.903			4.355	9
Capacitance (µF)	С	3	1	4	2	0.9677
Charge (µC)	Q	8.710			8.710	8.710
Energy (µJ)	U	12.64			18.96	39.19

We know that voltages in series add, so $\Delta V_{total} = \Delta V_1 + \Delta V_* + \Delta V_4$, which means $9 = 2.903 + \Delta V_* + 4.355$, which gives $\Delta V_* = 1.742$ V.

Because C_2 and C_3 (and therefore ΔV_2 and ΔV_3) are in parallel, $\Delta V_* = \Delta V_2 = \Delta V_3 = 1.742 \text{ V}$:

Quantity (unit)	Var.	C1	C2	C3	C4	Total
Voltage (V)	ΔV	2.903	1.742	1.742	4.355	9
Capacitance (µF)	С	3	1	4	2	0.9677
Charge (µC)	Q	8.710			8.710	8.710
Energy (µJ)	U	12.64			18.96	39.19

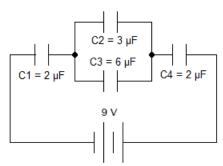
Finally, we can calculate Q from $Q = C\Delta V$ and U from $U_C = \frac{1}{2}Q\Delta V = \frac{1}{2}C(\Delta V)^2$:

Quantity (unit)	Var.	C1	C2	C3	C4	Total
Voltage (V)	ΔV	2.903	1.742	1.742	4.355	9
Capacitance (µF)	С	3	1	4	2	0.9677
Charge (µC)	Q	8.710	1.742	6.968	8.710	8.710
Energy (µJ)	U	12.64	1.52	6.07	18.96	39.19

Big Ideas Details

Homework Problems

1. **(S)** Fill in the table for the following circuit:



Quantity (unit)	Var.	C1	C2	C3	C4	Total
Voltage (V)	ΔV					9
Capacitance (µF)	С	2	3	6	2	
Charge (µC)	Q					
Energy (µJ)	U					

Note: the above units can be used directly with $Q = C\Delta V$ and

 $U = \frac{1}{2}Q\Delta V = \frac{1}{2}C(\Delta V)^2$ without converting. (Because microcoulombs = microfarads × volts and

microjoules = microcoulombs × volts.)

Big Ideas	Details		1100	and i	araner	encurts	Unit:	DC Circuits
	2.	(M) Fill in the table	for th	e followi	ng circuit:			
				C1 = 12 µF	C2 = 4 µF	C4 = 24 µF		
		Quantity (unit)	Var.	C1	C2	C3	C4	Total
		Voltage (V)	ΔV					64
		Capacitance (µF)	С	12	4	5	24	
		Charge (µC)	Q					
		Energy (µJ)	U					

Unit: DC Circuits

Details

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): 11.8.B, 11.8.B.1, 11.8.B.1.i, 11.8.B.1.ii, 11.8.B.1.iii, 11.8.B.2, 11.8.B.2.i, 11.8.B.2.ii, 11.8.B.2.iii, 11.8.B.2.iv, 11.8.B.2.v, 11.8.B.2.vi, 11.8.B.2.vii

Mastery Objective(s): (Students will be able to...)

• Solve problems involving time-varying circuits with charging and discharging capacitors.

Success Criteria:

- Correct relationships are applied for each quantity.
- Variables are correctly identified and substituted correctly into the correct equations and algebra is correct.

Language Objectives:

• Explain why a discharged capacitor behaves like a wire, and why a fullycharged capacitor behaves like an open switch.

Tier 2 Vocabulary: charge, capacitance, resistance

Labs, Activities & Demonstrations:

• RC circuit lab

Notes:

<u>RC circuit</u>: a circuit involving combinations of resistors and capacitors.

In an RC circuit, the amount and direction of current change with time as the capacitor charges or discharges. The amount of time it takes for the capacitor to charge or discharge is determined by the combination of the capacitance and resistance in the circuit. This makes RC circuits useful for intermittent (*i.e.*, with a built-in delay) back-and-forth switching. Some common uses of RC circuits include:

- clocks
- windshield wipers
- pacemakers
- synthesizers

When we studied resistor-only circuits, the circuits were steady-state, *i.e.*, voltage and current remained constant. RC circuits are time-variant, *i.e.*, the voltage, current, and charge stored in the capacitor(s) are all changing with time.

Charging a Capacitor

Recall that a capacitor is an electrical component that stores charge. No current actually flows through the capacitor. Recall also that capacitance (C) is a capacitor's ability to be charged by a given electric potential difference (voltage). Therefore, the maximum charge that a capacitor can hold is:

 $Q_{max} = C\Delta V$

In the previous section, the charge that we calculated was actually this maximum charge Q_{max} , which is the amount of charge that the capacitor would hold if it had been charged for "a long time" such that it was fully charged.

However, recall also that:

Big Ideas

Details

• In a capacitor with zero charge, every charge placed on one side causes an equivalent charge on the opposite side. This means:

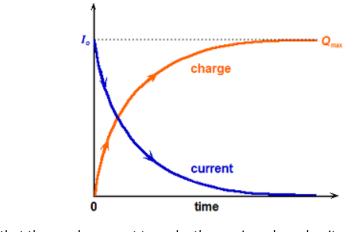
With respect to current, a capacitor with zero charge initially behaves like a wire.

• When a capacitor is fully charged, no additional charge can be added (unless the voltage is increased). This means:

With respect to current, a fully charged capacitor behaves like an open circuit.

This means that the behavior of the capacitor changes as the charges build up inside of it.

When a capacitor that initially has zero charge is connected to a voltage source, the current that flows through the circuit decreases exponentially, and the charge stored in the capacitor asymptotically approaches Q_{max} , the maximum charge that can be stored in that capacitor for the voltage applied.



(Note that the graphs are not to scale; the y-axis scale and units are necessarily different for charge and current.)

Big Ideas	Details Unit: DC Circuits
•	The equations for the charge in a capacitor and the current that flows "through" it
honors	as a function of time while a capacitor is charging are:
(not AP®)	$I = I_o e^{-t_{RC}} = \frac{\Delta V}{R} e^{-t_{RC}}$ $Q = Q_{\max} (1 - e^{-t_{RC}}) = C \Delta V (1 - e^{-t_{RC}})$
	$Q = Q_{\max}(1 - e^{-t/RC}) = C\Delta V(1 - e^{-t/RC})$
	where:
ļ	I = current(A)
	I_o = initial current (just after switch was closed) (A)
İ	$\Delta V = \text{voltage}(V)$
ļ	Q = charge(C)
	Q _{max} = (theoretical) maximum charge stored by capacitor at the circuit's voltage (C)
	e = base of exponential function = 2.71828
	t = time since switch was closed (s)
İ	$R = \text{resistance}(\Omega)$
	C = capacitance (F)
İ	We can rearrange the above equations to give:
	$\frac{I}{I_o} = 1 - \frac{Q}{Q_{\max}} = e^{-\frac{t}{R_c}}$
	Note that the value <i>RC</i> is the time constant of the circuit, often denoted by the variable τ . Thus, we can write the above equation as:
İ	
	$\frac{I}{I_o} = 1 - \frac{Q}{Q_{\text{max}}} = e^{-t/\tau}$
ļ	
İ	
İ	
İ	
ļ	
•	

Big Ideas Details

The *RC* term in the exponent is known as the time constant (τ) for the circuit. Larger values of *RC* mean the circuit takes longer to charge the capacitor. The following table shows the rate of decrease in current in the charging circuit and the rate of increase in charge on the capacitor as a function of time:

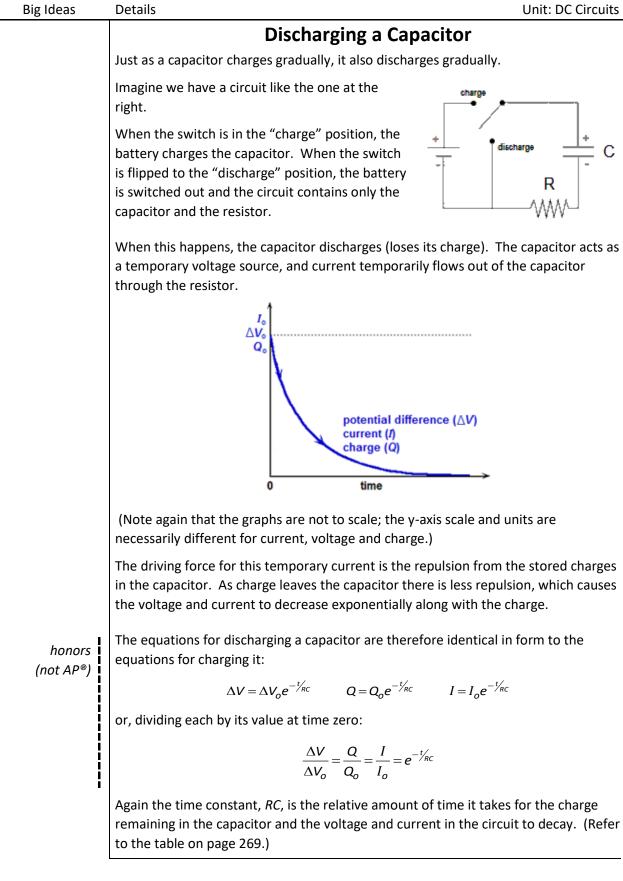
t	$\frac{I}{I_o} = \frac{\Delta V}{\Delta V_o} = e^{-t/R_c}$	$\frac{Q}{Q_{\rm max}} = 1 - e^{-t/_{\rm RC}}$
0	1	0
¼RC	0.78	0.22
½ RC	0.61	0.39
0.69 <i>RC</i>	0.5	0.5
RC	0.37	0.63
2 <i>RC</i>	0.14	0.86
4 <i>RC</i>	0.02	0.98
10 <i>RC</i>	4.5×10^{-5}	≈1

Note that the half-life of the charging (and discharging) process is approximately 0.69 *RC*.

Note also that while Q_{max} depends on the voltage applied, the rate of charging and discharging depend only on the resistance and capacitance in the circuit.

The AP[®] Physics 2 exam requires only a qualitative understanding of RC circuits. It is sufficient to understand that:

- The time constant $\tau = RC$ represents how quickly a capacitor will charge or discharge.
- After a "long time" (approximately 10τ), a capacitor that is charging can be assumed to be fully charged, and a capacitor that is discharging can be assumed to be fully discharged.
- After an amount of time equal to the time constant (t = τ = RC), a fully discharged capacitor will charge to approximately 63 % of its full capacity.
- After an amount of time equal to the time constant (*t* = *τ* = *RC*), a fully charged capacitor will discharge to approximately 37 % of its initial charge.



Big Ideas	Details	Unit: DC Circuits
	Sample Problem	
	 Q: A circuit has a 9V battery, an open switch, a 1kΩ resistor, and series. The capacitor has no residual charge. 	d a capacitor in
	9V = 1kΩ	
	When the switch is closed, the charge in the capacitor climbs maximum value in 50 ms. What is the capacitance of the cap	
	A: The charge increases at the rate of:	
	$Q(t) = Q_{\max}(1 - e^{-t/RC})$	
	We are given that $\frac{Q}{Q_{\text{max}}} = 0.86$, $t = 0.05$ s, and $R = 1000 \Omega$.	
	$\frac{Q}{Q_{\text{max}}} = 1 - e^{-\frac{t}{Rc}}$ $0.86 = 1 - e^{-\frac{0.05}{1000c}}$ $-0.14 = -e^{-\frac{0.05}{1000c}}$ $\ln(0.14) = \ln(e^{-\frac{0.05}{1000c}}) = \frac{-0.05}{1000c}$ $-1.97 = \frac{-0.05}{1000c}$ $1970 C = 0.05$ $C = \frac{0.05}{1970} = 2.5 \times 10^{-5} \text{ F} = 25 \mu\text{F}$ Note that we could have solved this problem by using the tak see that the capacitor is 86 % charged $\left(\frac{Q}{Q_{\text{max}}} = 0.86\right)$ when the capacitor is 86 % charged $\left(\frac{Q}{Q_{\text{max}}} = 0.86\right)$	

Big Ideas	Details Unit: DC Circuits
	Homework Problems
	Note: You will need to convert units in most of these problems.
	1. (S) A series RC circuit consists of a 9 V battery, a 3 Ω resistor, a 6 μ F capacitor and a switch. How long would it take after the switch is closed for the capacitor to reach 63 % of its maximum potential difference?
	Answer: 18 μs
	 (M) A circuit contains a 9 V battery, an open switch, a 1 kΩ resistor, and a capacitor, all in series. The capacitor initially has no charge. When the switch is closed, the charge on the capacitor climbs to 86 % of its maximum value in 50 ms. What is the capacitance of the capacitor?
	Answer: 25 μF

Big Ideas	Details	Unit: DC Circuits
honors (not AP®)	3.	(S) A heart defibrillator has a capacitance of $25 \ \mu$ F and is charged to a potential difference of $350 \ V$. The electrodes of the defibrillator are attached to the chest of a patient who has suffered a heart attack. The initial current that flows out of the capacitor is 10 mA.
		a. How much time does it take for the current to fall to 0.5 mA?
		Answer: 2.62 s
		b. How much charge is left on the defibrillator plates after 1.2 s?
		Answer: 2.22 mC

Big Ideas	Details	Unit: DC Circuits
honors	4. (M) In the following RC circuit:	
(not AP®)	$ \begin{array}{c} 7 \Omega \\ 7 \Omega \\ 12 V \\ 12 mF \\ 5 \Omega \end{array} $	
	the switch (S) has been closed for a long time.	
	a. When the switch is opened, how much time does in charge on the capacitor to drop to 13.5% of its orig	
	Answer: 0.288 s	
	b. What is the maximum current through the 5 Ω resi the switch is opened?	stor the instant
	Answer: 0.63 A	

Details

Introduction: Magnetism & Electromagnetism

Unit: Magnetism & Electromagnetism

Topics covered in this chapter:

Magnetism & Magnetic Permeability	
Magnetic Fields	
Magnetism & Moving Charges	
Electromagnetic Induction & Faraday's Law	296
Devices that Use Electromagnetism	299

This chapter discusses electricity and magnetism, how they behave, and how they relate to each other.

- *Magnetism* describes properties of magnets and what causes objects to be magnetic.
- *Magnetic Fields & Magnetic Flux* explains magnetic fields and magnetic flux and how it is calculated.
- *Electromagnetism* describes the relationship between electric fields and magnetic fields, and how changes in one induce changes in the other.
- *Devices that Use Electromagnetism* lists devices that combine electricity and magnetism and explains how they work.

One of the challenges encountered in this chapter is understanding which set of equations applies to a given situation.

Standards addressed in this chapter:

NGSS Standards/MA Curriculum Frameworks (2016):

- **HS-PS2-5.** Provide evidence that an electric current can produce a magnetic field and that a changing magnetic field can produce an electric current.
- **HS-PS3-5.** Develop and use a model of magnetic or electric fields to illustrate the forces and changes in energy between two magnetically or electrically charged objects changing relative position in a magnetic or electric field, respectively.

Introduction: Magnetism & Electromagnetism Page: 276

Big Ideas	Details Unit: Magnetism & Electromagnetism & Page: 276
	AP® Physics 2 Learning Objectives/Essential Knowledge (2024):
AP® only	12.1.A : Describe the properties of a magnetic field.
	12.1.A.1 : A magnetic field is a vector field that can be used to determine the
	magnetic force exerted on moving electric charges, electric currents, or magnetic materials.
	12.1.A.1.i : Magnetic fields can be produced by magnetic dipoles or combinations of dipoles, but never by monopoles.
	12.1.A.1.ii : Magnetic dipoles have north and south polarity.
	12.1.A.2 : A magnetic field is a vector quantity and can be represented using vector field maps.
	12.1.A.2.i : Magnetic field lines form closed loops.
	12.1.A.2.ii: Magnetic fields in a bar magnet form closed loops, with the external magnetic field pointing away from one end (defined as the north pole) and returning to the other end (defined as the south pole).
	12.1.B : Describe the magnetic behavior of a material as a result of the configuration of magnetic dipoles in the material.
	12.1.B.1: Magnetic dipoles result from the circular or rotational motion of electric charges. In magnetic materials, this can be the motion of electrons.
	12.1.B.1.i: Permanent magnetism and induced magnetism are system properties that both result from the alignment of magnetic dipoles within a system.
	12.1.B.1.ii: No magnetic north pole is ever found in isolation from a south pole. For example, if a bar magnet is broken in half, both halves are magnetic dipoles.
	12.1.B.1.iii : Magnetic poles of the same polarity will repel; magnetic poles of opposite polarity will attract.
	12.1.B.1.iv : The magnitude of the magnetic field from a magnetic dipole decreases with increasing distance from the dipole.
	12.1.B.2 : A magnetic dipole, such as a magnetic compass, placed in a magnetic field will tend to align with the magnetic field.
	12.1.B.3 : A material's composition influences its magnetic behavior in the presence of an external magnetic field.
	12.1.B.3.i : Ferromagnetic materials such as iron, nickel, and cobalt can be permanently magnetized by an external field that causes the alignment of magnetic domains or atomic magnetic dipoles.

Introduction: Magnetism & Electromagnetism Page: 277

lig Ideas	Details Unit: Magnetism & Electromagnetism
AP [®] only	12.1.B.3.ii: Paramagnetic materials such as aluminum, titanium, and magnesium interact weakly with an external magnetic field, in that the magnetic dipoles of the material do not remain aligned after the external field is removed.
	12.1.B.3.iii: All materials have the property of diamagnetism, in that their electronic structure creates a usually weak alignment of the dipole moments of the material opposite the external magnetic field.
	12.1.B.4 : Earth's magnetic field may be approximated as a magnetic dipole.
	12.1.C : Describe the magnetic permeability of a material.
	12.1.C.1 : Magnetic permeability is a measurement of the amount of magnetization in a material in response to an external magnetic field.
	12.1.C.2 : Free space has a constant value of magnetic permeability, known as the vacuum permeability μ_0 , that appears in equations representing physical relationships.
	12.1.C.3: The permeability of matter has values different from that of free space and arises from the matter's composition and arrangement. It is not a constant for a material and varies based on many factors, including temperature, orientation, and strength of the external field.
	12.2.A : Describe the magnetic field produced by moving charged objects.
	12.2.A.1 : A single moving charged object produces a magnetic field.
	12.2.A.1.i: The magnetic field at a particular point produced by a moving charged object depends on the object's velocity and the distance between the point and the object.
	12.2.A.1.ii: At a point in space, the direction of the magnetic field produced by a moving charged object is perpendicular to both the velocity of the object and the position vector from the object to that point in space and can be determined using the right-hand rule.
	12.2.A.1.iii: The magnitude of the magnetic field is a maximum when the velocity vector and the position vector from the object to that point in space are perpendicular.
	12.2.B : Describe the force exerted on moving charged objects by a magnetic
	field.

Introduction: Magnetism & Electromagnetism F Details Unit: Magnetism & Electrom

12.2.B.2: A magnetic field may exert a force on a charged object moving in that field.
12.2.B.2.i: The magnitude of the force exerted by a magnetic field on a moving charged object is proportional to the magnitude of the charge, the magnitude of the charged object's velocity, and the magnitude of the magnetic field and also depends on the angle between the velocity and magnetic field vectors.
12.2.B.2.ii: The direction of the force exerted by a magnetic field on a moving charged object is perpendicular to both the direction of the magnetic field and the velocity of the charge, as defined by the right- hand rule.
12.2.B.3 : In a region containing both a magnetic field and an electric field, a moving charged object will experience independent forces from each field.
12.2.B.4: The Hall effect describes the potential difference created in a conductor by an external magnetic field that has a component perpendicular to the direction of charges moving in the conductor.
12.3.A : Describe the magnetic field produced by a current-carrying wire.
12.3.A.1 : A current-carrying wire produces a magnetic field.
12.3.A.1.i: The magnetic field vectors around a long, straight, current- carrying wire are tangent to concentric circles centered on that wire. The field has no component toward, away from, or parallel to the long, straight, current-carrying wire.
12.3.A.1.ii : At a point in space, the magnitude of the magnetic field due to a long, straight, current-carrying wire is proportional to the magnitude of the current in the wire and inversely proportional to the perpendicular distance from the central axis of the wire to the point.
12.3.A.1.iii : The direction of the magnetic field created by a current- carrying wire is determined with the right-hand rule.
12.3.A.1.iv: The direction of the magnetic field at the center of a current- carrying loop is directed along the axis of the loop and can be found using the right-hand rule.
12.3.A.1.v : The magnetic field at a location near two or more current- carrying wires can be determined using vector addition principles.

Big Ideas

Introduction: Magnetism & Electromagnetism

	Introduction. Magnetism & Lieuromagnetism Page: 279
Big Ideas	Details Unit: Magnetism & Electromagnetism
AP [®] only	12.3.B : Describe the force exerted on a current-carrying wire by a magnetic field.
	12.3.B.1 : A magnetic field may exert a force on a current carrying wire.
	12.3.B.1.i : The magnitude of the force exerted by a magnetic field on a
	current-carrying wire is proportional to the current, the length of the portion of the wire within the magnetic field, and the magnitude of the magnetic field, and also depends on the angle between the direction of the current in the wire and the direction of the magnetic field.
	12.3.B.1.ii : The direction of the force exerted by the magnetic field on a current-carrying wire is determined by the right-hand rule.
	12.4.A : Describe the induced electric potential difference resulting from a change in magnetic flux.
	12.4.A.1 : Magnetic flux is a description of the amount of the component of a magnetic field that is perpendicular to a cross-sectional area.
	12.4.A.2: Magnetic flux through a surface is proportional to the magnitude of the component of the magnetic field perpendicular to the surface and to the cross-sectional area of the surface.
	12.4.A.2.i: The area vector is defined to be perpendicular to the plane of the surface and directed outward from a closed surface.
	12.4.A.2.ii : The sign of the magnetic flux indicates whether the magnetic field is parallel to or antiparallel to the area vector.
	12.4.A.3: Faraday's law describes the relationship between changing magnetic flux and the resulting induced emf in a system.
	12.4.A.4 : Lenz's law is used to determine the direction of an induced emf resulting from a changing magnetic flux.
	12.4.A.4.i : An induced emf generates a current that creates a magnetic field that opposes the change in magnetic flux.
	12.4.A.4.ii : The right-hand rule is used to determine the relationships between current, emf, and magnetic flux.
	12.4.A.5 : A common example of electromagnetic induction is a conducting rod on conducting rails in a region with a uniform magnetic field.
	Skills learned & applied in this chapter:
	 Working with material-specific constants from a table.

Details

Magnetism & Magnetic Permeability

Unit: Magnetism & Electromagnetism

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 12.1.B, 12.1.B.1,

12.1.B.1.i, 12.1.B.1.ii, 12.1.B.1.iii, 12.1.B.1.iv, 12.1.B.2, 12.1.B.3, 12.1.B.3.i,

12.1.B.3.ii, 12.1.B.3.ii, 12.1.B.4, 12.1.C, 12.1.C.1, 12.1.C.2, 12.1.C.3

Mastery Objective(s): (Students will be able to ...)

• List and explain properties of magnets.

Success Criteria:

• Explanations account for observed behavior.

Language Objectives:

• Explain why we call the ends of a magnet "north" and "south".

Tier 2 Vocabulary: magnet

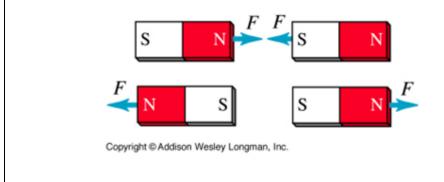
Labs, Activities & Demonstrations:

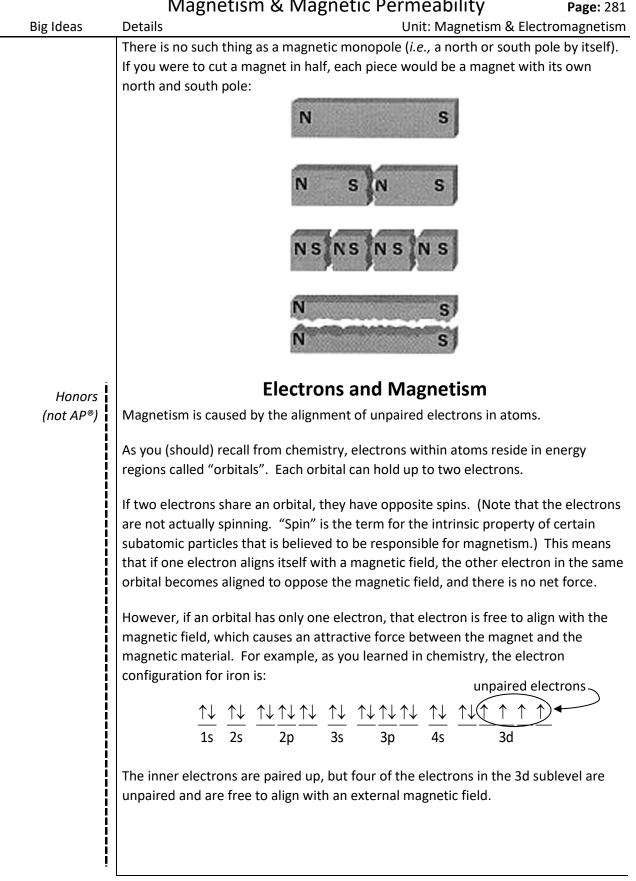
- neodymium magnets
- ring magnets repelling each other on a dowel
- magnets attracting each other across a gap

Notes:

<u>magnet</u>: a material with electrons that can align in a manner that attracts or repels other magnets.

A magnet is a dipole, meaning that it has two opposite ends or "poles", called "north" and "south". If a magnet is allowed to move freely, the end that points toward the north on Earth is called the north end of the magnet. The end that points toward the south on Earth is called the south end of the magnet. (The Earth's magnetic poles are near, but not in exactly the same place as its geographic poles.) All magnets have a north and south pole. As with charges, opposite magnetic poles attract, and like poles repel.





Magnetism & Magnetic Permeability

		viagnetismo	iviagnetic	Ferneability		age: 282
Big Ideas	Details			Unit: Magneti	sm & Electroma	gnetism
		e electrons in a su ce is not magnetic	-	ned randomly, the cted to a magnet.	S.	
		e electrons in a su c and will be attrac	-	ned, the substance t.	e is	
		i <u>etic</u> : a material wh se substances will v		re unable to align v nagnet.	with a magnetic	field.
	field			ns that can move to a magnet but are i	-	agnetic
	resu exhi	lting in a permane	nt magnet. So	it have permanentl me naturally occur obalt, nickel, gadol	ring materials t	hat
Honors (not AP®)	mate	erial becomes para	imagnetic.	mperature above v the French physicia		-
ł	disco	overed this effect.				
	If a paramagnetic material is heated above its Curie temperature, placed in a magnetic field (to force the electrons to align), and then cooled (while still in the magnetic field), the material becomes ferromagnetic. This is how permanent magnets are made.					
		Substance	Curie temperature (°C)	Substance	Curie temperature (°C)	
ļ		iron	770	cobalt	1130	
		iron(III) oxide	675	nickel	354	
		magnetite (iron (II,III) oxide)	585	dysprosium	-185.2	
!						

Magnetism & Magnetic Permeability

	Magnetism & Magnetic Permeability Page: 283
Big Ideas	Details Unit: Magnetism & Electromagnetism
	Magnetic Permeability
	Magnetic measurements and calculations involve fields that act over 3-dimensional space and change continuously with position. This means that most calculations relating to magnetic fields need to be represented using multivariable calculus, which is beyond the scope of this course.
	<u>magnetic permeability</u> (magnetic permittivity): the ability of a material to support the formation of a magnetic field. Magnetic permeability is represented by the variable μ . The magnetic permeability of empty space is defined to be $\mu_0 = 4\pi \times 10^{-7} \frac{N}{A^2}$.
Honors (not AP®)	magnetic susceptibility (χ): a measure of the degree to which a material will become magnetized when it is placed in a magnetic field.
	Diamagnetic materials have negative magnetic susceptibilities.
	Paramagnetic materials have positive magnetic susceptibilities.
	Ferromagnetic materials do not have well-defined magnetic susceptibilities, because these substances create their own magnetic fields, which interact with the external magnetic field.

Unit: Magnetism & Electromagnetism

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS3-5

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 12.1.A, 12.1.A.1,

12.1.A.1.i, 12.1.A.1.ii, 12.1.A.2, 12.1.A.2.i, 12.1.A.2.ii, 12.1.B.2, 12.1.B.4

Mastery Objective(s): (Students will be able to...)

- Describe and draw magnetic fields.
- Calculate magnetic flux.

Success Criteria:

Details

Big Ideas

- Magnetic field lines connect north and south poles of the magnet.
- Arrows on field lines point from north to south.

Language Objectives:

• Explain how a compass works.

Tier 2 Vocabulary: field, north pole, south pole

Labs, Activities & Demonstrations:

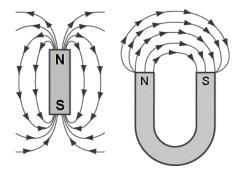
- magnetic field demonstrator plate
- placing various objects into the gap between two magnets
- ferrofluid
- representation of flux as dots on a balloon

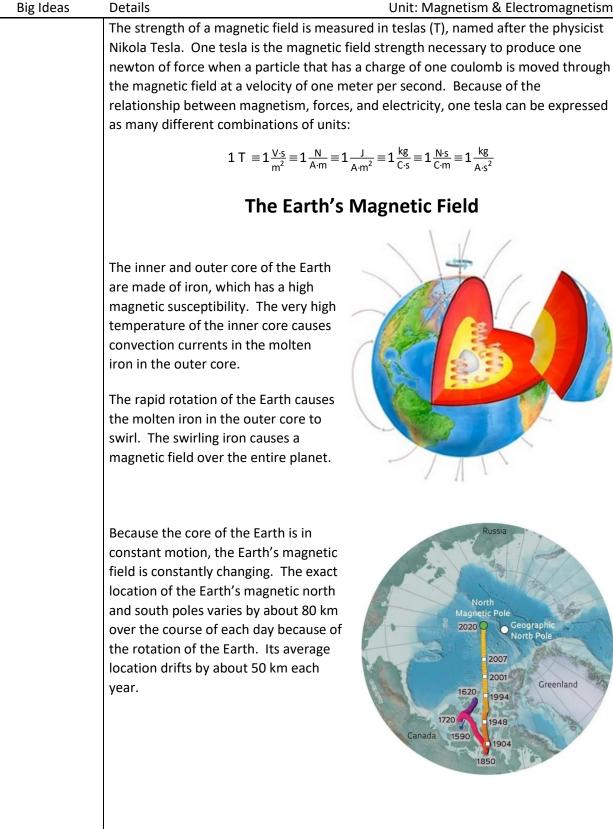
Notes:

<u>magnetic field</u> (\vec{B}) : a force field (region in which a force acts on objects that have a certain property) in which magnetic attraction and repulsion are occurring.

Any object that is a magnetic dipole (*i.e.*, a magnet or something that behaves like one) creates its own magnetic field. If the object is allowed to move freely, the magnetic field will attract and repel the poles of the object so that it aligns with the magnetic field.

Similar to an electric field, we represent a magnetic field by drawing field lines. Magnetic field lines point from the north pole of a magnet toward the south pole, and they show the direction that the north end of a compass or magnet would be deflected if it was placed in the field:





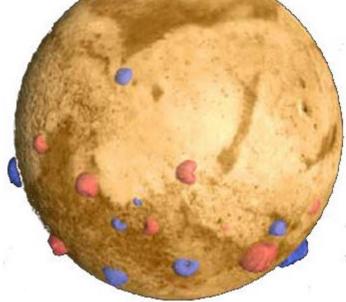
Page: 286 Unit: Magnetism & Electromagnetism

Not all planets have a planetary magnetic field. Mars, for example, is believed to have once had a planetary magnetic field, but the planet cooled off enough to disrupt the processes that caused it. Instead, Mars has some very strong localized magnetic fields that were formed when minerals cooled down in the presence of the planetary magnetic field.

In this picture, the blue and red areas represent regions with strong localized magnetic fields. On Mars, a compass could not be used in the ways that we use a compass on Earth; if you took a compass to Mars, the needle would point either toward or away from each of these regions.

Details

Big Ideas



Jupiter, on the other hand, has a planetary magnetic field twenty times as strong as that of Earth. This field may be caused by water with dissolved electrolytes or by liquid hydrogen.

Recall that the north pole of a magnet is the end that points toward the north on Earth. This must mean that if the Earth is a giant magnet, one of its magnetic poles must be near the geographic north pole, and the other magnetic pole must be near the geographic south pole.

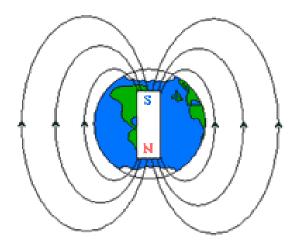
For obvious reasons, the Earth's magnetic pole near the north pole is called the Earth's "north magnetic pole" or "magnetic north pole". Similarly, the Earth's magnetic pole near the south pole is called the Earth's "south magnetic pole" or "magnetic south pole".

However, because the north pole of a magnet points toward the north, the Earth's north magnetic pole (meaning its location) must therefore be the <u>south</u> pole of the giant magnet that is the Earth.

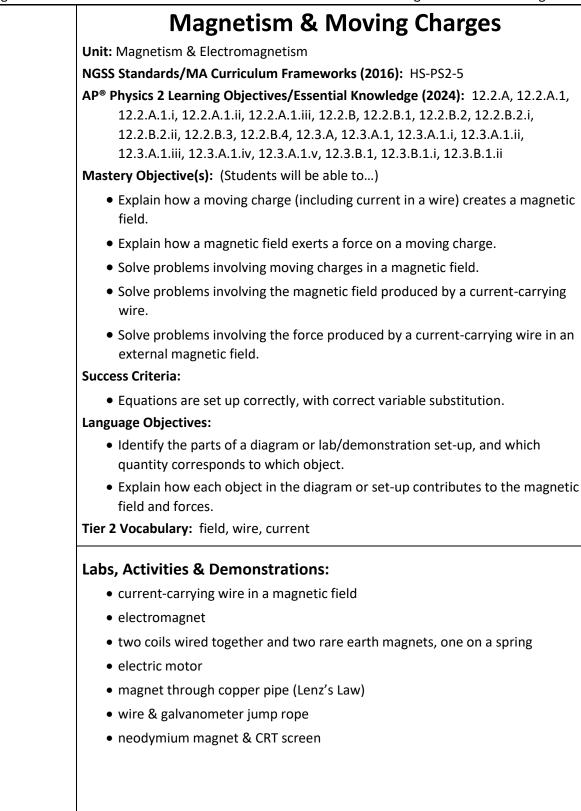
Big Ideas

Details

Similarly, because the south pole of a magnet points toward the south, the Earth's south magnetic pole (meaning its location) must therefore be the <u>north</u> pole of the giant Earth-magnet.



Unfortunately, the term "magnetic north pole," "north magnetic pole" or any other similar term almost always means the magnetic pole that is in the north part of the Earth. There is no universally accepted way to name the poles of the Earth-magnet.



Big Ideas

Details

	Magnetism & Moving Charges Page: 289
Big Ideas	Details Unit: Magnetism & Electromagnetism
	Notes:
	Recall that electrons have both charge and a property called "spin" [*] , which is responsible for magnetism, as discussed in <i>Magnetism & Magnetic Permeability</i> , starting on page 280.
	The interaction of these properties has several consequences:
	• When an electron moves, both its charge and its magnetic spin are moving. The movement of this magnetic spin creates a magnetic field.
	• An electric field is produced by charged objects. (See <i>Electric Fields and Electric Potential</i> , starting on page 167.) When these charges move, the electric field changes.
	• Thus, moving electrons cause changes to both magnetic and electric fields, and changes to either a magnetic or an electric field cause electrons to move.
	Therefore, <i>a changing electric field produces a magnetic field</i> , and <i>a changing magnetic field produces an electric field</i> .
	Note that this and the remaining topics in this unit involve the cross-product of vectors and the right-hand rule. It would be useful to review <i>Vector Multiplication</i> , starting on page 26.
	Forces and Moving Charges
	The changing electric field given by the cross-product of the velocity of the charged particle and the magnetic field:
	$\vec{E} = \vec{v} \times \vec{B}$ and $E = vB\sin\theta$
	Because the force is given by $\vec{F} = q\vec{E}$, the force \vec{F} on a point charge q that is moving through a magnetic field \vec{B} with velocity \vec{v} is therefore:

 $\vec{F}_B = q(\vec{v} \times \vec{B})$ and $F_B = qvB\sin\theta$

The cross-product means that the direction of the force must be perpendicular to both the velocity of the charged object and the magnetic field.

^{*} Remember that electrons are not actually spinning. The property was named based on a simpler understanding of the behavior of electrons than we have now.

Big Ideas	Details Unit: Magnetism & Electromagnetism
	Magnetism, Forces, and Current-Carrying Wires
	Recall that current is a flow of charges, which means that an electric current moving
	through a magnetic field creates a force on the wire carrying the current.
	Recall from <i>Electric Current & Ohm's Law</i> starting on page 195, that $\vec{I} = \frac{\Delta q}{t}$. Recall
	from physics 1 that $\vec{v} = \frac{\vec{d}}{t} = \frac{\ell}{t}$. In this case, we can replace \vec{d} with ℓ , where ℓ is
	the length (distance) of the section of the wire that passes through the magnetic field.
	Combining these equations gives $q\vec{v} = \ell \vec{I}$, which we can use to create the equation:
	$\vec{F} = \ell (\vec{I} \times \vec{B})$ and $F = \ell IB \sin \theta$
	Note that the direction of the cross products $\vec{v} \times \vec{B}$ and $\vec{I} \times \vec{B}$ can be determined using the right-hand rule.
	A current passing through a magnetic field would be represented like the diagram at the right.
	In this diagram, the battery has voltage V, the resistor has resistance R, and the length of wire passing through the magnetic field is ℓ . The direction of the current, \vec{I} , as it passes through the magnetic field is from the bottom of the page to the top.
	The magnetic field has strength B , and is denoted by the symbols \otimes \otimes \otimes \otimes which denote a magnetic field going <u>into</u> the page. (A field coming out of the page would be denoted by \odot \odot \odot \odot \odot \odot instead. Think of the circle as an arrow inside a tube. The dot represents the tip of the arrow facing toward you, and the "X" represents the fletches (feathers) on the tail of the arrow facing away from you.) By the right-hand rule, the direction of the force on the wire would be to the left.

Magnetism & Moving Charges

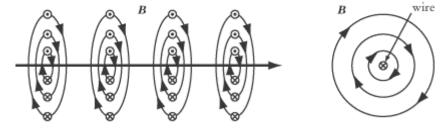
Unit: Magnetism & Electromagnetism For example, suppose we were given the following for the above diagram:

ven the following for the above diagram:
$\vec{B} = 4.0 \times 10^{-5} \text{ T}$
V = 30 V
$R = 5 \Omega$
$\ell = 2 m$
Force on the wire:
$\vec{F} = \ell(\vec{I} imes \vec{B})$
$F = \ell IB \sin \theta$
F = (2)(6)(4.0×10 ⁻⁵)sin(90°)
$F = (2)(6)(4.0 \times 10^{-5})(1)$
$F = 4.8 \times 10^{-4} N$

If the current is going upward through the magnetic field, and the magnetic field is pointing into the paper, then the right-hand rule tells us that the force would be directed to the left.

Magnetic Field Produced by Electric Current

An electric current moving through a wire also produces a magnetic field around the wire:



wire seen from above

wire seen from behind

This time, we use the right-hand rule with our thumb pointing in the direction of the current, and our fingers curl in the direction of the magnetic field.

The strength of the magnetic field produced is given by the Ampere's Law, named for the French physicist, André-Marie Ampère, who discovered this relationship in the 1820s:

$$B = \frac{\mu_o}{2\pi} \cdot \frac{I}{r}$$

where *B* is the strength of the magnetic field, μ_{o} is the magnetic permeability of free space, *I* is the current, and *r* is the distance from the wire. (The variable *r* is used because the distance is in all directions, which means we would use polar or cylindrical coordinates.)

Big Ideas

Details

Details

Big Ideas

Combined Electric and Magnetic Fields

As stated above, the force on a charged particle due to an electric field is:

 $\vec{F}_e = q\vec{E}$

and the force on a charged particle due to a magnetic field is:

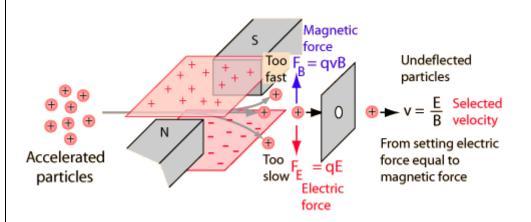
 $\vec{F}_{B} = q(\vec{v} \times \vec{B})$

Therefore, the force on a charged particle that interacts simultaneously with an electric field and a magnetic field must be the sum of the two:

 $\vec{F}_{EM} = q(\vec{E} + \vec{v} \times \vec{B})$

An application of this combination is a particle sorter, which allows only particles with a given velocity to pass through.

Particles that enter a mass spectrometer must have the correct velocity in order for the mass spectrometer to be able to separate the particles properly. Before the particles enter the mass spectrometer, they first pass through a particle sorter, which applies opposing electric and magnetic forces to the particle:



If the particles are moving too quickly, the magnetic force is stronger and the particles are deflected upwards. If the particles are moving too slowly, the electric force is stronger, and the particles are deflected downwards. For particles with the desired velocity, the forces are equal, there is no net force, and the particles are not deflected.

Big Ideas	Magnetism & Moving Cha Details U	nit: Ma		m & El	lectror	Page: nagnet				
2.8.0000	Sample Problem:									
	Q: A proton has a velocity of $1 \times 10^5 \frac{\text{m}}{\text{s}}$ to the	х	х	х	х	х	x			
	right when it is at point <i>P</i> in a uniform magnetic field of 0.1 T that is directed into	x	x	x	x	x	х			
	the page. Calculate the force (magnitude	х	х	x	х	х	х			
	and direction) on the proton and sketch its path.	х	x	Р. х	• x	x	^v х			
		x	x	х	x	x	х			
	A: The force on the proton is given by:									
	$\vec{F}_B = q(\vec{v} \times \vec{B}) = qv$	∕Bsin∂	1							
	Because the velocity of the particle and the d perpendicular, $\sin\theta = \sin(90^\circ) = 1$ and therefore			-						
	$F_B = qvB$									
	$F_B = (1.6 \times 10^{-19})(1)$	×10 ⁵)((0.1)							
	$F_B = 1.6 \times 10^{-15} \text{ N}$									
	$r_B = 1.6 \times 10$ N The direction is given by the right-hand rule.	Start v	with th	e finge	ers of y	/our ri	ght			
		ocity (to ward th which it is up	o the r he mag mean wards.	ight) a gnetic s that . (Note	nd rot field (i the foi e that i	ate yo nto th rce on if the	ur e			
	The direction is given by the right-hand rule. hand pointing straight in the direction of velo right hand until you can bend your fingers to page). Your thumb will be pointing upwards, positively charged particle moving to the righ particle had been negatively charged, it woul direction.) However, note that the action of the force	ocity (to ward th which it is up	o the r he mag mean wards.	ight) a gnetic s that . (Note	nd rot field (i the foi e that i	ate yo nto th rce on if the	ur e a			
	The direction is given by the right-hand rule. hand pointing straight in the direction of velo right hand until you can bend your fingers to page). Your thumb will be pointing upwards, positively charged particle moving to the righ particle had been negatively charged, it woul direction.)	ocity (to ward th which it is up d have X	o the r he mag mean wards. move	ight) a gnetic s that . (Note d in th	nd rot field (i the for e that i e oppo	ate yo nto the rce on if the osite	ur e a			
	The direction is given by the right-hand rule. hand pointing straight in the direction of veloc right hand until you can bend your fingers too page). Your thumb will be pointing upwards, positively charged particle moving to the righ particle had been negatively charged, it woul direction.) However, note that the action of the force causes a change in the direction of the proton's velocity, and the change in the direction of the proton's velocity changes the	ocity (to ward ti which at is up d have X X	o the r he mag mean wards. move X X	ight) a gnetic s that . (Note	nd rot field (i the for e that i ie oppo	ate yo nto the rce on if the osite	ur e a			
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	The direction is given by the right-hand rule. hand pointing straight in the direction of veloc right hand until you can bend your fingers too page). Your thumb will be pointing upwards, positively charged particle moving to the righ particle had been negatively charged, it woul direction.) However, note that the action of the force causes a change in the direction of the proton's velocity, and the change in the direction of the proton's velocity changes the	ocity (to ward ti which at is up d have X X	o the r he mag mean wards. move X X	ight) a gnetic s that . (Note d in th	nd rot field (i the for e that i ie oppo	ate yo nto the rce on if the osite	ur e a ;; ; ; ;			
	The direction is given by the right-hand rule. hand pointing straight in the direction of veloc right hand until you can bend your fingers too page). Your thumb will be pointing upwards, positively charged particle moving to the righ particle had been negatively charged, it woul direction.) However, note that the action of the force causes a change in the direction of the proton's velocity, and the change in the direction of the proton's velocity changes the direction of the force. This feedback loop results in the proton moving in a continuous	ward ti which at is up d have X X X	o the r he mag mean wards. move X X X	ight) a gnetic s that . (Note d in th	nd rot field (i the for e that i e oppo	ate you nto the rce on if the osite	ur e a			
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	.	Magnetism & Moving Charges Page: 294
Big Ideas	Details	Unit: Magnetism & Electromagnetism
	1.	Homework Problems (M) A wire 1 m long carries a current of 5 A. The wire is at right angles to a uniform magnetic field. The force on the wire is 0.2 N. What is the strength of the magnetic field?
	2.	Answer: 0.04 T (S) A wire 0.75 m long carries a current of 3 A. The wire is at an angle of 30° to a uniform magnetic field. The force on the wire is 0.5 N. What is the strength of the magnetic field?
	3.	Answer: $0.\overline{4}$ T (M) Two currents (one of 2 A and the other of 4 A) flow through wires that are parallel to each other, with the currents flowing in the same direction. The wires are 3 m long and are separated by 8 cm (0.08 m). What is the net magnetic field at the midpoint between the two wires? (<i>Hint: Find the magnetic field produced by each wire and add them, remembering that magnetic fields are vectors.</i>)
		Answer: 1×10 ⁻⁵ T

Magnetism & Moving Charges

Big Ideas	Details		Unit: Magnetism & Electromagnetism
	4.	(M)	A wire 2 m long moves perpendicularly through a 0.08 T field at a speed
		of 7	7 <u>m</u> .
		a.	What emf is induced?
			Answer: 1.12 V
		b.	If the wire has a resistance of 0.50 Ω , use Ohm's Law to find the current
			that flows through the wire.
			Answer: 2.24 A

Unit: Magnetism & Electromagnetism

Electromagnetic Induction & Faraday's Law

Unit: Magnetism & Electromagnetism

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS3-5

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 12.1.A, 12.1.A.1,

12.1.A.1.i, 12.1.A.1.ii, 12.1.A.2, 12.1.A.2.i, 12.1.A.2.ii, 12.1.B.2, 12.1.B.4

Mastery Objective(s): (Students will be able to...)

- Describe and draw magnetic fields.
- Calculate magnetic flux.

Success Criteria:

- Magnetic field lines connect north and south poles of the magnet.
- Arrows on field lines point from north to south.

Language Objectives:

• Explain how a compass works.

Tier 2 Vocabulary: field, north pole, south pole

Labs, Activities & Demonstrations:

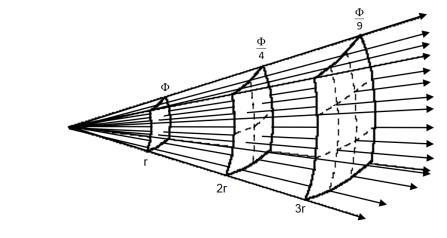
- ferrofluid
- representation of flux as dots on a balloon

Notes:

Magnetic Flux

flux: the flow of fluid, energy or particles across a given area.

If a quantity (such as a magnetic field) originates from a point, the field spreads out and the amount of flux through a given area decreases as the square of the distance from that point.



Electromagnetic Induction & Faraday's Law Page: 297

araday's Law Page: 297 Unit: Magnetism & Electromagnetism

magnetic flux (Φ): the total amount of a magnetic field that passes through a surface.

Stronger magnetic fields are generally shown with a higher density of field lines. Using this representation, you can think of the magnetic flux as the number of field lines that pass through an area.

The equation for magnetic flux is Faraday's Law, named for the English physicist Michael Faraday. The equation is usually presented as a surface integral, but in algebraic form it looks like the following:

$$\Phi_B = \vec{B} \cdot \vec{A} = BA \cos \theta$$

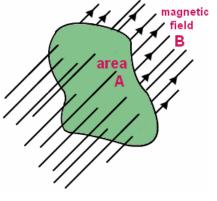
 \vec{B} = strength of magnetic field (T)

 Φ = magnetic flux (Wb)

where:

Details

Big Ideas



 \vec{A} = area of the region of interest that the magnetic field passes through (m²)

The unit for magnetic flux is the weber (Wb). One tesla is one weber per square meter.

$$1T \equiv 1\frac{Wb}{m^2}$$

Big Ideas Details

Unit: Magnetism & Electromagnetism

Magnetic Fields and Electric Current

Like gravitational and electric fields, a magnetic field is a force field. (Recall that force fields are vector quantities, meaning that they have both magnitude and direction.) The strength of a magnetic field is measured in teslas (T), named after the Serbian-American physicist Nikola Tesla.

 $1T = 1\frac{N}{A \cdot m}$

In the 1830s, English physicists Michael Faraday and Joseph Henry each independently discovered that an electric current could be produced by moving a magnet through a coil of wire, or by moving a wire through a magnetic field. This process is called electromagnetic induction.

If we move a conductive rod or wire that has length ℓ at a velocity v through a magnetic field of strength B, the magnetic forces send positive charges to one end of the rod and negative charges to the other. This creates a potential difference (emf) between the ends of the rod:

 $\mathcal{E} = \mathbf{v} \mathbf{B} \ell$

If the rod or wire is part of a closed loop (circuit), then the induced ε produces a current around the closed loop. From Ohm's Law, $\varepsilon = IR$, we get:

$$I = \frac{\mathcal{E}}{R} = \frac{\mathbf{v}B\ell}{R}$$

This production of emf is called the Hall effect, after American physicist Edwin Hall, who discovered this relationship in 1879.

EMF Produced by Changing Magnetic Flux

A changing magnetic field produces an electromotive force (emf) in a loop of wire. This emf is given by the equation:

$$\mathcal{E} = -\frac{d\Phi_B}{dt} = -\frac{\Delta\Phi_B}{\Delta t} = -\frac{\Delta(BA\cos\theta)}{\Delta t}$$
(calculus) (algebraic)

If we replace the loop of wire with a coil that has *n* turns, the equation becomes:

$$\mathcal{E} = -n \frac{d\Phi_B}{dt} = -n \frac{\Delta \Phi_B}{t}$$
(calculus) (algebraic)

Unit: Magnetism & Electromagnetism

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-5

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 12.2.B, 12.2.B.1,

12.2.B.2, 12.2.B.2.ii, 12.3.A.1, 12.3.A.1.i, 12.3.A.1.iii, 12.3.A.1.iv, 12.3.B.1, 12.3.B.1.ii

Mastery Objective(s): (Students will be able to ...)

- Explain the basic design of solenoids, motors, generators, transformers and mass spectrometers.
- Calculate the voltage and power from a step-up or step-down transformer.

Success Criteria:

- Descriptions & explanations account for observed behavior.
- Calculations are set up and executed correctly.

Language Objectives:

• Explain how various devices work including solenoids, electromagnets and electric motors.

Tier 2 Vocabulary: force, field

Labs, Activities & Demonstrations:

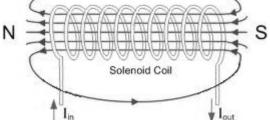
- build electromagnet
- build electric motor
- build speaker

Notes:

Solenoid

A solenoid is a coil made of fine wire. When a current is passed through the wire, it produces a magnetic field through the center of the coil.

When a current is applied, a permanent magnet placed in the center of the solenoid will be attracted or repelled and will move. Magnetic Field due to the Current Flow



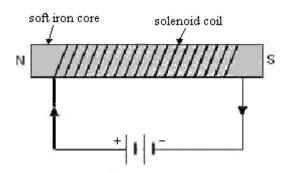
One of the most common uses of a solenoid is for electric door locks.

Big Ideas Details

Electromagnet

An electromagnet is a device that acts as magnet only when electric current is flowing through it.

An electromagnet is made by placing a soft iron core in the center of a solenoid. The high magnetic permeability of iron causes the resulting magnetic field to become thousands of times stronger:



Because the iron core is not a permanent magnet, the electromagnet only works when current is flowing through the circuit. When the current is switched off, the electromagnet stops acting like a magnet and releases whatever ferromagnetic objects might have been attracted to it.

Of course, the above description is a simplification. Real ferromagnetic materials such as iron usually experience magnetic remanence, meaning that some of the electrons in the material remain aligned, and the material is weakly magnetized.

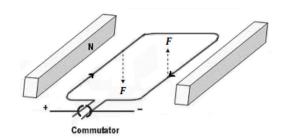
While magnetic remanence is undesirable in an electromagnet, it is the basis for magnetic computer storage media, such as audio and computer tapes and floppy and hard computer disks. To write information onto a disk, a disk head (an electromagnetic that can be moved radially) is pulsed in specific patterns as the disk spins. The patterns are encoded on the disk as locally magnetized regions.

When encoded information is read from the disk, the moving magnetic regions produce a changing electric field that causes an electric current in the disk head.

Details **Big Ideas**

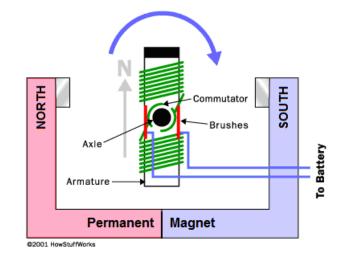
Motor

The force produced by a moving current in a magnetic field can be used to cause a loop of wire to spin:



A commutator is used to reverse the direction of the current as the loop turns, so that the combination of attraction and repulsion always applies force in the same direction.

If we replace the loop of wire with an electromagnet (a coil of wire wrapped around a material such as iron that has both a high electrical conductivity and a high magnetic permeability), the electromagnet will spin with a strong force.



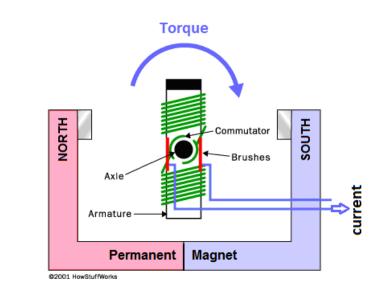
An electromagnet that spins because of its continuously switching attraction and repulsion to the magnetic field produced by a separate set of permanent magnets is called a motor. An electric motor turns electric current into rotational motion, which can be used to do work.

Details

Big Ideas

Generator

A <u>generator</u> uses the same components and operates under the same principle as a motor, except that a mechanical force is used to spin the coil. When the coil moves through the magnetic field, it produces an electric current. Thus, a generator is a device that turns rotational motion (work) into an electric current.



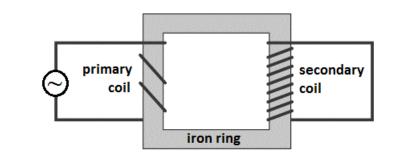
Recall from the previous section that Lenz's Law gives the emf produced by the generator. Because the coil is rotating through a uniform magnetic field, the magnetic flux through the coil is constantly changing, which means calculus is needed to calculate the emf produced.

$$\mathcal{E} = -n \frac{d\Phi_B}{dt}$$

Inductor (Transformer)

Because electric current produces a magnetic field, a ring made of a ferromagnetic material can be used to move an electric current. An inductor (transformer) is a device that takes advantage of this phenomenon in order to increase or decrease the voltage in an AC circuit.

The diagram below shows an inductor or transformer.



The current on the input side (primary) generates a magnetic field in the iron ring. The magnetic field in the ring generates a current on the output side (secondary).

In this particular transformer, the coil wraps around the output side more times than the input. This means that each time the current goes through the coil, the magnetic field adds to the electromotive force (voltage). This means the voltage will increase in proportion to the increased number of coils on the output side. However, the magnetic field on the output side will produce less current with each turn, which means the current will decrease in the same proportion:

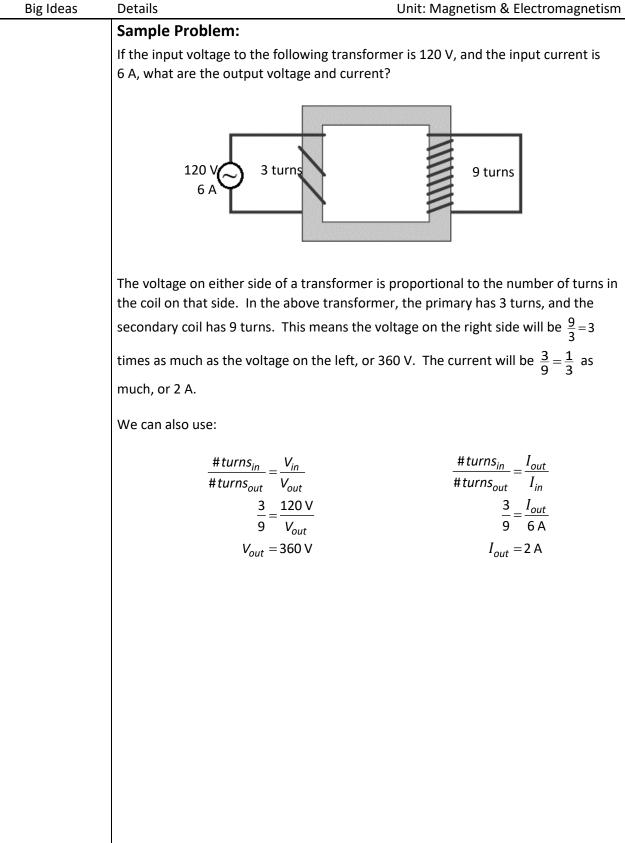
$$\frac{\#turns_{in}}{\#turns_{out}} = \frac{V_{in}}{V_{out}} = \frac{I_{out}}{I_{in}}$$
$$P_{in} = P_{out}$$

A transformer like this one, which produces an increase in voltage, is called a <u>step-up</u> <u>transformer</u>; a transformer that produces a decrease in voltage is called a <u>step-down</u> <u>transformer</u>.

Big Ideas

Details

Devices that Use Electromagnetism Page: 304 s Unit: Magnetism & Electromagnetism



Details

Big Ideas

agnetism Page: 305 Unit: Magnetism & Electromagnetism

Mass Spectrometer

A mass spectrometer is a device that uses the path of a charged particle in a magnetic field to determine its mass.

The particle is first selected for the desired velocity, as described on page 292. Then the particle enters a region where the only force on it is from the applied magnetic field. (In the example below, the magnetic field is directed out of the page.)

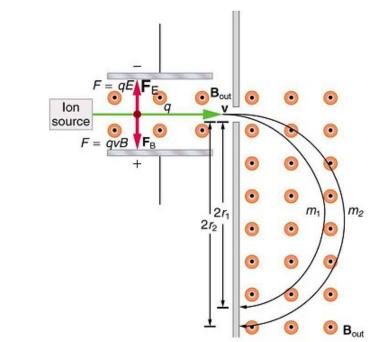


Image © 2016 by Douglas College Physics. Used with permission.

The magnetic field applies a force on the particle perpendicular to its path. As the particle's direction changes, the direction of the applied force changes with it, causing the particle to move in a circular path.

The path of the particle is the path for which the centripetal force (which you may recall from physics 1) is equal to the magnetic force:

$$F_{B} = F_{c}$$

$$qvB = \frac{mv^{2}}{r}$$

$$r = \frac{mv^{2}}{qvB} = \frac{mv}{qB}$$

Thus if the particles are all ions with the same charge and are selected for having the same speed, the radius of the path will be directly proportional to the mass of the particle.

Big Ideas	Details	Unit: Mechanical Waves
	Introduction: Mechanica	l Waves
	Unit: Mechanical Waves	
	Topics covered in this chapter:	
	Waves	
	Wave Interactions	
	Sound & Music	
	Sound Level (Loudness)	
	Doppler Effect	
	Exceeding the Speed of Sound	
	This chapter discusses properties of waves that travel thro (mechanical waves).	ugh a medium
	 Waves gives general information about waves, include equations. Wave Interactions describes what happe space within a medium. 	
	 Sound & Music describes the properties and equatio music and musical instruments. 	ns of waves that relate to
	Sound Level describes the decibel scale and how loug	dness is measured.
	 The Doppler Effect describes the change in pitch due or receiver (listener). 	to motion of the source
	• Exceeding the Speed of Sound describes the Mach sc	ale and sonic booms.
	Standards addressed in this chapter:	
	NGSS Standards/MA Curriculum Frameworks (2010	6):
	HS-PS4-1. Use mathematical representations to suppor relationships among the frequency, wavelength, and traveling within various media. Recognize that elect travel through empty space (without a medium) as waves that require a medium.	nd speed of waves ctromagnetic waves can
AP [®] only	AP [®] Physics 2 Learning Objectives/Essential Knowl	edge (2024):
- ,	14.1.A: Describe the physical properties of waves and	wave pulses.
	14.1.A.1: Waves transfer energy between two locat matter between those locations.	ions without transferring
	14.1.A.1.i : A wave pulse is a single disturbance that without transferring matter between two locations of the second s	

Introduction: Mechanical Waves

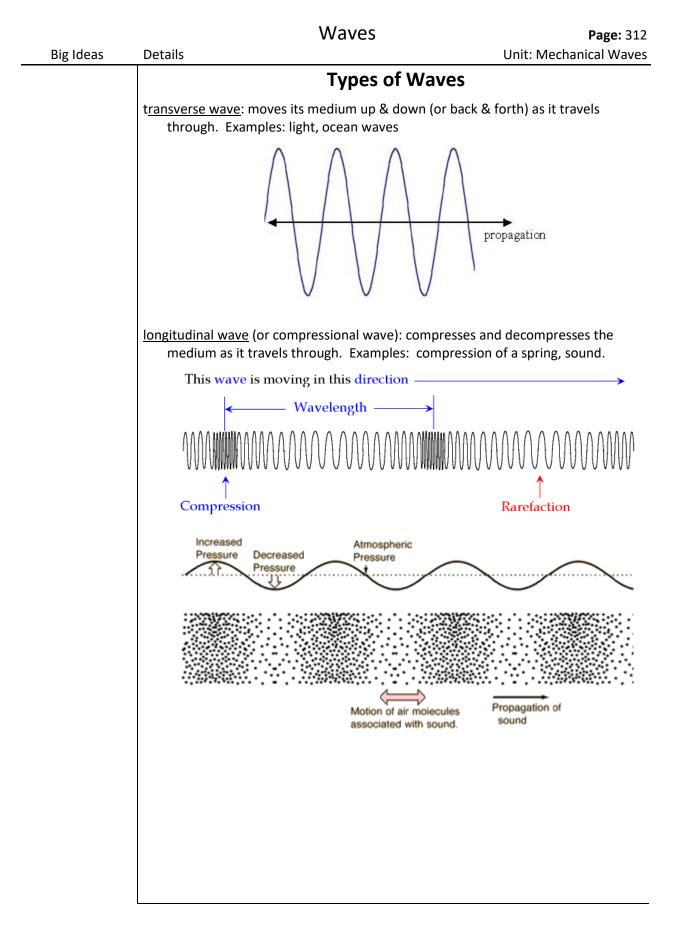
	Introduction: Mechanical Waves Page: 308
Big Ideas	Details Unit: Mechanical Waves
AP [®] only	14.1.A.1.ii: A wave is modeled as a continuous, periodic disturbance with well-defined wavelength and frequency.
	14.1.A.2: Mechanical waves or wave pulses require a medium in which to propagate. Electromagnetic waves or wave pulses do not require a medium in which to propagate.
	14.1.A.3: The speed at which a wave or wave pulse propagates through a medium depends on the type of wave and the properties of the medium.
	14.1.A.3.i : The speed of all electromagnetic waves in a vacuum is a universal physical constant, $c = 3 \times 10^8 \frac{\text{m}}{\text{s}}$.
	14.1.A.3.ii : The speed at which a wave pulse or wave propagates along a string is dependent upon the tension in the string, F_{τ} , and the mass per length of the string.
	14.1.A.3.iii: In a given medium, the speed of sound waves increases with the temperature of the medium.
	14.1.A.4 : In a transverse wave, the direction of the disturbance is perpendicular to the direction of propagation of the wave.
	14.1.A.5 : In a longitudinal wave, the direction of the disturbance is parallel to the direction of propagation of the wave.
	14.1.A.5.i : Sound waves are modeled as mechanical longitudinal waves.
	14.1.A.5.ii: The regions of high and low pressure in a sound wave are called compressions and rarefactions, respectively.
	14.1.A.6 : Amplitude is the maximum displacement of a wave from its equilibrium position.
	14.1.A.6.i: The amplitude of a longitudinal pressure wave may be determined by the maximum increase or decrease in pressure from equilibrium pressure.
	14.1.A.6.ii : The loudness of a sound increases with increasing amplitude.
	14.1.A.6.iii: The energy carried by a wave increases with increasing amplitude.
	14.2.A : Describe the physical properties of a periodic wave.
	14.2.A.1 : Periodic waves have regular repetitions that can be described using period and frequency.
	14.2.A.1.i : The period is the time for one complete oscillation of the wave.
	14.2.A.1.ii : The frequency is the rate at which the wave repeats.
	14.2.A.1.iii : The amplitude of a wave is independent of the period and the frequency of that wave.
	14.2.A.1.iv : The energy of a wave increases with increasing frequency.
	14.2.A.1.v : The frequency of a sound wave is related to its pitch.

Introduction: Mechanical Waves

Big Ideas	Details Unit: Mechanical Waves
AP [®] only	14.2.A.1.vi : Wavelength is the distance between successive corresponding positions (such as peaks or troughs) on a wave.
	 14.2.A.2: A sinusoidal wave can be described by equations for the displacement from equilibrium at a specific location as a function of time. A wave can also be described by an equation for the displacement from equilibrium at a specific time as a function of position.
	14.2.A.3 : For a periodic wave, the wavelength is proportional to the wave's speed and inversely proportional to the wave's frequency.
	14.3.A : Describe the interaction between a wave and a boundary.
	14.3.A.1 : A wave that travels from one medium to another can be transmitted or reflected, depending on the properties of the boundary separating the two media.
	14.3.A.1.i: A wave traveling from one medium to another (for example, a wave traveling between low-mass and high-mass strings) will result in reflected and transmitted waves.
	14.3.A.1.ii : A reflected wave is inverted if the transmitted wave travels into a medium in which the speed of the wave decreases.
	14.3.A.1.iii: A reflected wave is not inverted if the transmitted wave travels into a medium in which the speed of the wave increases.
	14.3.A.1.iv : The frequency of a wave does not change when it travels from one medium to another.
	Skills learned & applied in this chapter:
	• Visualizing wave motion.

Big Ideas	Details	Page: 310 Unit: Mechanical Waves
0	Waves	
	Unit: Mechanical Waves	
	NGSS Standards/MA Curriculum Frameworks (2016	5): HS-PS4-1
	AP [®] Physics 2 Learning Objectives/Essential Knowle 14.1.A.1.i, 14.1.A.1.ii, 14.1.A.2, 14.1.A.3, 14.1.A 14.1.A.5, 14.1.A.5.i, 14.1.A.5ii, 14.1.A.6, 14.1.A 14.2.A.1.ii, 14.2.A.1.iii, 14.2.A.1.iv, 14.2.A.1.vi,	edge (2024): 14.1.A, 14.1.A.1, A.3.i, 14.1.A.3.iii, 14.1.A.4, A.6.i, 14.2.A, 14.2.A.1, 14.2.A.1.i,
	Mastery Objective(s): (Students will be able to)	
	 Describe and explain properties of waves (free 	quency, wavelength, etc.)
	 Differentiate between transverse, longitudinal 	l and transverse waves.
	• Calculate wavelength, frequency, period, and	velocity of a wave.
	Success Criteria:	
	 Parts of a wave are identified correctly. 	
	 Descriptions & explanations account for obser 	ved behavior.
	Language Objectives:	
	 Describe how waves propagate. 	
	Tier 2 Vocabulary: wave, crest, trough, frequency, v	wavelength
	Labs, Activities & Demonstrations:	
	 Show & tell: transverse waves in a string tied a a spring, torsional waves. 	at one end, longitudinal waves in
	Buzzer in a vacuum.	
	 Tacoma Narrows Bridge collapse movie. 	
	 Japan tsunami TV footage. 	
	Notes:	
		-
	Notes: <u>wave pulse</u> : a single disturbance that travels from o	tween two locations.
	Notes: <u>wave pulse</u> : a single disturbance that travels from o transfers energy without transferring matter between the setward of the setwa	tween two locations.
	Notes: <u>wave pulse</u> : a single disturbance that travels from o transfers energy without transferring matter bet <u>wave</u> : a continuous, periodic disturbance with well- frequency.	tween two locations. defined wavelength and

as Detai	le	Wa	ves	Page Unit: Mechanical W
1		a wave that pro	nagates through a m	nedium via contact betwe
p	articles of t			inical waves include ocea
1		gy of the wave is ses through it.	transmitted via the p	particles of the medium a
2	moved b	y the wave passin	g through and then r	rticles of the medium are return to their original below is an example.)
3	-		duck motion	west in liquids. The veloc
	a mecha	nical wave is depe	ndent on characteris	stics of the medium:
			exa	mple
	state	relevant factors	exa medium	mple velocity of sound
	state gas			1
		factors density,	medium air	velocity of sound
	gas	factors density, pressure density,	medium air (20 °C and 1 atm)	velocity of sound $343 \frac{m}{s}$ (768 $\frac{mi}{hr}$)



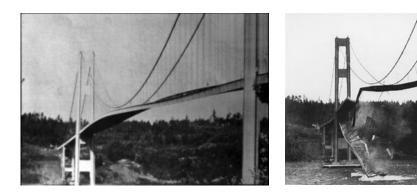
honors (not AP®) Details

Big Ideas

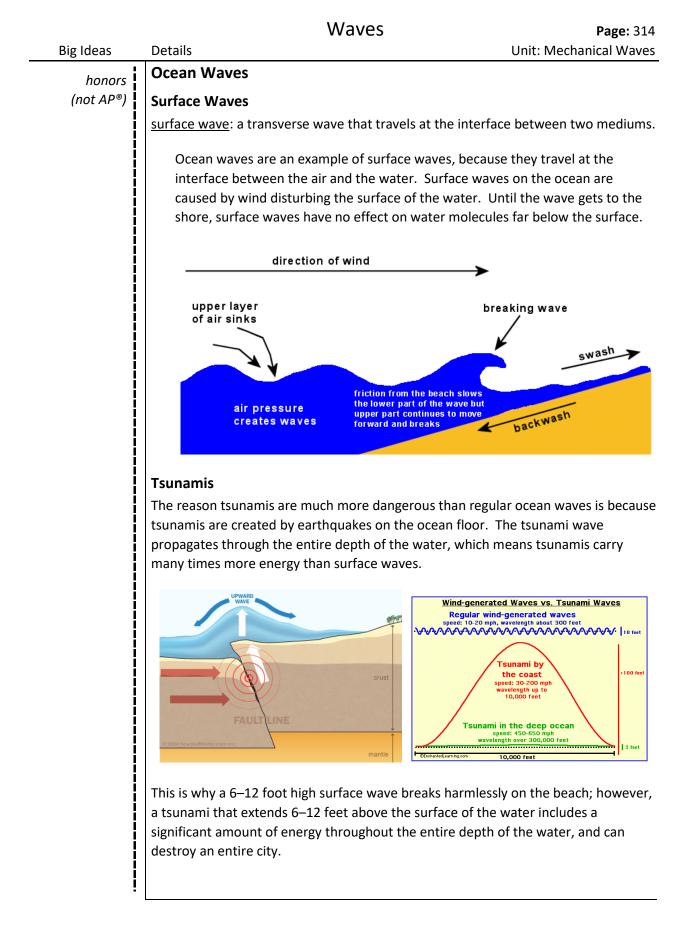
torsional wave: a type of transverse wave that propagates by twisting about its direction of propagation.

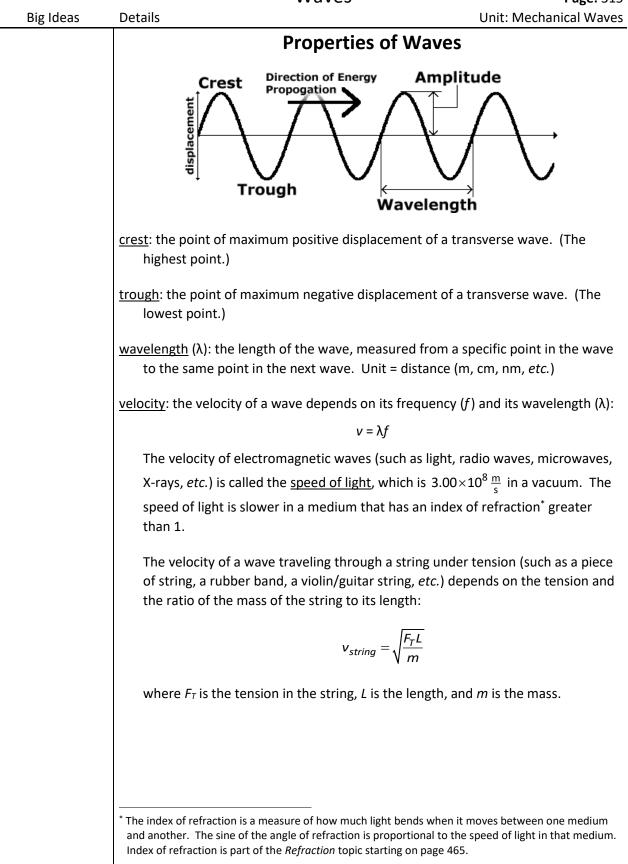


The most famous example of the destructive power of a torsional wave was the Tacoma Narrows Bridge, which collapsed on November 7, 1940. On that day, strong winds caused the bridge to vibrate torsionally. At first, the edges of the bridge swayed about eighteen inches. (This behavior had been observed previously, earning the bridge the nickname "Galloping Gertie".) However, after a support cable snapped, the vibration increased significantly, with the edges of the bridge being displaced up to 28 feet! Eventually, the bridge started twisting in two halves, one half twisting clockwise and the other half twisting counterclockwise, and then back again. This opposing torsional motion eventually caused the bridge to twist apart and collapse.



The bridge's collapse was captured on film. Video clips of the bridge twisting and collapsing are available on the internet. There is a detailed analysis of the bridge's collapse at http://www.vibrationdata.com/Tacoma.htm

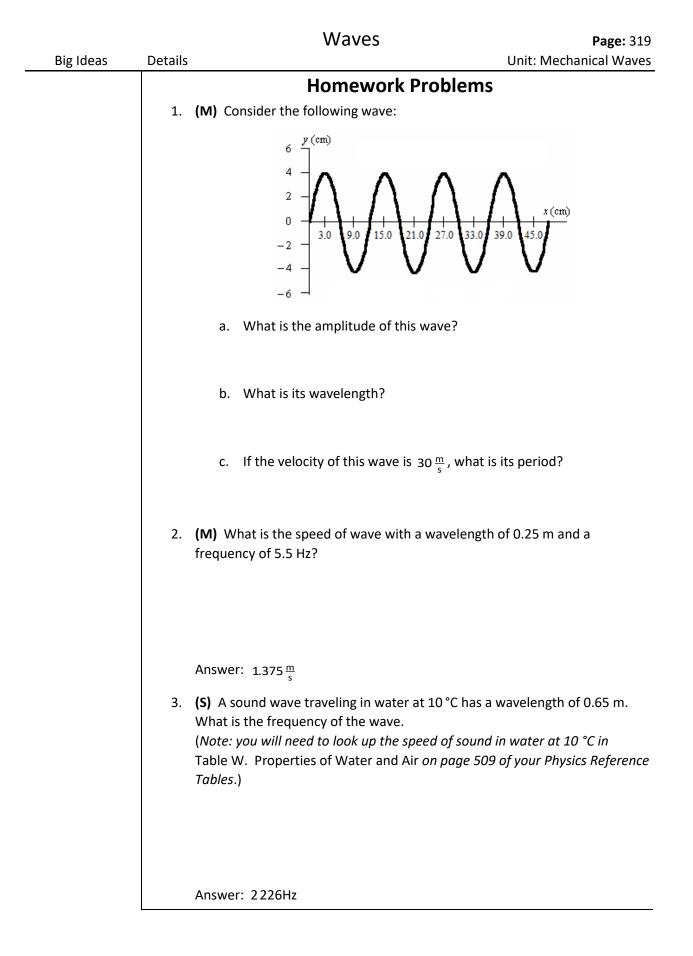




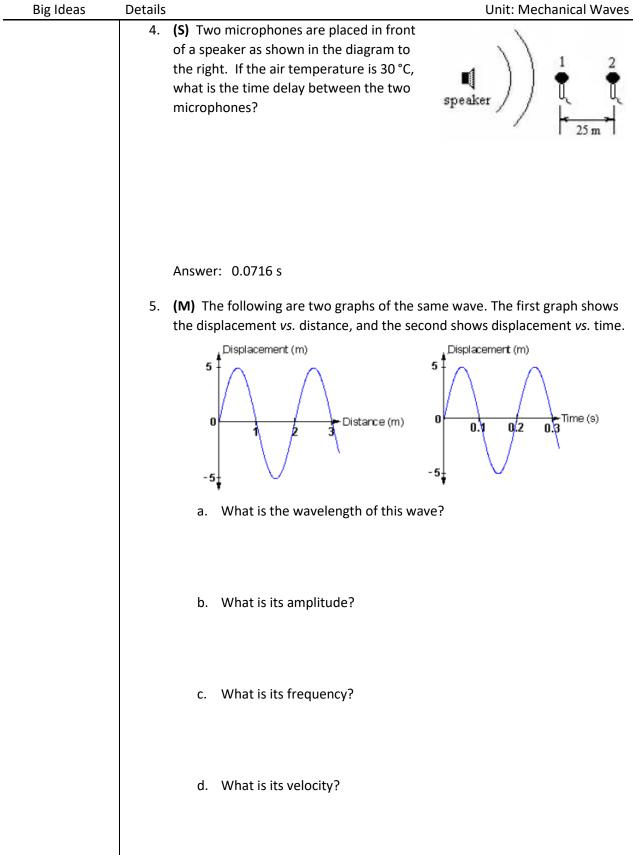
	Waves	Page: 316
Big Ideas	Details	Unit: Mechanical Waves
	amplitude (A): the distance of maximum displacement of the wave passes through it.	of a point in the medium as
	For a transverse wave, the amplitude is the maximu of a trough.	um height of a crest or depth
	For a longitudinal wave, the amplitude is a particle distance from the equilibrium point. In the case of the amplitude as loudness, which is described in mo <i>Level (Loudness)</i> , starting on page 343.	sound waves, we perceive
	intensity: the intensity of a wave pulse is the power tra where the area is defined as the region where the w through a plane perpendicular to the direction of pr	wave pulse strikes or passes
	For example, suppose that a wave pulse transfers a	power $P = 1 W$ through an
	area $A = 1 \text{ m}^2$ at a distance $r = 1 \text{ m}$. This wave puls $I = \frac{P}{A} = 1 \frac{W}{m}.$	se would have an intensity of
	P A A A A A A A A A A A A A A A A A A A	A A A A A A A A A A A A A A A A A A A A
	As the wave pulse travels farther from its source, it intensity decreases as the square of distance (this c	-
	of a sphere, which is $4\pi r^2$), so at a distance of 2 m, an intensity of $0.25 \frac{W}{m}$, and at a distance of 3 m, the	the wave pulse would have
	intensity of $0.11\frac{W}{m}$.	
	The intensity of a wave pulse is proportional to the	square of its amplitude.

	vvaves	Page: 31/	
Big Ideas	Details	Unit: Mechanical Waves	
	Periodic Waves Periodic waves are waves that have consistent, regular repetitions.		
	frequency (f or v): the number of waves that travel pass of time. Unit = $1/_{time}$ (Hz = $1/_s$)	t a point in a given amount	
	Note that while high school physics courses generall frequency, college courses often use v (the Greek left from but easy to confuse with the Roman letter "v")	tter "nu", which is different	
	The energy of a wave is proportional to both its amplitude and its frequency. Each pulse carries an amount of energy proportional to the amplitude. The number of pulses of energy delivered in a given amount of time is the frequency. (Think of boxing: the strength of each punch is the amplitude, and the number of punches per second is the frequency.)		
	period or time period (T): the amount of time between two adjacent waves. Unit = time (usually seconds)		
	$T = \frac{1}{f}$		
	sinusoidal waves:a wave whose graph of displacement vs. time is the trigonometry function sine or cosine.Most of the periodic waves that we will study in this class are sinusoidal waves. Some examples include light waves, sound waves, motions of springs and pendulums, uniform circular motion, vibrations, (electrical) alternating current, vibrations (such as strings in musical instruments), and some aspects of ocean currents, climate cycles, population cycles, and economic trends.In a sinusoidal wave, the general equation for displacement vs. time is: $x(t) = A\cos(2\pi ft) = A\cos(\alpha t)$ where:		
	 x(t) = position as a function of time 		
	• x = displacement from equilibrium position	1	
	• $t = time$		
	• f = frequency • ω = angular velocity		
	• ω = angular velocity		

	Waves	Page: 318	
Big Ideas		echanical Waves	
	The equation for displacement as a function of position is:		
	$y(x) = A\cos\left(2\pi\frac{x}{\lambda}\right)$		
	where:		
	 y(x) = displacement (y-position) as a function of position i of propagation (x-position) 	n the direction	
	 x = position in the direction of propagation (x-position) λ = wavelength 		
	Sample Problem:		
	Q: The Boston radio station WZLX broadcasts waves with a frequen 100.7 MHz. If the waves travel at the speed of light, what is the	-	
	A: $f = 100.7 \text{ MHz} = 100700000 \text{ Hz} = 1.007 \times 10^8 \text{ Hz}$		
	$v = c = 3.00 \times 10^8 \frac{\text{m}}{\text{s}}$		
	$v = \lambda f$		
	$3.00 \times 10^8 = \lambda (1.007 \times 10^8)$		
	$\lambda = \frac{3.00 \times 10^8}{1.007 \times 10^8} = 2.98 \mathrm{m}$		
	1.007×10 ⁻		



Waves



Wave Interactions

Unit: Mechanical Waves

Details

Big Ideas

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS4-1

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 14.2.A,

14.2.A.3, 14.3.A, 14.3.A.1, 14.3.A.1.i, 14.3.A.1.ii, 14.3.A.1.iii, 14.3.A.1.iv, 14.8.A.2

Mastery Objective(s): (Students will be able to...)

• Explain the behavior of waves when they pass each other in the same medium and when they reflect off something.

Success Criteria:

• Descriptions & explanations account for observed behavior.

Language Objectives:

• Explain what happens when two waves pass through each other.

Tier 2 Vocabulary: reflection

Labs, Activities & Demonstrations:

- waves on a string or spring anchored at one end
- large Slinky with longitudinal and transverse waves passing each other

Notes:

A wave that encounters a boundary between one medium and another can be transmitted or reflected.

transmission: when a wave continues traveling from one medium into another.

<u>reflection</u>: when a wave "bounces" back from the boundary between one medium and another.

When a wave travels from one medium into another, its frequency does not change.

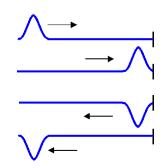
Reflection

When a wave is reflected:

- The wave is inverted (turned upside-down) if it travels into a wave that causes its speed to decrease.
- The wave is not inverted if it travels into a medium that causes its speed to increase.

Wave Interactions

An example of this is shaking a rope to send a pulse along it. If the rope is attached to a wall, the speed of the wave in the wall would be faster (because the wall is more dense), so the wave is reflected without inverting. If the rope is not attached to anything, the speed of the wave in air would be slower (because the air is less dense), so the wave is inverted when it is reflected.



Superposition

Waves are not physical objects. A wave is defined as a disturbance of the particles of a medium, but the waves are energy carriers, not the medium itself.

This means that:

Big Ideas

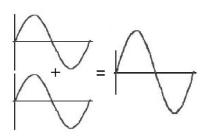
Details

- When two or more waves encounter one another, the medium at the meeting point is moved separately by each wave. This means that the displacement of each particle of the medium is the vector sum of the amplitudes of each separate wave.
- As the waves continue beyond the meeting point, the interactions caused by each wave continue with each wave. This means the waves "pass through" each other.

When waves are superimposed (occupy the same space), their amplitudes add.

<u>constructive interference</u>: when waves add in a way that the amplitude of the resulting wave is larger than the amplitudes of the component waves.

Because the wavelengths are the same and the maximum, minimum, and zero points all coïncide (line up), the two component waves are said to be "in phase" with each other.

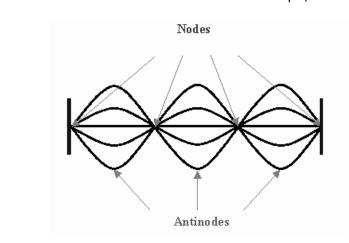


Wave Interactions

	Wave Interactions	Page: 323
Big Ideas	Details	Unit: Mechanical Waves
	destructive interference:way that the amplitude of the resulting wave is smaller than the amplitudes of the component waves. (Sometimes we say that the waves "cancel" each other.)Because the wavelengths are the same but the maximum, minimum, and zero points do not coïncide, the waves are said to be "out of phase" with each other.	+ = +
	Constructive Interference	Destructive Interference

Standing Waves

standing wave: when a reflected periodic wave is in phase with the incident (incoming) wave. When this happens, the reflections cause constructive interference, which amplifies the wave. This amplification is called "resonance", which will be discussed further in the *Sound & Music* topic, starting on page 329.



Because human eyes have a "frame rate" of 30–60 "frames" per second, standing waves appear stationary to us. Points along the wave with zero displacement (which appear not to be moving) are called "nodes". Points of maximum displacement are called "antinodes".

For a wave with boundaries to media that are denser at both ends, the wave is inverted when it is reflected. In these situations, standing waves occur when the medium is an exact multiple of half the wavelength.

Physics 2 In Plain English

Big Ideas

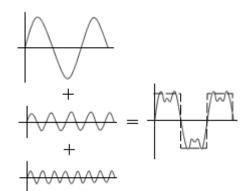
Details

Wave Interactions

Details

Big Ideas

When waves with different wavelengths and amplitudes are superimposed, the result can be complex:

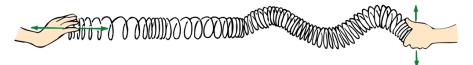


This is, for example, how it is possible to hear multiple sounds at once, even though the sounds share the same medium (the air between the source and your ears).

This is also how radio waves encode a signal on top of a "carrier" wave. Your radio's antenna receives ("picks up") radio waves within a certain range of frequencies. Imagine that the bottom wave (the one with the shortest wavelength and highest frequency) is the "carrier" wave. If you tune your radio to its frequency, the radio will filter out other waves that don't include the carrier frequency. Then your radio subtracts the carrier wave, and everything that is left is sent to the speakers.



1. **(M)** A Slinky is held at both ends. The person on the left creates a longitudinal wave, while at same time the person on the right creates a transverse wave with the same frequency. Both people stop moving their ends of the Slinky just as the waves are about to meet.



a. Draw a picture of what the Slinky will look like when the waves completely overlap.

b. Draw a picture of what the Slinky will look like just after the waves no longer overlap.

Big Ideas

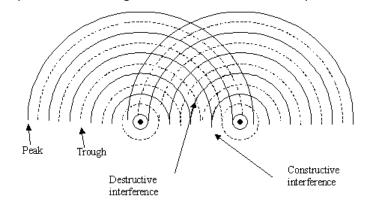
Details



Details

Two-Dimensional Interference Patterns

When two progressive waves propagate into each other's space, the waves produce interference patterns. This diagram shows how interference patterns form:



The following picture^{*} shows an interference pattern created by ocean waves, one of which has been reflected off a point on the shore. The wave at the left side of the picture is traveling toward the right, and the reflected wave at the bottom right of the picture is traveling toward the top of the picture.



Photo © 2015 by Jeff Bigler. Used with permission.

Because the sun is low in the sky (the picture was taken just before sunset), the light is reflected off the water, and the crests of the waves produce shadows behind them.

^{*} Taken from Tortola in the British Virgin Islands, looking west toward Jost Van Dyke.

Wave Interactions

Big Ideas

Details

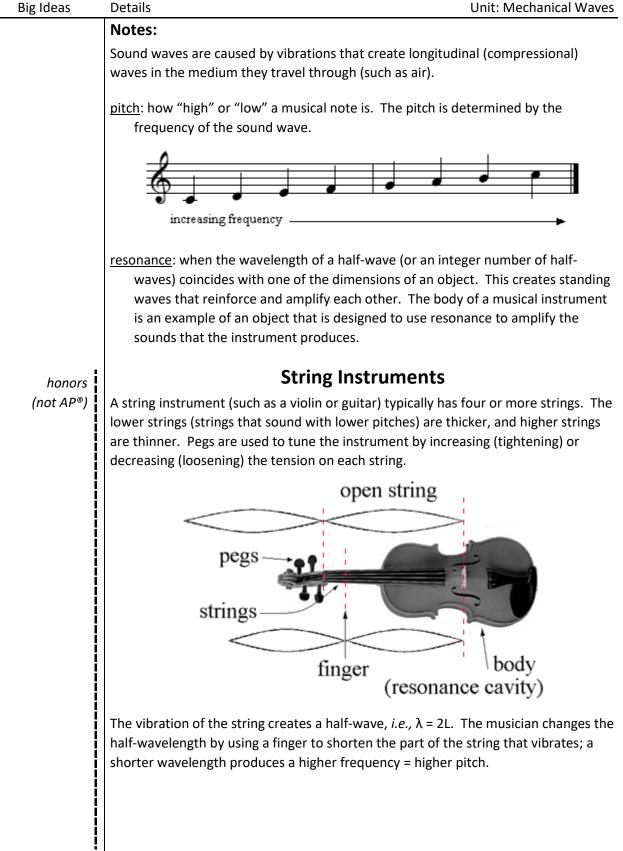
The English physicist Thomas Young performed an experiment in 1801 in which he passed light through two narrow slits and observed the following interference pattern:



In this picture, the bright regions are wave "peaks", and the dark regions are "troughs". The brightest intersections are regions where the peaks interfere constructively, and the darkest intersections are regions where the troughs interfere constructively.

Prior to Young's double slit experiment, the prevailing opinion, held by Isaac Newton, was that light was a particle. Young's experiment was conclusive proof that light has wave properties.

		Sound & Music	Page: 329
Big Ideas	Details		Unit: Mechanical Waves
		Sound & Mus	sic
	Unit: Mechanic	cal Waves	
	NGSS Standar	ds/MA Curriculum Frameworks (2	.016): HS-PS4-1
	AP [®] Physics 2	Learning Objectives/Essential Kno	•
	Mastery Obje	ctive(s): (Students will be able to)	
	Describe	how musical instruments produce sou	unds.
	Describe	how musical instruments vary pitch.	
	Calculate	frequencies of pitches produced by a	vibrating string or in a pipe.
	Success Criter	ia:	
	Description	ons & explanations account for observ	ved behavior.
	 Variables equations 	are correctly identified and substitute s.	ed correctly into the correct
	 Algebra is reasonab 	s correct and rounding to appropriate le.	number of significant figures is
	Language Obj	ectives:	
	• Explain w	hat produces the vibrations in various	s types of musical instruments.
	Tier 2 Vocabu	lary: pitch	
	Labs, Activiti	es & Demonstrations:	
	-	ell: violin, penny whistle, harmonica, I	Boomwhackers.
		z resonators—bottles of different size th your mouth open.	es/air volumes, slapping your
	Frequence	y generator & speaker.	
	 Rubens tu 	ube ("sonic flame tube").	
	Measure	the speed of sound in air using a reso	nance tube.



	Sound 8		Page: 331
Big Ideas	Details		Mechanical Waves
	The velocity of the wave produced length and mass of the vibrating po	•	
		$v_{string} = \sqrt{\frac{F_T L}{m}}$	
	where:		
	f = frequency (Hz)	F_T = tension (N)	
m = mass of string (kg) $L = length$			$=\frac{\lambda}{2}$
	For a given velocity and wavelength, the frequency (pitch) produced is:		
	$f = \frac{v}{\lambda} = \frac{v}{2L} = \frac{1}{2L}\sqrt{\frac{F_TL}{m}} = \sqrt{\frac{F_T}{4mL}}$		
	The tuning pegs on a string instrum increasing or decreasing the tensio		juency by
	The thickness of a string affects its therefore vibrates more slowly, cau different strings on the same instru	using it to have a lower pitch. T	This is why
honors	Pipes &	Wind Instruments	
(not AP®)	A pipe (in the musical instrument so mouthpiece (or air inlet) causes the the air molecules to compress and dimensions of the closed section of wavelength. The wavelength and s	e air to oscillate as it enters the spread out at regular intervals the instrument, which determ	pipe. This causes based on the nines the
	Most wind instruments use one of	three ways of causing the air to	o oscillate:
	Brass Instruments With brass instruments like trumper presses his/her lips tightly against to the appropriate frequency. The eff through valves or slides to enable so be discussed in detail later.)	he mouthpiece, and the player ective length of the instrumen	r's lips vibrate at t (pipe) is changed
	Reed Instruments		
	With reed instruments, air is blown back and forth. Clarinets and saxon cane (a semi-stiff plant similar to ba instruments") use two pieces of can and accordions use reeds made fro	ohones use a single reed made amboo). Oboes and bassoons (ne that vibrate against each oth	from a piece of ("double-reed

honors (not AP®)

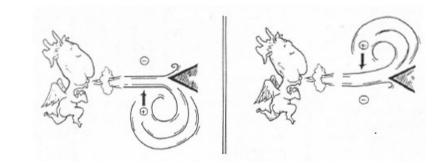
Details

Big Ideas

The effective length of the instrument is changed by covering or uncovering holes along the instrument (pipe) to enable standing waves of different frequencies. (This will be discussed in detail later.)

Whistles (Instruments with Fipples)

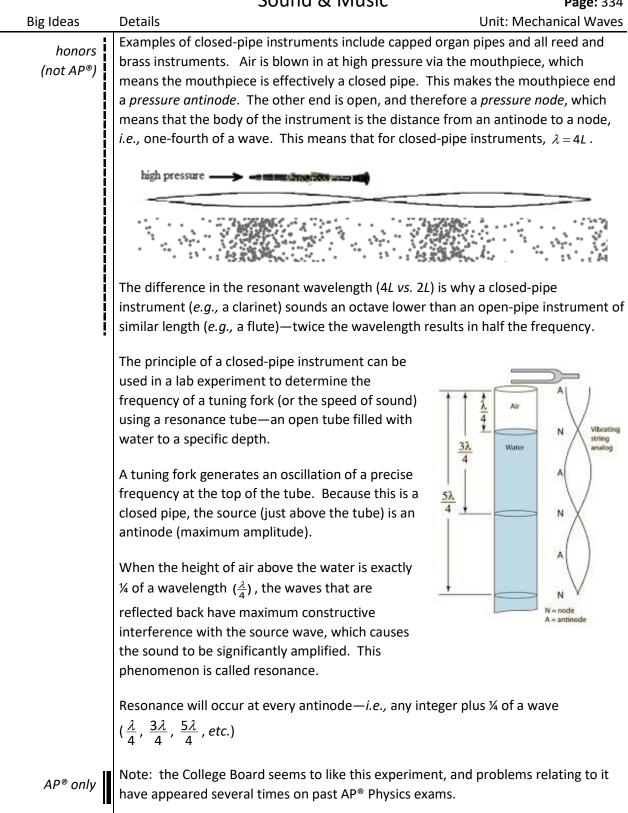
Instruments with fipples include recorders, whistles and flutes. A fipple is a sharp edge that air is blown past. The separation of the air going past the fipple results in a pressure difference on one side *vs.* the other. Air moves toward the lower pressure side, causing air to build up and the pressure to increase. When the pressure becomes greater than the other side, the air switches abruptly to the other side of the fipple. Then the pressure builds on the other side until the air switches back:

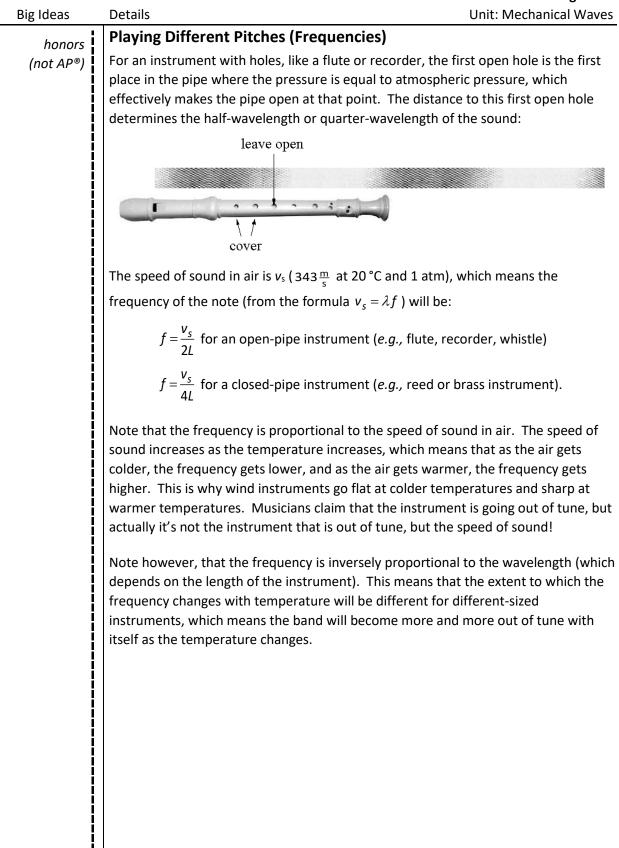


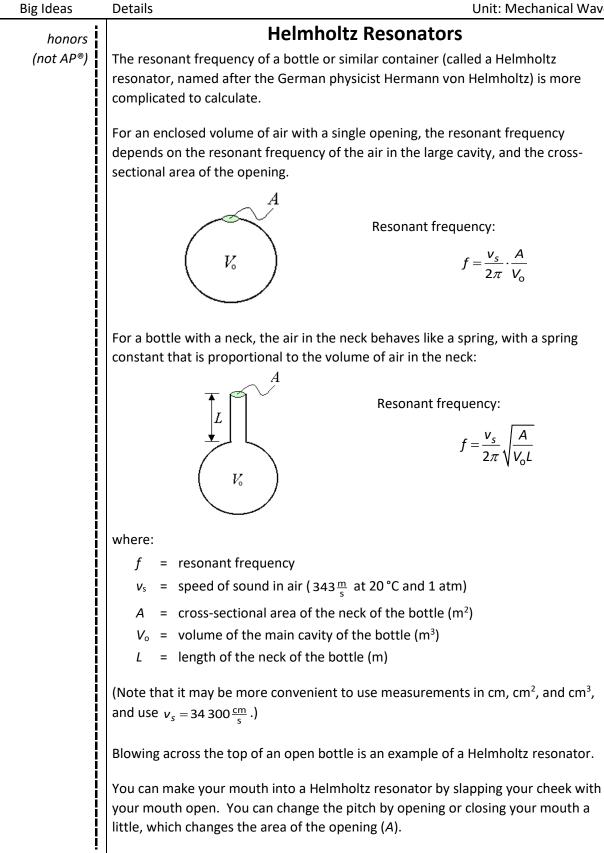
The frequency of this back-and-forth motion is what determines the pitch.

As with reed instruments, the effective length of the instrument is changed by covering or uncovering holes along the instrument (pipe) to enable standing waves of different frequencies.

	Sound & Music Page: 333
Big Ideas	Details Unit: Mechanical Waves
	Open vs. Closed Pipes
	The end of a pipe can be either open to the air or closed. The following diagram
	shows a pipe that is closed at one end and open at the other:
	closed end displacement node pressure antinode
	Air molecules cannot move through the closed end of the pipe. The closed end of
	the pipe is therefore a <i>displacement node</i> , because there can be no displacement of
	the molecules at that end.
	Air molecules have unrestricted movement at the open end of the pipe, because there is no pipe at that point. The open end of the pipe is therefore a <i>displacement</i> <i>antinode</i> , because there can be maximum displacement of the molecules at that end.
	At the open end of the pipe, air pressure must be the same as atmospheric pressure, because any difference in pressure would cause molecules to move toward the area of lower pressure. Because there can be no pressure variation at the open end, the open end of the pipe is a <i>pressure node</i> .
	Conversely, at the closed end of the pipe, there is nowhere for air molecules to go to alleviate pressure differences. Because there can be maximum pressure variation at the closed end, the closed end of the pipe is a <i>pressure antinode</i> .
, i	Open vs. Closed-Pipe Instruments
honors (not AP®)	An open-pipe instrument is open to the atmosphere at both ends. A closed-pipe instrument is open at one end but closed at the other.
	Examples of open-pipe instruments include uncapped organ pipes, whistles, recorders and flutes.
İ	I open end
ļ	
	Notice that the two openings are <i>pressure nodes</i> (where the air pressure <i>must</i> be equal to atmospheric pressure. This means that the length of the body of the instrument (<i>L</i>) is a half-wave, and that the wavelength (λ) of the sound produced must therefore be twice as long, <i>i.e.</i> , $\lambda = 2L$. (This is similar to string instruments, in which the length of the vibrating string is a half-wave.)
!	







honors (not AP®) Details

Big Ideas

Frequencies of Music Notes

The frequencies that correspond with the pitches of the Western equal temperament scale are:

pitch		frequency (Hz)	pitch	frequency (Hz)
ţ.	A	440.0	E E	659.3
;	В	493.9	F	698.5
\$	С	523.3	G	784.0
;	D	587.3		880.0

A note that is an octave above another note has exactly twice the frequency of the lower note. For example, the A on the second line of the treble clef staff has a frequency of 440 Hz.^{*} The A one octave above it (one ledger line above the staff) has a frequency of $440 \times 2 = 880$ Hz.

Harmonic Series

<u>harmonic series</u>: the additional, shorter standing waves that are generated by a vibrating string or column of air that correspond with integer numbers of half-waves.

<u>fundamental frequency</u>: the natural resonant frequency of a particular pitch.

<u>harmonic</u>: a resonant frequency produced by vibrations that contain an integer number of half-waves that add up to the half-wavelength of the fundamental.

The harmonics are numbered based on their pitch relative to the fundamental frequency. The harmonic that is closest in pitch is the 1^{st} harmonic, the next closest is the 2^{nd} harmonic, *etc.*

Any sound wave that is produced in a resonance chamber (such as a musical instrument) will produce the fundamental frequency plus all of the other waves of the harmonic series. The fundamental is the loudest, and each harmonic gets quieter as you go up the harmonic series.

^{*} Most bands and orchestras define the note "A" to be exactly 440 Hz, and use it for tuning.

nental frequency and the fir
>>>
\frown
ch (relative to fundamental)
ndamental.
e octave above.
e octave + a fifth above.
o octaves above.
o octaves + approximately a jor third above.
o octaves + a fifth above.
<u>a</u> e t <u>a</u> e
vo c.

honors	
(not AP®)	

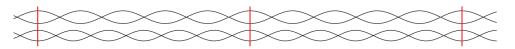
Details

Big Ideas

Beats

When two or more waves are close but not identical in frequency, their amplitudes reinforce each other at regular intervals.

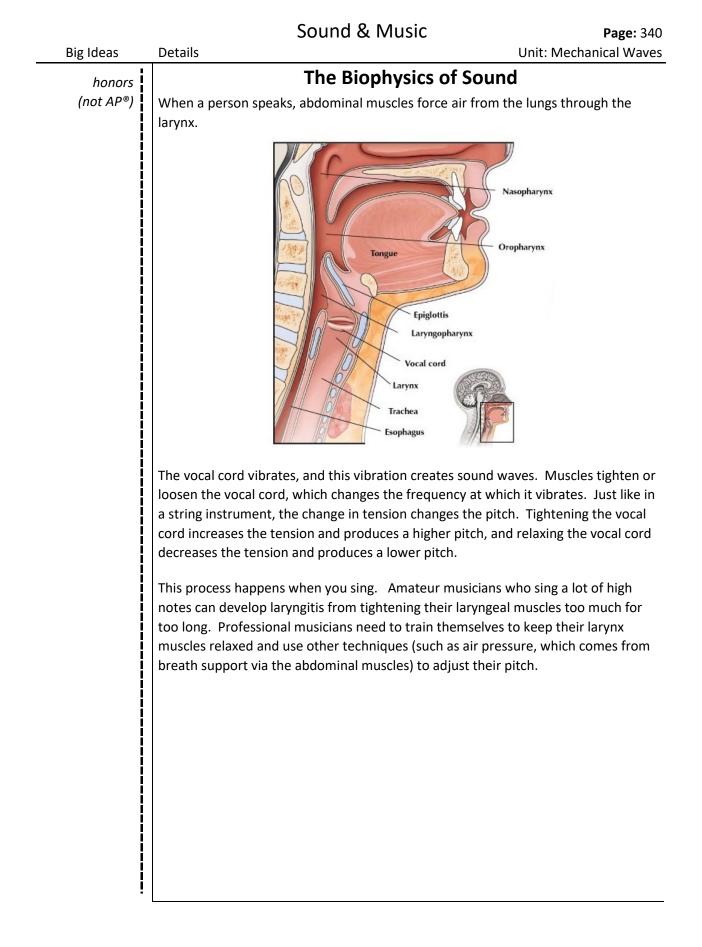
For example, when the following pair of waves travels through the same medium, the amplitudes of the two waves have maximum constructive interference every five half-waves (2½ full waves) of the top wave and every six half-waves (3 full waves) of the bottom wave.



If this happens with sound waves, you will hear a pulse or "beat" every time the two maxima coïncide.

The closer the two wavelengths (and therefore also the two frequencies) are to each other, the more half-waves it takes before the amplitudes coïncide. This means that as the frequencies get closer together, the time between the beats gets longer.

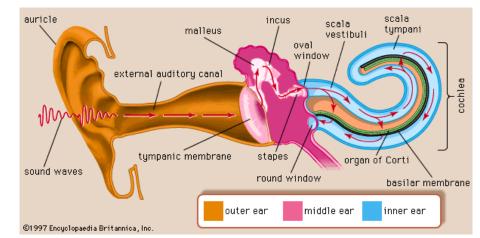
Piano tuners listen for these beats and adjust the tension of the string they are tuning until the time between beats gets longer and longer and finally disappears. Musicians in bands and orchestras use the same technique to adjust their notes until they are exactly in tune with each other.



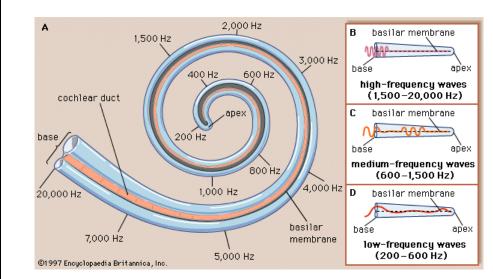
Big Ideas honors (not AP[®])

Details

When the sound reaches the ears, it travels through the auditory canal and causes the tympanic membrane (eardrum) to vibrate. The vibrations of the tympanic membrane cause pressure waves to travel through the middle ear and through the oval window into the cochlea.

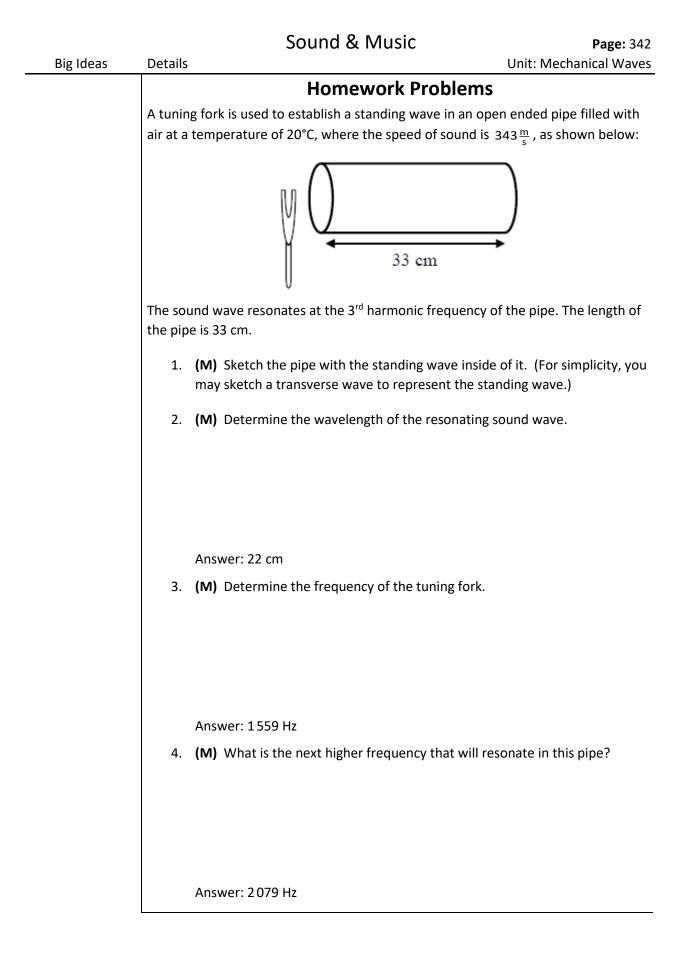


The basilar membrane in the cochlea is a membrane with cilia (small hairs) connected to it, which can detect very small movements of the membrane. As with a resonance tube, the wavelength determines exactly where the sound waves will vibrate the basilar membrane the most strongly, and the brain determines the pitch (frequency) of sounds based on the precise locations excited by these frequencies.



Long-term exposure to loud sounds destroys the cilia near the base of the basilar membrane, causing the person to lose the ability to hear high-frequency sounds. This is why younger people can hear higher frequencies than older people.

Because consonants utilize high frequencies, people who have lost the ability to hear high frequencies often have trouble distinguishing words in conversations.



Physics 2 In Plain English

Sound Level (Loudness)

Unit: Mechanical Waves

Details

Big Ideas

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): 14.1.A.6,

14.1.A.6.ii

Mastery Objective(s): (Students will be able to ...)

- Explain sound levels in decibels.
- Explain the Lombard Effect.

Success Criteria:

• Descriptions & explanations account for observed behavior.

Language Objectives:

• Explain how loudness is measured.

Tier 2 Vocabulary: level

Labs, Activities & Demonstrations:

• VU meter.

Notes:

sound level: the perceived intensity of a sound. Usually called "volume".

Sound level is measured in decibels (dB). One decibel is one tenth of one bel, but the unit bel is not used.

The decibel is defined based on the power (energy per unit time, which you should remember from Physics 1) that is carried by a sound wave:

$$L_{P} = 10\log\frac{P}{P_{o}}$$

where L_P is the loudness, *P* is the power carried by the sound wave, and P_o is the power carried by a reference wave that is defined to be zero decibels.

You will not be asked to calculate decibels from this equation, but you should understand that because the scale is logarithmic, a difference of one bel (10 dB) represents a tenfold increase or decrease in sound level.

Sound Level (Loudness)

The following table lists the approximate sound levels of various sounds:

sound level (dB)	Description
0	threshold of human hearing at 1 kHz
10	a single leaf falling to the ground
20	background in TV studio
30	quiet bedroom at night
36	whispering
40	quiet library or classroom
42	quiet voice
40–55	typical dishwasher
50–55	normal voice
60	TV from 1 m away
60	normal conversation from 1 m away
60–65	raised voice
60–80	passenger car from 10 m away
70	typical vacuum cleaner from 1 m away
75	crowded restaurant at lunchtime
72–78	loud voice
85	hearing damage (long-term exposure)
84–90	shouting
80–90	busy traffic from 10 m away
100–110	rock concert, 1 m from speaker
110	chainsaw from 1 m away
110–140	jet engine from 100 m away
120	threshold of discomfort
120	hearing damage (single exposure)
130	threshold of pain
140	jet engine from 50 m away
194	sound waves become shock waves

Big Ideas

Details

Sound Level (Loudness)

	Sound Lever (Loudness)	Page: 345
Big Ideas	Details	Unit: Mechanical Waves
honors	Adjusting Sound Level in Conversation	
(not AP®)	In crowds, people unconsciously adjust the sound levels of be heard above the ambient noise. This behavior is called named for Étienne Lombard, the French doctor who first o	the Lombard effect,
	The Lombard coëfficient is the ratio of the increase in sour the increase in sound level of the background noise:	nd level of the speaker to
	$L = \frac{\text{increase in speech level (dB)}}{\text{increase in background noise (db)}}$	1B)
	Researchers have observed values of the Lombard coëffici 1.0, depending on the circumstances.	ent ranging from 0.2 to
	When you are working in groups in a classroom, as the not person has to talk louder to be heard, which in turn makes The Lombard effect creates a feedback loop in which the s louder and louder until your teacher complains and everyo volume.	s the noise level louder. Sound gets progressively
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	Doppler Effect Page: 346
Big Ideas	Details Unit: Mechanical Waves
	Doppler Effect
	Unit: Mechanical Waves
	NGSS Standards/MA Curriculum Frameworks (2016): N/A
	AP [®] Physics 2 Learning Objectives/Essential Knowledge (2024): 14.5.A, 14.5.A.1, 14.5.A.2, 14.5.A.2.i, 14.5.A.2.ii, 14.5.A.2.iii
	Mastery Objective(s): (Students will be able to)
	• Explain the Doppler Effect and give examples.
	 Calculate the apparent shift in wavelength/frequency due to a difference in velocity between the source and receiver.
	Success Criteria:
	 Descriptions & explanations account for observed behavior.
	 Variables are correctly identified and substituted correctly into the correct equations.
	 Algebra is correct and rounding to appropriate number of significant figures is reasonable.
	Language Objectives:
	 Explain how loudness is measured.
	Tier 2 Vocabulary: shift
	Labs, Activities & Demonstrations:
	Buzzer on a string.
	Notes:
	Doppler effect or Doppler shift: the apparent change in frequency/wavelength of a wave due to a difference in velocity between the source of the wave and the observer. The effect is named for the Austrian physicist Christian Doppler.
	You have probably noticed the Doppler effect when an emergency vehicle with a siren drives by.
	HERE COMES NALKING TRAT OF HERS OF HER

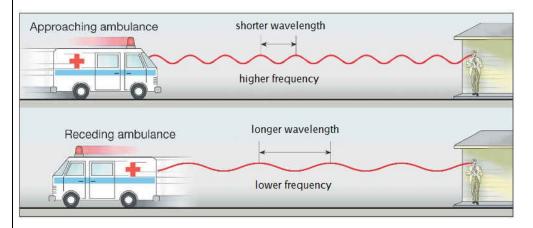
Details

Big Ideas

The Doppler shift occurs because a wave is created by a series of pulses at regular intervals, and the wave moves at a particular speed.

If the source is approaching, each pulse arrives sooner than it would have if the source had been stationary. Because frequency is the number of pulses that arrive in one second, the moving source results in an increase in the frequency observed by the receiver.

Similarly, if the source is moving away from the observer, each pulse arrives later, and the observed frequency is lower.



Pig Idoas	Details	Doppler Effect	Page: 348 Unit: Mechanical Waves
Big Ideas	Details	Calculating the Doppler S	
honors (not AP®)	The change in fre	equency is given by the equation:	
		$f = f_o \left(\frac{\mathbf{v}_w \pm \mathbf{v}_r}{\mathbf{v}_w \pm \mathbf{v}_s} \right)$	
	where:		
	f_{\circ} = freque	red frequency ncy of the original wave y of the wave	
		y of the receiver (you)	
	v _s = velocit	y of the source	
	The rule for addi	ing or subtracting velocities is:	
	the soun higher.	viver's (your) velocity is in the numerator. In a source the pulses arrive sooner, wh So if you are moving toward the sound, ad away from the sound, subtract your veloci	ich makes the frequency d your velocity. If you are
	you, this to be sm	rce's velocity is in the denominator. If the some makes the frequency higher, which means naller. This means that if the source is mov ity. If the source is moving away from you	s the denominator needs ing toward you, subtract
	reason through t higher, that mea smaller. If it wou	norize a rule for this—you will just confuse the equation. If something that's moving w ins you need to make the numerator larger uld make the frequency lower, that means ler or the denominator larger.	vould make the frequency or the denominator
AP [®] only	Note that the AP effect; you will n	Physics exam requires only a qualitative ot be required to calculate Doppler shifts.	treatment of the Doppler

Doppler Effect

	Doppler Effect	Page: 349
Big Ideas	Details	Unit: Mechanical Waves
honors	Sample Problem:	
(not AP®)	Q: The horn on a fire truck sounds at a pitch of 350 Hz. frequency when the fire truck is moving toward you a	
	perceived frequency when the fire truck is moving av	vay from you at $20\frac{m}{2}$?
	Assume the speed of sound in air is $343\frac{m}{s}$.	5
	A: The observer is not moving, so $v_r = 0$.	
	The fire truck is the source, so its velocity appears in	the denominator.
	When the fire truck is moving toward you, that make This means we need to make the denominator smalle <i>subtract</i> v _s :	
	$f = f_o \left(\frac{v_w}{v_w - v_s} \right) = 350 \left(\frac{343}{343 - 20} \right) = 350($	1.062) = 372 Hz
	When the fire truck is moving away, the frequency w we need to make the denominator larger. This mear	
	$f = f_o \left(\frac{v_w}{v_w + v_s} \right) = 350 \left(\frac{343}{343 + 20} \right) = 350(0)$).9449) = 331 Hz
	Note that the pitch shift in each direction correspond on the musical scale.	ls with about one half-step
ļ		

honors (not AP®)

Big Ideas

Exceeding the Speed of Sound

Unit: Mechanical Waves

Details

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): N/A

Mastery Objective(s): (Students will be able to...)

- Explain what a "sonic boom" is.
- Calculate Mach numbers.

Success Criteria:

- Explanations account for observed behavior.
- Variables are correctly identified and substituted correctly into the correct equations.
- Algebra is correct and rounding to appropriate number of significant figures is reasonable.

Language Objectives:

- Explain how a sonic boom is produced.
- Tier 2 Vocabulary: sonic boom

Labs, Activities & Demonstrations:

• Crack a bullwhip.

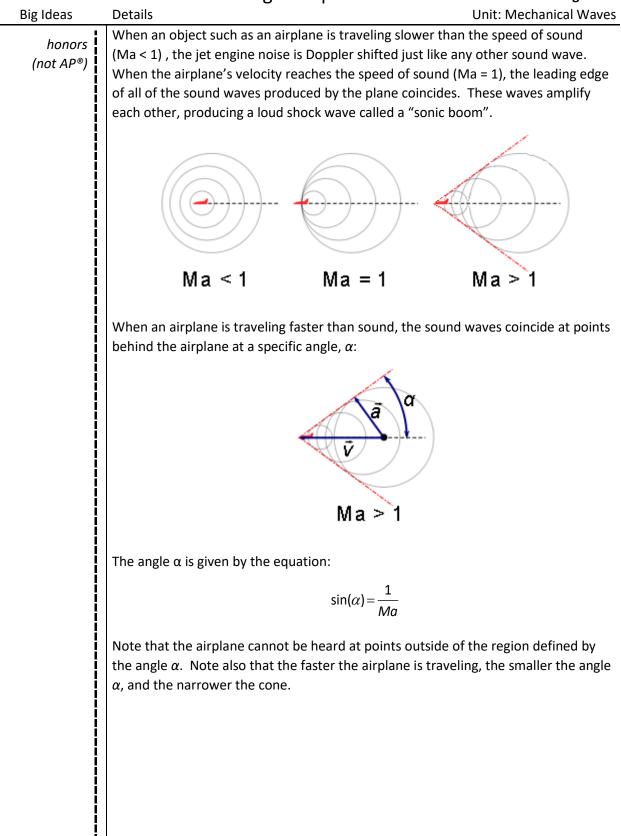
Notes:

The speed of an object relative to the speed of sound in the same medium is called the Mach number (abbreviation Ma), named after the Austrian physicist Ernst Mach.

$$Ma = \frac{v_{object}}{v_{sound}}$$

Thus "Mach 1" or a speed of Ma = 1 is the speed of sound. An object such as an airplane that is moving at 1.5 times the speed of sound would be traveling at "Mach 1.5" or Ma = 1.5.

Exceeding the Speed of Sound



I

Exceeding the Speed of Sound

Big Ideas Details Unit: Mechanical Wave honors The shock wave temporarily increases the temperature of the air affected by it. If the air is humid enough, when it cools by returning to its normal pressure, the wate vapor condenses and forms a cloud, called a vapor cone:	
<i>nonors</i> $(not AP^{\otimes})$ the air is humid enough, when it cools by returning to its normal pressure, the wate	/es
	ter
The "crack" of a bullwhip is also a sonic boom—when a bullwhip is snapped sharply the end of the bullwhip travels faster than sound and creates a miniature shock wave.	у,

Big Ideas	Details Unit: Light & Optics
	Introduction: Light & Optics
	Unit: Light & Optics
	Topics covered in this chapter:
	Electromagnetic Waves
	Color
	Reflection
	Mirrors
	Refraction
	Polarization
	Lenses
	Diffraction413
	Scattering419
	This chapter discusses the behavior and our perception of light.
	• <i>Electromagnetic Waves</i> discusses properties and equations that are specific to electromagnetic waves (including light).
	 Color discusses properties of visible light and how we perceive it.
	• <i>Reflection</i> and <i>Mirrors</i> discuss properties of flat and curved mirrors and steps for drawing ray tracing diagrams.
	 Refraction and Lenses discuss properties of convex and concave lenses and steps for drawing ray tracing diagrams.
	 Polarization, Diffraction, and Scattering discuss specific optical properties of light.
	One of the new skills learned in this chapter is visualizing and drawing representations of how light is affected as it is reflected off a mirror or refracted by a lens. This can be challenging because the behavior of the light rays and the size and location of the image changes depending on the location of the object relative to the focal point of the mirror or lens. Another challenge is drawing precise, to-scale ray tracing drawings such that you can use the drawings to accurately determine properties of the image, or of the mirror or lens.

	Introduction: Light & Optics	Page: 354
Big Ideas	Details	Unit: Light & Optics
	Standards addressed in this chapter:	
	Massachusetts Curriculum Frameworks (2016):	
	HS-PS4-5. Communicate technical information about how devices use the principles of wave behavior and wave matter to transmit and capture information and energy.	e interactions with
AP [®] only	AP [®] Physics 2 Learning Objectives/Essential Knowledge (2	024):
, only	13.1.A : Describe light as a ray.	
	13.1.A.1 : A light ray is a straight line that is perpendicul a light wave and points in the direction of travel of the	
	13.1.A.1.i: Light rays can be used to determine the be geometric optics, where the wave nature of light	-
	13.1.A.1.ii: Rays are not sufficient to understand the interference and diffraction, the wave nature of to the second	
	13.1.A.1.iii: A laser is a common source of a single co beam of light that can be modeled as a ray.	herent, monochromatic
	13.1.A.2: Ray diagrams depict the path of light before a with matter.	and after an interaction
	13.1.B : Describe the reflection of light from a surface.	
	13.1.B.1 : Light that is incident on a surface can be refle	cted.
	13.1.B.2: The law of reflection states that the angle bet and the normal (the line perpendicular to the surfa between the reflected ray and the normal.	•
	13.1.B.3: Diffuse reflection is the reflection of light from results in light reflected in many different direction normal to the surface varies over the area over who	s, because the line
	13.1.B.4: Specular reflection is the reflection of light from and results in light uniformly reflected from the sur normal to the surface has an approximately consta area the light strikes.	om a smooth surface face, because the line
	13.2.A : Describe the image formed by a mirror.	
	13.2.A.1: Incident light rays parallel to the principal axis (converging) mirror will be reflected toward a comi focal point.	
	13.2.A.2: Incident light rays parallel to the principal axis mirror will be reflected such that they appear to ha common location behind the mirror, called the foca	ve originated from a
	13.2.A.3 : The focal point of a plane mirror is an infinite mirror.	distance from the
	mirror.	

Big Ideas	Details Unit: Light & Optics
AP® only	13.2.A.4 : The focal point of a spherical mirror may be approximated as a point
	located on the principal axis of the mirror halfway between the surface of
	the mirror and the center of the mirror's radius of curvature.
	13.2.A.5 : A real image is formed by a mirror when light rays emanating from a common point are reflected and then intersect at a common point.
	13.2.A.6 : A virtual image is formed by a mirror when reflected light rays diverge such that they appear to have originated from a common point.
	13.2.A.7 : The location of an image depends on the focal length of the mirror and the distance between the object and the surface of the mirror.
	13.2.A.7.i: The locations of a mirror's focal point, an object near the mirror, and the image of the object formed by the mirror follow sign conventions that are used to determine those locations relative to the mirror itself.
	13.2.A.7.ii : The distance between the image formed and a plane mirror is equal to the distance between the object and the plane mirror.
	13.2.A.8: The magnification of an image formed by a mirror is the ratio of the size of the image produced to the size of the object itself and depends on the locations of the object and image relative to the mirror.
	13.2.A.9 : Ray diagrams can be used to determine the location, type, size, and orientation of images formed by mirrors.
	13.2.A.9.i : The three principal rays are typically used to find the images formed by mirrors. The principal rays are 1) the ray parallel to the principal axis, 2) the ray that reflects at the center of the mirror where the principal axis intersects the mirror, and 3) the ray that passes through the focal point of the mirror.
	13.2.A.9.ii : Images formed by a mirror can be upright or inverted, virtual or real, and reduced, enlarged, or the same size as the object.
	13.3.A : Describe the refraction of light between two media.
	13.3.A.1 : Refraction is the change in direction of a light ray as the ray passes from one medium into another.
	13.3.A.2 : Refraction is a result of the speed of light changing when light enters a new medium.
	13.3.A.3 : The index of refraction of a given medium is inversely proportional to the speed of light in the medium.
	13.3.A.4 : Snell's law relates the angles of incidence and refraction of a light ray passing from one medium into another to the indices of refraction of the two media.
	13.3.A.4.i : When a light ray travels from a medium with a higher index of refraction into a medium with a lower index of refraction, the ray refracts away from the normal.

Big Ideas	Details		Unit: Light & Optics
AP® only	13	3.3.A.4.ii: When a light ray travels from a medium wit refraction into a medium with a higher index of refracts toward the normal.	
	13	3.3.A.4.iii: When a light ray is incident along the norm transmitted ray is not refracted.	al to a surface, the
		3.A.5 : Total internal reflection may occur when light p medium into another medium with a lower index of r	
	13	3.3.A.5.i: Total internal reflection of light occurs beyon incidence.	nd a critical angle of
	13	3.3.A.5.ii : For incident rays at the critical angle, the ra degrees and travels along the surface of the materi	
	13	3.3.A.5.iii : For incident rays beyond the critical angle, (no light is transmitted into the other medium).	all light is reflected
	13.4.4	A: Describe the image formed by a lens.	
	13.4	I.A.1 : Incident light rays parallel to the principal axis of (converging) lens will be refracted and converge towa location on the transmitted side of the lens, called th	ard a common
		I.A.2 : Incident light rays parallel to the principal axis c (diverging) lens will be refracted and diverge as if the focal point on the incident side of the lens.	
		I.A.3: A real image is formed by a lens when light rays common point are refracted such that they intersect point.	
		I.A.4: A virtual image is formed by a lens when refract such that they appear to have originated from a complexity of the second such that they appear to have originated from a complexity of the second such that they appear to have originated from a complexity of the second such that the second such	
		I.A.5 : For a thin lens, the location of an image depend of the lens and the distance between the object and lens, as given by the thin-lens equation.	-
	13	3.4.A.5.i : The locations of a lens's focal point, an object the object formed by the lens follow sign convention determine those locations relative to the lens itself	ons that are used to
	13	3.4.A.5.ii: Lenses have a focal point on both sides of the on the shape of the respective side of the lens.	e lens that depends
	13.4	I.A.6: For a thin lens, the magnification of an image is of the image produced to the size of the object itself locations of the object and image relative to the lens.	and depends on the
	13.4	I.A.7: Ray diagrams can be used to determine the loca orientation of images formed by lenses.	ation, type, size, and
	13.4		ition, type, size, and

Big Ideas	Details	Unit: Light & Optics
AP® only		13.4.A.7.i: The three principal rays are typically used to find the images formed by lenses. The principal rays are 1) the ray parallel to the principal axis, 2) the ray that passes through the center of the lens where the principal axis intersects the lens, and 3) the ray that passes through the focal point of the lens.
	1	I.3.4.A.7.ii: Images formed by a lens can be upright or inverted, virtual or real, and reduced, enlarged, or the same size as the object.
	14.4.	A: Describe the properties of an electromagnetic wave.
	14.	4.A.1 : Electromagnetic waves consist of oscillating electric and magnetic fields that are mutually perpendicular.
	1	I4.4.A.1.i: Electromagnetic waves are transverse waves because the oscillations of the electric and magnetic fields are perpendicular to the direction of propagation.
	1	I.4.4.A.1.ii: Electromagnetic waves are commonly assumed to be plane waves, which are characterized by planar wave fronts.
	14.	.4.A.2 : Electromagnetic waves do not need a medium through which to propagate.
	14.	.4.A.3: Categories of electromagnetic waves are characterized by their wavelengths.
	1	L4.4.A.3.i: Categories of electromagnetic waves include (in order of decreasing wavelength, spanning a range from kilometers to picometers) radio waves, microwaves, infrared, visible, ultraviolet, X- rays, and gamma rays.
	1	L4.4.A.3.ii: Visible electromagnetic waves are further broken into categories of color, including (in order of decreasing wavelength) red, orange, yellow, green, blue, and violet.
		L4.4.A.3.iii: Visible electromagnetic waves are also called light. Sometimes, electromagnetic waves of all wavelengths are collectively referred to as light or electromagnetic radiation.
	Skills le	arned & applied in this chapter:
	• Dra	awing ray diagrams from mirrors and through lenses.

Details

Big Ideas

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS4-1, HS-PS4-3, HS-PS4-5

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): 14.1.A, 14.1.A.3.i, 14.2.A, 14.2.A.1.iv, 14.4.A, 14.4.A.1, 14.4.A.1.i, 14.4.A.1.ii, 14.4.A.2, 14.4.A.3,

14.4.A.3.i, 14.4.A.3.ii, 14.4.A.3ii

Mastery Objective(s): (Students will be able to...)

• Describe the regions of the electromagnetic spectrum.

Success Criteria:

• Descriptions & explanations account for observed behavior.

Language Objectives:

- Explain why ultraviolet waves are more dangerous than infrared.
- Tier 2 Vocabulary: wave, light, spectrum

Labs, Activities & Demonstrations:

- red vs. green vs. blue lasers on phosphorescent surface
- blue laser & tonic water
- wintergreen Life Savers[™] (triboluminescence)

Notes:

<u>electromagnetic wave</u>: a transverse, traveling wave that is caused by oscillating electric and magnetic fields.

Electromagnetic waves travel through space and do not require a medium.

The electric field creates a magnetic field, which is perpendicular to it. This magnetic field creates a perpendicular electric field, which creates another magnetic field, and so on. The repulsion between these induced fields causes the wave to propagate. Direction of propagation Electric Field Magnetic Field

Electromagnetic Waves

Electromagnetic waves (such as light, radio waves, *etc.*) travel at a constant speed, which is determined by the rate at which the electric and magnetic fields create each other. These rates are determined by the electric permittivity (ε) and magnetic permeability (μ) of the medium, which means the speed of light is different in different mediums. (See *Electric Permittivity* on page 159 and *Magnetic Permeability* on page 283. The speed of light in different mediums will be discussed further in the section on *Refraction*, starting on page 384.)

In a vacuum, the speed of light is:

Big Ideas

Details

$$c = \frac{1}{\sqrt{\mu_o \varepsilon_o}} \approx 3.00 \times 10^8 \, \frac{\text{m}}{\text{s}} \approx 186\,000\,\frac{\text{mi.}}{\text{s}} \approx 1\frac{\text{ft.}}{\text{ns}}$$

The variable *c* is used instead of *v*, to indicate that the speed of light is constant for a given medium.

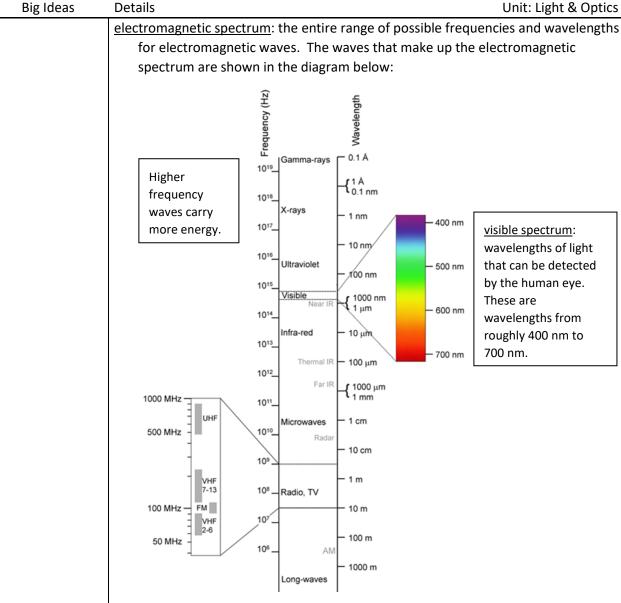
Recall that the speed of a wave equals its frequency times its wavelength:

 $c = \lambda f$

plane wave: a wave whose value at any moment is the same through any plane that

is perpendicular to the direction of propagation. Electromagnetic waves can be considered to be plane waves, which means that an electromagnetic wave consists of an infinite number of transverse waves, at every possible angle perpendicular to the direction of propagation.

Electromagnetic Waves



The energy (E) that a wave carries is proportional to the frequency. (Think of it as the number of bursts of energy that travel through the wave every second.) For electromagnetic waves (including light), the constant of proportionality is Planck's constant (named after the physicist Max Planck), which is denoted by a script h in equations.

The energy of a wave is given by the Planck-Einstein equation:

$$E = hf = \frac{hc}{\lambda}$$

where *E* is the energy of the wave in Joules, *f* is the frequency in Hz, *h* is Planck's constant, which is equal to 6.626×10^{-34} J·s, *c* is the speed of light, and λ is the wavelength in meters.

Antennas

Details

Big Ideas

An antenna is a piece of metal that is affected by electromagnetic waves and is used to amplify waves of specific wavelengths. The optimum length for an antenna is either the desired wavelength, or some fraction of the wavelength such that one wave is an exact multiple of the length of the antenna. (*E.g.*, good lengths for an antenna could be $\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{8}$, *etc.* of the wavelength.)

Sample problem:

Q: What is the wavelength of a radio station that broadcasts at 98.5 MHz?

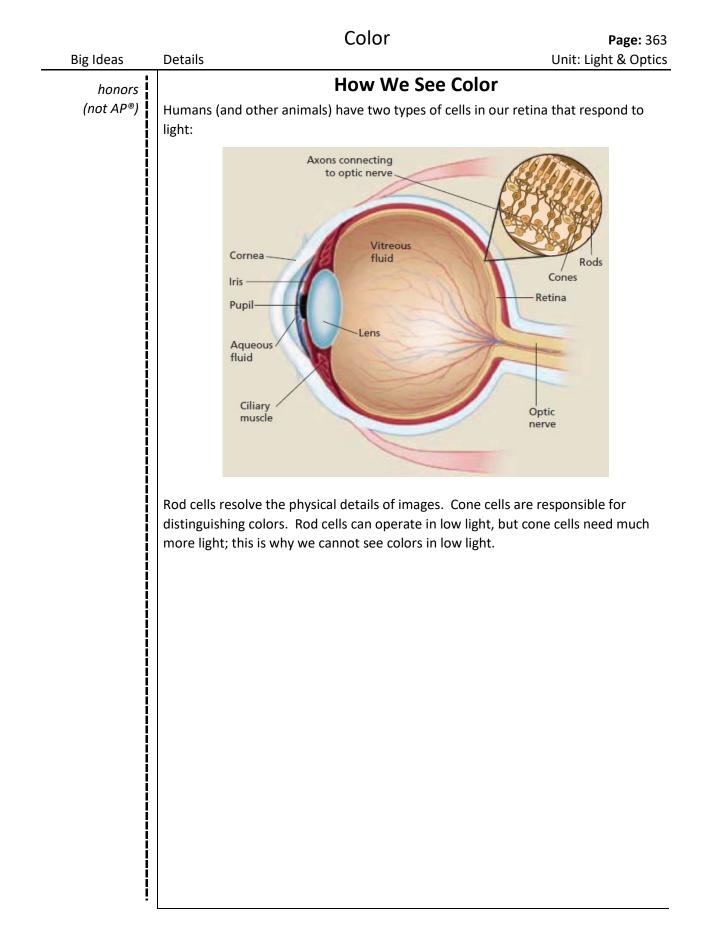
A:
$$c = \lambda f$$

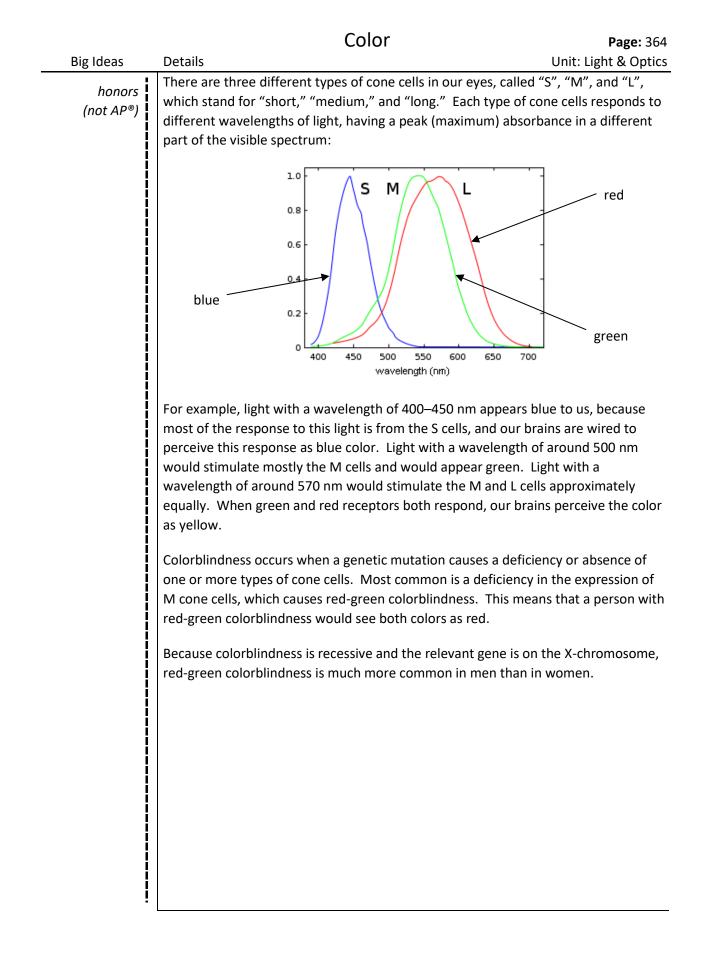
 $3.00 \times 10^8 = \lambda (9.85 \times 10^7)$
 $\lambda = \frac{3.00 \times 10^8}{9.85 \times 10^7} = 3.05 \,\mathrm{m}$

- Q: What would be a good length for an antenna that might be used to receive this radio station?
- A: 3.05 m (about 10 feet) is too long to be practical for an antenna. Somewhere between half a meter and a meter is a good size.
 - $\frac{1}{4}$ wave would be 0.76 m (76 cm), which would be a good choice.

Big Ideas	Details		Unit: Light & Optio
honors		Color	
(not AP®)	Unit: Light & Optics		
i	NGSS Standards/MA	A Curriculum Frameworks (201	L 6): N/A
ļ	AP [®] Physics 2 Learn	ing Objectives/Essential Know	ledge (2024): 14.4.A.3.ii
ļ	Mastery Objective(s	s): (Students will be able to)	
ļ	• Explain how co	olors are produced and mixed.	
	 Explain why w 	e see colors the way we do.	
İ	Success Criteria:		
-	Descriptions 8	explanations account for obse	erved behavior.
İ	Language Objective	5:	
ļ	• Explain how so	omeone who is red-green color	r blind might see a green object.
ļ	Tier 2 Vocabulary: o	color, mixing	
	Labs. Activities &	Demonstrations:	
ļ	 colored light b 		
İ			
ļ	Notes:		
ļ		es/wavelengths in the part of the second s	he spectrum that the eye can
ļ	detect is called <u>visib</u>	<u>le light</u> .	
İ	color: the perception	n by the human eye of how a li	ght wave appears, based on its
ļ	wavelength/free	juency.	
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Color





	Color	Page: 365
Big Ideas	Details	Unit: Light & Optics
honors	Direct Light: Additive N	lixing
(not AP®)	Because our cone cells respond to red, green, and blue light, we call these colors the primary colors of light. Other colors can be made by mixing different amounts of these colors, thereby stimulating the different types of cone cells to different degrees. When all colors are mixed, the light appears white. <u>primary color</u> : light that excites only one type of cone cell. The primary colors of light are red,	Yellow Green Red Cyan Blue Magenta
	green, and blue.	Additive (light)
	secondary color: light that is a combination of exactly to secondary colors of light are cyan, magenta, and yel	wo primary colors. The
	Reflected Light: Subtractiv	e Mixing
	 When light shines on an object, properties of that object cause it to absorb certain wavelengths of light and reflect others. The wavelengths that are reflected are the ones that make it to our eyes, causing the object to appear that color. <u>pigment</u>: a material that changes the color of reflected light by absorbing light with specific wavelengths. <u>primary pigment</u>: a material that absorbs light of only one primary color (and reflects the other two prima pigments are cyan, magenta, and yellow. Note that colors of light. <u>secondary pigment</u>: a pigment that absorbs two primar other). The secondary pigments are red, green, and the primary colors of light. 	these are the secondary ry colors (and reflects the

	Cc	blor	Page: 366
Big Ideas	Details		Unit: Light & Optics
Big Ideas honors (not AP®)		r is biological, so mixing primate ed average of positions on the	ry colors is not a color wheel. The
	fraction (from $0 - 1$) of red light, the <i>y</i> -axis is the fraction of green light, and the fraction of blue is implicit [1 - (red + green)]. Notice that equal fractions (0.33) of red, green and blue light would produce white light.	02 Greenish tive	Pink Red Purplish Purple 0.5 0.6 0.7 0.8
	To show the effects of mixing two connect them with a line. The line effects of mixing. (<i>E.g.</i> , the midpo each of the source colors.) This m the mixtures of different compou	ear distance along that line sho pint would represent the color nethod is how fireworks manu	ows the proportional generated by 50% of facturers determine

-	Details Unit: Light & Optics
	Reflection
	Unit: Light & Optics
	NGSS Standards/MA Curriculum Frameworks (2016): N/A
	AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 13.1.A, 13.1.A.1, 13.1.A.1.i, 13.1.A.1.ii, 13.1.A.1.iii, 13.1.B, 13.1.B, 13.1.B.1, 13.1.B.2, 13.1.B.3, 13.1.B.4
	Mastery Objective(s): (Students will be able to)
	• Explain why light is reflected off smooth surfaces. Success Criteria:
	• Descriptions & explanations account for observed behavior. Language Objectives:
	• Explain why light is reflected off smooth surfaces.
	Tier 2 Vocabulary: light, reflection, virtual image, real image
	Labs, Activities & Demonstrations:
	 full length mirror on the wall (does amount of image visible change with distance?)
	Mirascope ("hologram maker")
	Notes:
	reflection: when a wave "bounces" off an object and changes direction.
	specular reflection: reflection from a smooth surface.
	diffuse reflection: reflection from a rough surface.
	 <u>virtual image</u>: a perceived image that appears to be the point of origin of photons (rays of light) that diverge. Because light is reflected back from a mirror (<i>i.e.,</i> light cannot pass through it), a <i>virtual image</i> is one that appears <i>behind</i> (or "inside") <i>the mirror</i>. A virtual image is what you are used to seeing in a mirror.
	 <u>real image</u>: a reflected image that is created by photons (rays of light) that converge. Because light is reflected back from a mirror (<i>i.e.,</i> light cannot pass through it), a <i>real image</i> is one that appears <i>in front of the mirror</i>. A real image created by a mirror looks like a hologram.
	A rule of thumb that works for both mirrors and lenses is that a real image is produced by the convergence of actual rays of light. A virtual image is our

5	Reflectio	6
Big Ideas	Details Specular reflection: reflection from a smooth surface, such as a mirror. If the photons of light from the source are parallel when they strike the surface, they will also be parallel when they reflect from the surface. This results in a reflected image that appears to be the same size, sh original object.	Unit: Light & Optics Specular Reflection
	 <u>Diffuse reflection</u> : reflection from a rough surface, such as a wall. Light striking a rough surface will illuminate the surface. However, because the reflected light rays are not parallel, the reflected light does not create a reflected image of the object. <u>mirror:</u> a surface that causes specular read mirror but behaves like one is often a mirror but behaves like one is often. 	eflection. An object that was not made to be

Reflection

	Reflect	Page: 369	
<u>Big Ideas</u>	Details When light waves strike a mirrored surface at an angle (measured from the perpendicular or "normal" direction), they are reflected at the same angle away from the perpendicular. The most common statement of this concept is "The angle of incidence equals the angle of reflection." This can be stated mathematically as either $\theta = \theta'$ or $\theta_i = \theta_r$.	incident light angle of incidence normal angle of reflection reflected light	Unit: Light & Optics

	Mirrors	Page: 37
g Ideas	Details	Unit: Light & Option
	Mirrors	
	Unit: Light & Optics	
	NGSS Standards/MA Curriculum Frameworks (2016): N/A	
	AP® Physics 2 Learning Objectives/Essential Knowledge (2024) 13.2.A.2, 13.2.A.3, 13.2.A.4, 13.2.A.5, 13.2.A.6, 13.2.A.7, 2 13.2.A.8, 13.2.A.9, 13.2.A.9.i, 13.2.A.9.ii	
	Mastery Objective(s): (Students will be able to)	
	 Draw ray tracing diagrams for reflection from flat and cur mirrors. 	ved (spherical)
	 Numerically calculate the distance from the mirror to its f to the image. 	ocus and the mirro
	Success Criteria:	
	 Ray diagrams correctly show location of object, focus and 	image.
	 Calculations are correct with correct algebra. 	
	Language Objectives:	
	• Explain when and why images are inverted (upside-down) <i>vs.</i> upright.
	Tier 2 Vocabulary: light, reflection, virtual image, real image, m	nirror, focus
	Labs, Activities & Demonstrations:	
	Mirascope	
	 turn a glove inside-out 	
	Notes:	
	<u>mirror</u> : a surface that light rays reflect from at the same angle t	he light rays came
	from.	
	<u>convex</u> : an object that curves outward.	
	<u>concave</u> : an object that curves inward.	
	flat: an object that is neither convex nor concave.	
	<u>ray</u> : a beam of light. Rays travel in a straight line unless they are reflection or refraction.	e redirected by
	<u>laser</u> : a beam of coherent light that travels in a straight line with Laser light is spatially coherent, meaning that it can be focu not spread out, and also temporally coherent, meaning that narrow frequency spectrum. (We often describe lasers as e single frequency.)	sed tightly and does t the light is of a ver

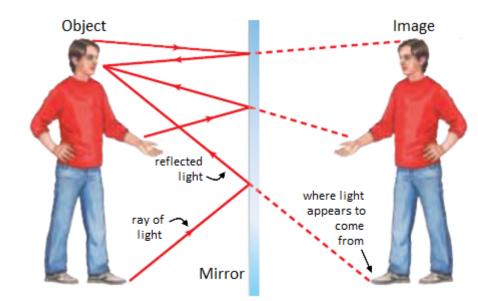
	Mirrors	Page: 371
Big Ideas		Unit: Light & Optics
	"Laser" is an acronym for "Light Amplification by Stimulated E Radiation". The first laser was built in 1960 by Theodore Main	
	focal point: the point at which parallel rays striking a mirror conve	erge.
	principal axis: a line perpendicular to a mirror (<i>i.e.,</i> with an angle such that a ray of light is reflected back along its incident (income	
	The principal axis is often shown as a single horizontal line, bu mirror has a principal axis.	ut every point on a

Big Ideas

Flat Mirrors

Details

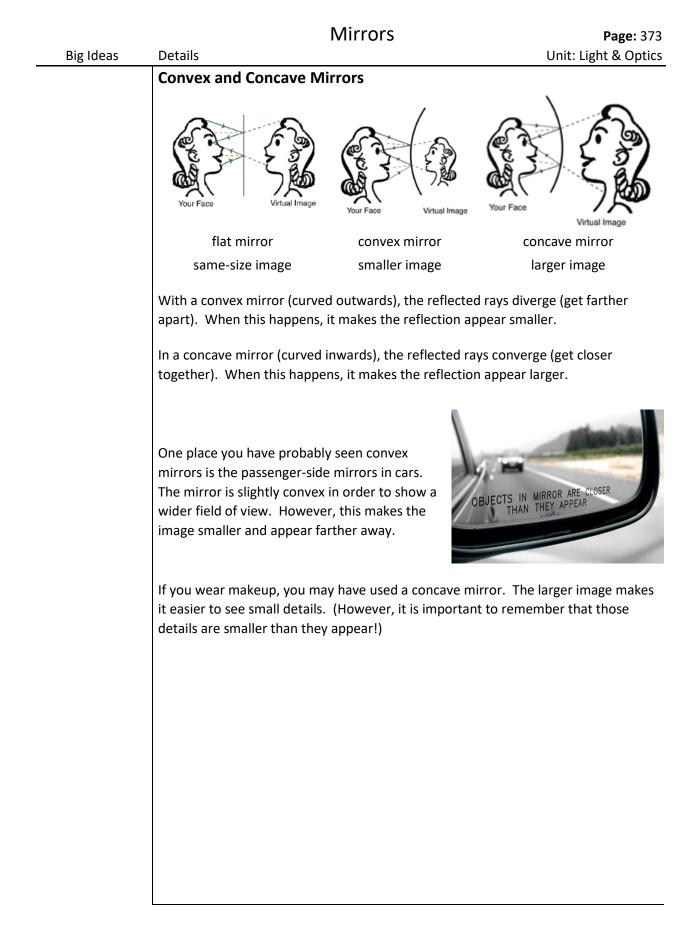
With a flat mirror, the light reflected off the object (such as the person in the picture below) bounces off the mirror and is reflected back. Because our eyes and the part of our brains that decode visual images can't tell that the light has been reflected, we "see" the reflection of the object in the mirror.

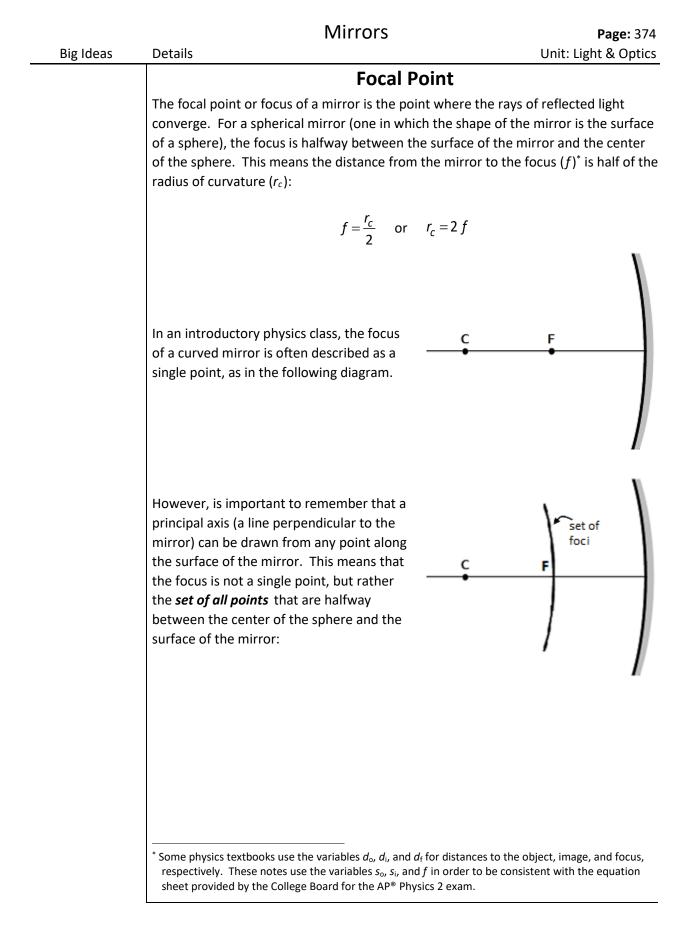


If the mirror is flat, the reflection is the same size and the same distance from the mirror as the actual object. However, the image looks like it is reversed horizontally, but not vertically.

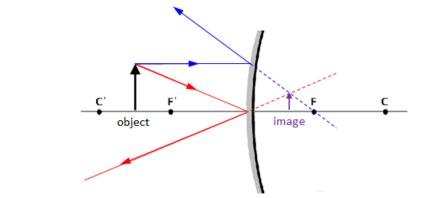
It would seem that the mirror "knows" to reverse the image horizontally but not vertically. (Of course this is not true. If you want the mirror to reverse the image vertically, all you need to do is put the mirror on the floor.) What is actually happening is that light is reflected straight back from the mirror. Anything that is on your right will also be on the right side of the image (from your point of view; if the image were actually a person, this would be the other person's left). Anything that is on top of you will also be on top of the image as you look at it.

What the mirror is doing is the same transformation as flipping a polygon over the *y*-axis. *The reversal is actually front-to-back* (where "front" means closer to the mirror and "back" means farther away from it).





		Mirrors	Page: 375
Big Ideas	Details		Unit: Light & Optics
	-	Ray Tracin of finding the location, size and) the rays of light to see where t	orientation of an image in a mirror
	the princ the same principal relative t	light that hits the mirror on cipal axis is reflected back at e angle relative to that axis. (The angle of incidence to the principal axis equals e of reflection.)	C F
	parallel t reflected	light that hits the mirror to the principal axis is I directly toward or away e focal point of the mirror (the	C F
	-	aw a pair of rays from the top o e, the intersection will be at the	f the object as described by #1 and top of the image of the object.
	strikes the mirro	r parallel to the principal axis (fr eflected through the focus (also	oal axis (step 1 above), the ray that om step 2 above) , and that same from step 2 above)—are called the
	Convex Mirro For a convex mir smaller than the	ror, the image is always virtual (behind the mirror) and is always



	101111013	Page: 376
Big Ideas	Details	Unit: Light & Optics
	Concave Mirrors	
	For a concave mirror, what happens with the image chan the object is relative to the center of curvature and the for tracing in each the following cases.	
	 If the object is closer to the mirror than the focus, you see a virtual image (behind the mirror) that is upright (right-side-up), and larger than the original. 	object image
	 If the object is at the focus, there is no image because the rays do not converge. 	object C F
	 3. If the object is between the focus and the center of curvature, you see a real image (in front of the mirror) that is behind the object, inverted (upside-down), and larger. 	object

		Mirrors	Page: 377
Big Ideas	Details		Unit: Light & Optics
	you see a real, i	at the center of curvature, nverted image that is the ame distance from the pject.	object C F image
	than the center real, inverted in	arther from the mirror of curvature, you see a nage that is smaller and rror than the object.	object
		Equations	ľ
			e calculated from the distance to sing the following equation:
		$\frac{1}{s_o} + \frac{1}{s_i} = \frac{1}{f}$	
	_		ve in front of the mirror (where a ror (where a virtual image would
		(h_i) can be calculated from d s_o), using the following equivalence of the following equivalence of the second seco	the height of the object (<i>h</i> _o) and quation:
		$M = \frac{h_i}{h_o} = -\frac{s_i}{s_o}$	
		0 0	right-side-up), and a negative own).
	magnification: the ratio	o of the size of the image to	the size of the object.

2 0 000	
Sample	Problem:

Details

Big Ideas

- Q: An object that is 5 cm high is placed 9 cm in front of a spherical convex mirror. The radius of curvature of the mirror is 10 cm. Find the height of the image and its distance from the mirror. State whether the image is real or virtual, and upright or inverted.
- A: The mirror is convex, which means the focus is behind the mirror. This is the side where a **virtual** image would be, so the distance to the focus is therefore negative. The distance to the focus is half the radius of curvature, which means f = -5 cm. From this information, we can find the distance from the mirror to the image (s_i):

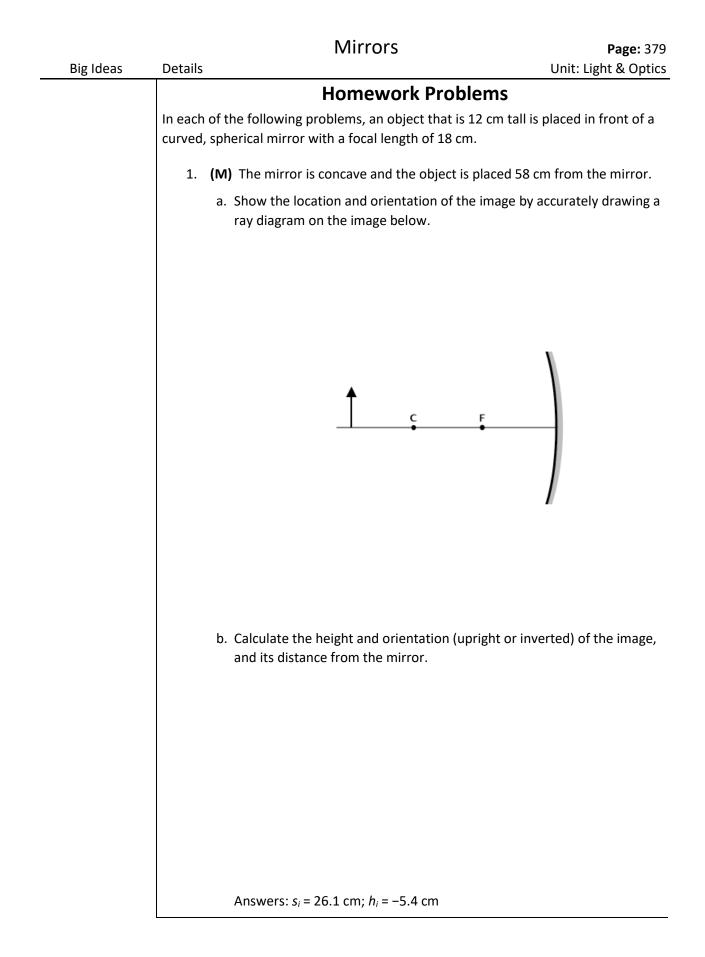
$\frac{1}{1} + \frac{1}{1} = \frac{1}{1}$	
$s_o s_i f$	1 - 14
$\frac{1}{1+1} = \frac{1}{1}$	s _i 45
$\frac{1}{9} + \frac{1}{s_i} = \frac{1}{-5}$	$s_i = -\frac{45}{14} = -3.2 \mathrm{cm}$
$\frac{5}{1} + \frac{1}{1} = -\frac{9}{1}$	$\frac{3_i}{14} = \frac{-3.2}{14}$
45 <i>s_i</i> 45	

The value of -3.2 cm means the image is a virtual image located 3.2 cm behind the mirror.

Now that we know the distance from the mirror to the image, we can calculate the height of the image (h_i) :

$$\frac{h_i}{h_o} = -\frac{s_i}{s_o}$$
(5)(3.2) = 9 h_i
$$\frac{h_i}{5} = -\frac{-3.2}{9}$$
 $h_i = \frac{16}{9} = +1.8 \text{ cm}$

The image is 1.8 cm high. Because the height is a positive number, this means the image is upright (right-side-up).



		Mirrors	Page: 380
Big Ideas	Details	(S) The mirror is concave and the object is placed	Unit: Light & Optics
	2.	a. Show the location and orientation of the ima ray diagram on the image below.	
		F.	
		b. Calculate the height and orientation of the ir the mirror.	nage, and its distance from
		Answers: $s_i = 36$ cm; $h_i = -12$ cm	

			Mirrors	Page: 381
Big Ideas	Details	(5)	The mirror is concave and the object is placed 32 cr	Unit: Light & Optics
	5.	а.	Show the location and orientation of the image by ray diagram on the image below.	
				١
			C F	
		b.	Calculate the height and orientation of the image, the mirror.	and its distance from
			Answers: <i>s</i> ^{<i>i</i>} = 41.1 cm; <i>h</i> ^{<i>i</i>} = −15.4 cm	

			Mirrors	Page: 382
Big Ideas	Details	()		Unit: Light & Optics
	4.	(M)	The mirror is concave and the object is placed 6 c	
		а.	Show the location and orientation of the image b ray diagram on the image below.	y accurately drawing a
			- C F	
		b.	Calculate the height and orientation of the image the mirror.	e, and its distance from
			Answers: $s_i = -9$ cm; $h_i = 18$ cm	

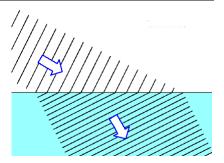
	_		Mirrors	Page: 383
Big Ideas	Details 5.	(M)	The mirror is convex and the object is placed 15 c	Unit: Light & Optics
	5.	a.	Show the location and orientation of the image b ray diagram on the image below.	
		b.	Calculate the height and orientation of the image the mirror.	c e, and its distance from
			Answers: $s_i = -8.2$ cm; $h_i = 6.5$ cm	

	Refraction	Page: 384
Big Ideas	Details	Unit: Light & Optics
	Refraction	
	Unit: Light & Optics	
	NGSS Standards/MA Curriculum Frameworks (2016): N/A	
	AP® Physics 2 Learning Objectives/Essential Knowledge (2024 13.3.A.2, 13.3.A.3, 13.3.A.4, 13.3.A.4.i, 13.3.A.4.ii, 13.3.A 13.3.A.5.i, 13.3.A.5.ii, 13.3.A.5.iii, 14.9.A, 14.9.A.1, 14.9.A 14.9.A.2.ii, 14.9.A.3, 14.9.A.4, 14.9.A.4.i, 14.9.A.4.ii, 14.9 14.9.A.5.ii, 14.9.A.5.iii	4.iii, 13.3.A.5, A.2, 14.9.A.2.i,
	Mastery Objective(s): (Students will be able to)	
	 Explain how and why refraction happens. 	
	 Solve problems using Snell's Law. 	
	Success Criteria:	
	• Explanation accounts for the size, location and orientation	on of the image.
	Calculations are correct with correct algebra and trigono	metry.
	Language Objectives:	
	• Explain why we see the image of an object through a ma the object in its actual location.	gnifying glass but not
	Tier 2 Vocabulary: light, reflection, virtual image, real image, l	ens, focus
	Labs, Activities & Demonstrations:	
	 laser through clear plastic 	
	 laser through bent plastic (total internal reflection) 	
	 laser through falling stream of water (with 1 drop milk) 	
	Pyrex stirring rod in vegetable oil (same index of refraction	on)
	• penny in cup of water	
	Notes:	
	refraction: a change in the velocity and direction of a wave as i medium to another. The change in direction occurs becaus different velocities in the different media.	•
	index of refraction: a number that relates the velocity of light i velocity of light in a vacuum.	n a medium to the

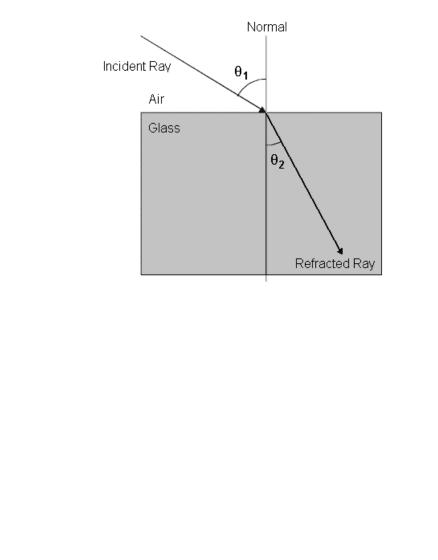
When light crosses from one medium to another, the difference in velocity of the waves causes the wave to bend. For example, in the picture below, the waves are moving faster in the upper medium. As they enter the lower medium, they slow down. Because the part of the wave that enters the medium soonest slows down first, the angle of the wave changes as it crosses the boundary.

Big Ideas

Details



When the waves slow down, they are bent toward the normal (perpendicular), as in the following diagram:



The index of refraction of a medium is the velocity of light in a vacuum divided by the velocity of light in the medium:

 $n = \frac{c}{v}$

Thus the larger the index of refraction, the more the medium slows down light as it passes through.

The index of refraction for some substances is given below.

Substance	Index of Refraction	Substance	Index of Refraction
vacuum	1.00000	quartz	1.46
air (0°C and 1 atm)	1.00029	glass (typical)	1.52
water (20°C)	1.333	NaCl (salt) crystals	1.54
acetone	1.357	polystyrene (#6 plastic)	1.55
ethyl alcohol	1.362	diamond	2.42

These values are for yellow light with a wavelength of 589 nm.

For light traveling from one medium into another, the ratio of the speeds of light is related inversely to the ratio of the indices of refraction, as described by Snell's Law (named for the Dutch astronomer Willebrord Snellius):

$$\frac{\sin\theta_1}{\sin\theta_2} = \frac{v_1}{v_2} = \frac{n_2}{n_1}$$

The more familiar presentation of Snell's Law is:

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

Sample Problem:

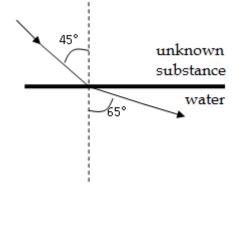
Big Ideas

Details

Q: Incident light coming from an unknown substance strikes water at an angle of 45°. The light refracted by the water at an angle of 65°, as shown in the diagram at the right. What is the index of refraction of the unknown substance?

A: Applying Snell's Law:

 $n_{1} \sin \theta_{1} = n_{2} \sin \theta_{2}$ $n_{1} \sin(45^{\circ}) = (1.33) \sin(65^{\circ})$ $n_{1} = \frac{(1.33) \sin 65^{\circ}}{\sin 45^{\circ}} = \frac{(1.33)(0.906)}{0.707} = 1.70$



	Refra	ction	Page: 387
Big Ideas	Details		Unit: Light & Optics
	The index of refraction of a medium through it. The index of refraction violet end of the spectrum) and les red end of the spectrum.	is greater for shorter wavele	engths (toward the
	 <u>prism</u>: an object that refracts light If light passes through a prism (from air into the prism and back out) and the two interfaces are 	White light	
	not parallel, the different indices of refraction for the different wavelengths will cause the light to spread out.		
	When light is bent by a prism, the ratio of wavelengths. Thus, we can sir sir		

Thin-Film Interference

Thin-film interference occurs when light strikes a thin film of liquid. Some of the light is reflected off the film, and some is refracted through the film and reflected off the interface between the film and the surface on the other side of it.

Big Ideas

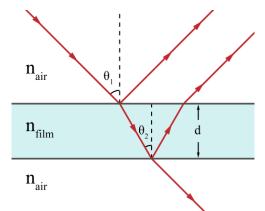
Details

You have likely seen thin-film interference, which you observe as the colors on the surface of a soap bubble or an oil slick.



Thin-film interference in a soap bubble. Used with permission.

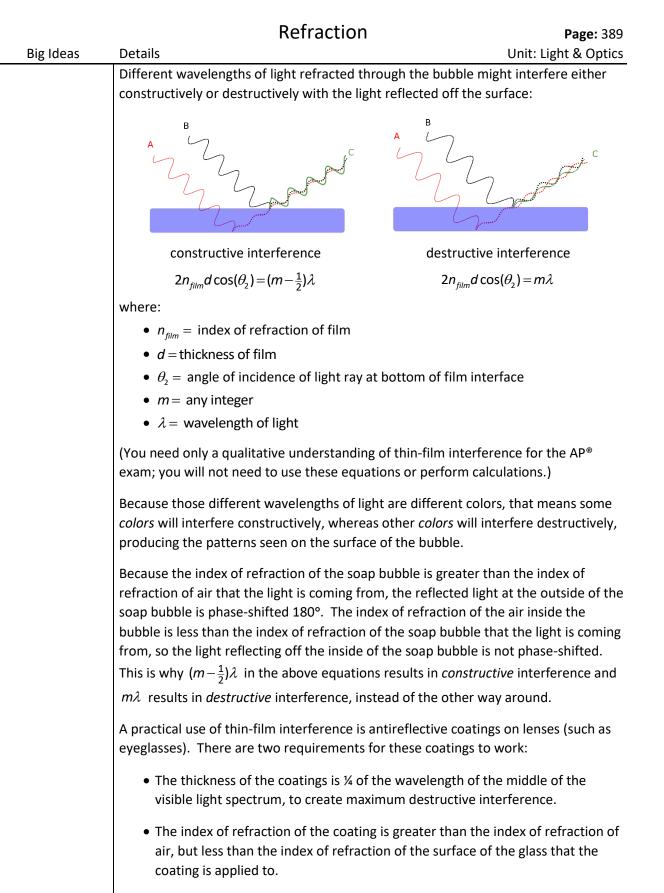
The following diagram shows what happens when light strikes the bubble:



Light passing through the air strikes a soap bubble of thickness d at an incident angle of θ_1 .

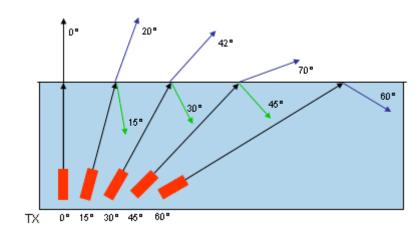
Some of the light is reflected at the same angle. The rest of the light is refracted through the bubble at angle θ_2 (as described by Snell's Law). Some of that refracted light is reflected off the interface between the soap bubble and the air inside it, also at angle θ_2 .

The light is then refracted back into the air outside the bubble, parallel to the original ray (angle θ_1).



Total Internal Reflection

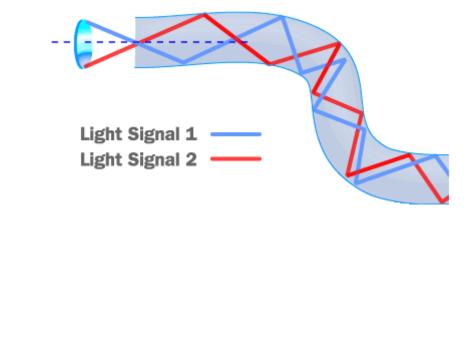
If a light wave is traveling from a slower medium to a faster one and the angle is so steep that the refracted angle would be 90° or greater, the boundary acts as a mirror and the light ray reflects off of it. This phenomenon is called *total internal reflection*:



critical angle (θ_c): the angle beyond which total internal reflection occurs.



Total internal reflection is how optical fibers (long strands of optically pure glass with a high index of refraction) are used to transmit information over long distances, using pulses of light.



Total internal reflection is also the principle behind speech teleprompters:



The speaker stands behind a clear piece of glass. The image of the speech is projected onto the glass. The text is visible to the speaker, but not to the audience.

Big Ideas

Details

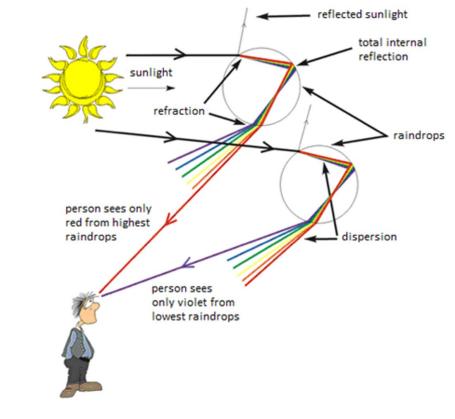
Details

Rainbows

A rainbow occurs from a combination of refraction, total internal reflection, and a second refraction, with raindrops acting as the prisms.

When this process occurs, different wavelengths of are refracted at different angles. Because colors near the red end of the spectrum have a lower index of refraction, the critical angle is shallower for these wavelengths, and they are reflected at a shallower angle than colors closer to the violet end of the spectrum.

The overall change in the direction of the light after this combination of refraction– reflection–refraction (including both refractions as well as the reflection) ranges from approximately 40° for violet light to approximately 42° for red light. This difference is what produces the spread of colors in a rainbow, and is why red is always on the outside of the rainbow and violet is always on the inside.



Because the light reflected and refracted through the raindrops must be viewed at angles of 40–42°, rainbows can be seen only when the sun is low in the sky (around sunrise or sunset). Otherwise, the rainbow would appear below the horizon.

When internal reflection occurs twice on the inside of a raindrop, the result is a second rainbow. The second rainbow appears above the first because the angle of light exiting the raindrop is greater—varying from 50° for red light to 52.5° for violet light. Both internal reflections create a phase shift of 180°, reversing the colors (as with thin-film interference), which is why violet is on the outside of the second rainbow, and red is on the inside.

This is a picture of a double rainbow in Lynn, Massachusetts. Note that the order of the colors in the second rainbow is reversed.



Note also that the sky is brighter inside the primary rainbow. There are two reasons for this. First, it's not actually true that each band is only one color of light. Because red light reflects at <u>all</u> angles greater than or equal to 40°, red light is therefore a component of all of the colors inside the red band of the rainbow. The same is true for each of the other colors; inside of the violet band, all wavelengths of visible light are present, and the result is white light. Outside of the red band, no visible light is refracted, which causes the sky outside the rainbow to appear darker.

The second reason is that raindrops scatter light at all wavelengths, and light scattering is also a significant contributing factor to the brightness inside. (See the *Scattering* topic starting on page 419 for more information.)

You may also notice that because the second rainbow is reversed, the sky is slightly brighter <u>outside</u> of the second rainbow.

Big Ideas

Details

		Refraction	Page: 394			
Big Ideas	Details		Unit: Light & Optics			
	Homework Problems					
		need to look up indices of refraction in Table Q on pa ce Tables in order to answer these questions.	ge 587 of your Physics			
		(M) A ray of light traveling from air into borosilicate gat an angle of 30°. What will be the angle of refractio				
		Answer: 19.8°				
		(S) Light traveling through air encounters a second m light to $2.7 \times 10^8 \frac{m}{s}$. What is the index of refraction of				
		Answer: 1.11				
	3.	(M) What is the velocity of light as it passes through a	a diamond?			
		Answer: $1.24 \times 10^8 \frac{\text{m}}{\text{s}}$				

Big Ideas Details	Refraction	Page: 395 Unit: Light & Optics
4.		vard the surface of the that will cause beam
	Answer: 48.6°	
5.	(S) A graduated cylinder contains a layer of silicone oil laser beam is shone into the silicone oil from above (in from the vertical. What is the angle of the beam in the	air) at an angle of 25°
	Answer: 18.5°	
6.	(S) A second graduated cylinder contains only a layer laser beam is shone into the water from above (in air) 25° from the vertical. What is the angle of the beam in	at the same angle of
	Answer: 18.5°	

Polarization

Unit: Light & Optics

Details

Big Ideas

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 14.3.A, 14.3.A.2, 14.3.A.2.ii, 14.3.A.2.ii, 14.3.A.3

Mastery Objective(s): (Students will be able to...)

• Explain how and under which circumstances light can be polarized.

Success Criteria:

• Explanation accounts for the filtering of waves of other orientations and for the specific direction.

Language Objectives:

• Explain how polarized sunglasses work.

Tier 2 Vocabulary: polarized

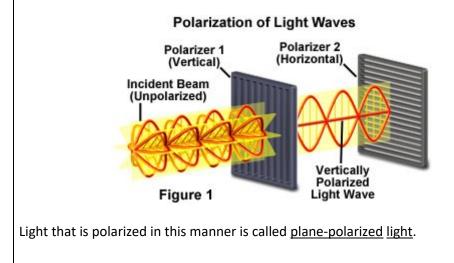
Labs, Activities & Demonstrations:

• polarizing filters

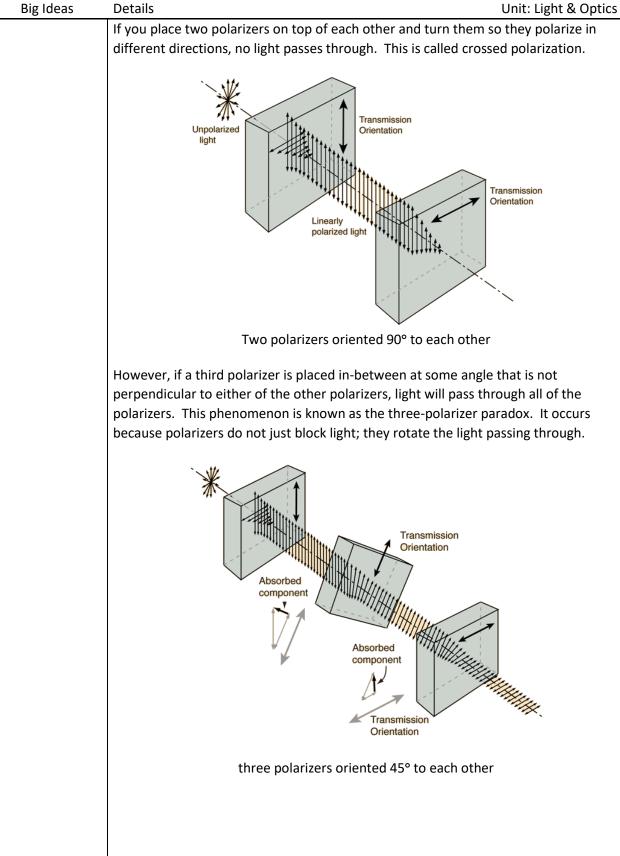
Notes:

Light (and other electromagnetic waves) are transverse waves with amplitudes in all directions that are perpendicular to the direction of propagation. However, light can be filtered such that it travels in a single plane. This process is called polarization.

Polarization can occur when light waves are reflected under certain conditions (which will be discussed later in this topic), or when light is passed through a special filter called a polarizer, which allows light to pass through in only one plane (direction). The action of a polarizer is shown in the following diagram:



Polarization



A flat surface can act as a polarizer at certain angles. The Scottish physicist Sir David Brewster derived a formula for the angle of maximum polarization based on the indices of refraction of the two substances:

$$\theta_{\scriptscriptstyle B} = \tan^{-1} \left(\frac{n_2}{n_1} \right)$$

where:

Details

Big Ideas

 $\theta_B = \text{Brewster's angle, the angle of incidence at which unpolarized light striking a surface is perfectly polarized when reflected.}$

 $n_1 \& n_2$ = indices of refraction of the two substances

The two pictures below were taken with the same camera and a polarizing filter. Compare the window of the house in the middle of each picture.

In the picture on the left, the camera's polarizing filter is aligned with the light reflected off the window. In the picture on the right, the polarizing filter is rotated 90°, so that none of the reflected light from the window can get to the camera lens.



Another example is light reflecting off a wet road. When the sun shines on a wet road at a low angle, the reflected light is polarized parallel to the surface (*i.e.*, horizontally). Sunglasses that are polarized vertically (*i.e.*, that allow only vertically polarized light to pass through) will effectively block most or all of the light reflected from the road.

Yet another example is the light that creates a rainbow. When sunlight reflects off the inside of a raindrop, the angle of incidence is very close to Brewster's angle. This causes the light that exits the raindrop to be polarized in the same direction as the bows of the rainbow (*i.e.*, horizontally at the top). This is why you cannot see a rainbow through polarized sunglasses!

Note that polarization generally reduces the intensity of the light.

Note also that because the displacement of a longitudinal wave is along the direction of propagation rather than perpendicular to it, longitudinal waves cannot be polarized.

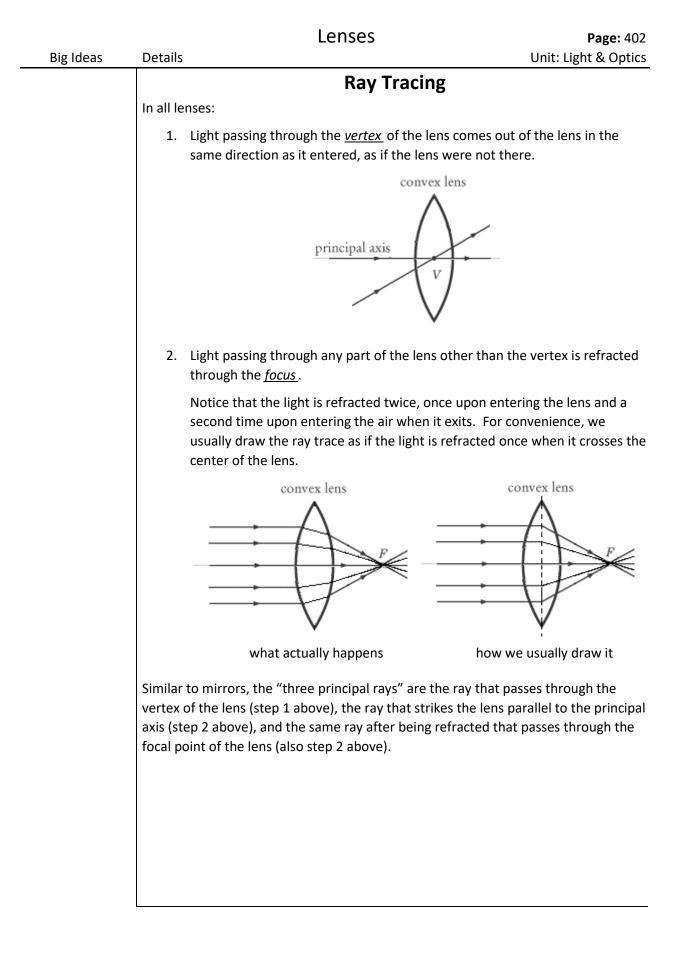
D	5	Lenses	Page: 399
g Ideas	Details		Unit: Light & Optic
		Lenses	
	Unit: Light & Optic	CS	
	NGSS Standards/N	MA Curriculum Frameworks (2016)	: N/A
	-	rning Objectives/Essential Knowled .4.A.3, 13.4.A.4, 13.4.A.5, 13.4.A.5.i 3.4.A.7.ii	
	Mastery Objective	e(s): (Students will be able to)	
	 Draw ray tra 	icing diagrams for refraction throug	h convex and concave lenses.
	 Numerically the image. 	calculate the distance from the len	s to its focus and the lens to
	Success Criteria:		
	 Ray diagram 	s correctly show location of object,	focus and image.
	 Calculations 	are correct with correct algebra.	
	Language Objectiv	/es:	
	Explain when	n and why images are inverted (ups	side-down) vs. upright.
	Tier 2 Vocabulary:	: light, refraction, virtual image, rea	al image, lens, focus
	-	& Demonstrations:	
	Fresnel lens		
	 optics bench 	ı lab	
	Notes:		
	produce an image	to curved mirrors in that they chang of an object that can have a differe mirror relative to the object.	
		nt from mirrors in that light passes t fraction instead of reflection.	through them, which means
		metrical optical device which refrant nt either converge or diverge.	cts light in a way that makes
	convex lens: a lens	s that refracts light so that it conver	ges as it passes through.
	concave lens: a ler	ns that refracts light so that it diverg	ges as it passes through.
	focus or focal poin	<u>it</u> : the point at which light rays conv	verge after passing through the

	LEIISES	Page: 400
Big Ideas	Details	Unit: Light & Optics
	principal axis: a line perpendicular to the surface of the lens, through it is refracted at an angle of 0° (<i>i.e.</i> , the direction	
	The principal axis is often shown as a single horizontal lin the surface of a lens has a principal axis. Note also that i its principal axis may be different on each side.	
	vertex: the point where the principal axis passes through the	center of the lens.
	<u>real image</u> : an image produced by light rays that pass throug <i>image</i> will appear on the <i>opposite side of the lens</i> from the seeing through a magnifying glas	the object. A real image
	<u>virtual image</u> : an apparent image produced at the point whe to originate. A <i>virtual image</i> will appear on the <i>same sid</i> object.	
	A rule of thumb that works for both mirrors and lenses is tha produced by the convergence of the <i>actual rays of light</i> . A v perception of where the rays of light would have come from.	rirtual image is our
	upright image: an image that is oriented in the same directio side-up")	n as the object.("right-
	inverted image; an image that is oriented in the opposite dire ("upside-down")	ection from the object.

Big Ideas	Details	Unit: Light & Optics
	Calculatio	ons
	The equations for lenses are the same as the e Distances are measured from the vertex.	quations for curved mirrors.
	The magnification (<i>M</i>) is the ratio of the height object (<i>h</i> _o), which is equal to the ratio of the di- the object (<i>s</i> _o). $M = \frac{h_i}{h_o} = -$	istance of the image (<i>s_i</i>) to distance of
	h _o	s _o
	As with mirrors, the distance to the image is de and negative for a virtual image. However, not caused by the rays of light that pass through th behind a lens, where as a real image is in front	te that with lenses the real image is ne lens, which means a real image is
	Note also that for lenses, this means that the p the positive for the image are opposite.	oositive direction for the object and
	As with mirrors, the distance from the vertex or by the equation:	of the lens to the focus (f) is defined
	$\frac{1}{s_i} + \frac{1}{s_o} = \frac{1}{s_o}$	$\frac{1}{f}$

Lenses

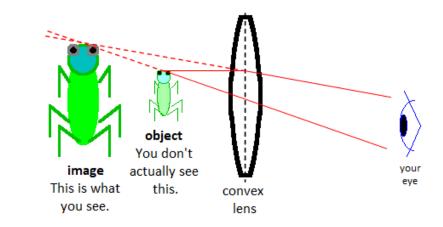
Page: 401



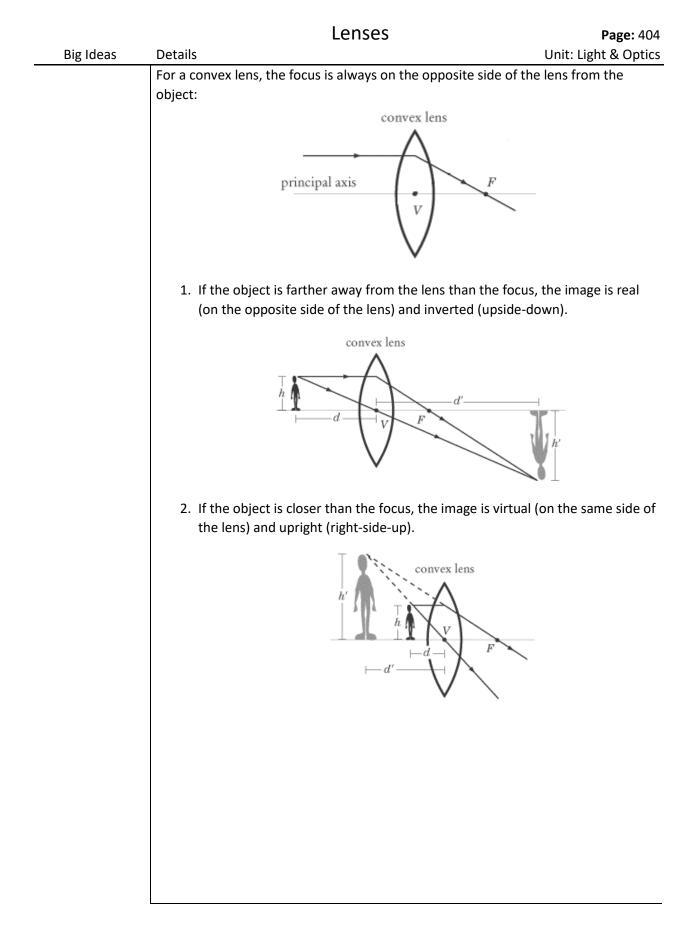
Convex Lenses

A convex lens causes light rays to converge (bend towards each other) as they pass through.

The most familiar use of convex lenses is as a magnifying glass. Note how the bending of the light rays makes the object appear larger.



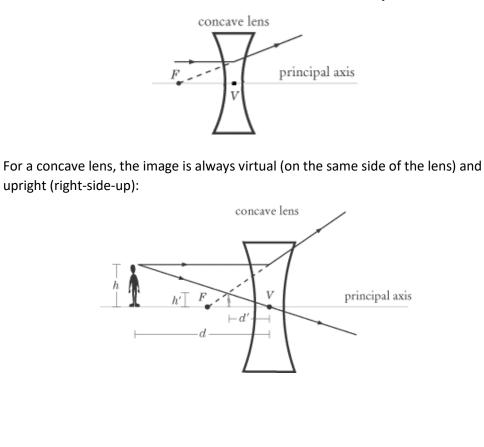
Note also that the lens bends **all** of the light. Your eyes cannot see the unbent light rays, which means you cannot see the actual object in its actual location; you <u>only</u> see the image.





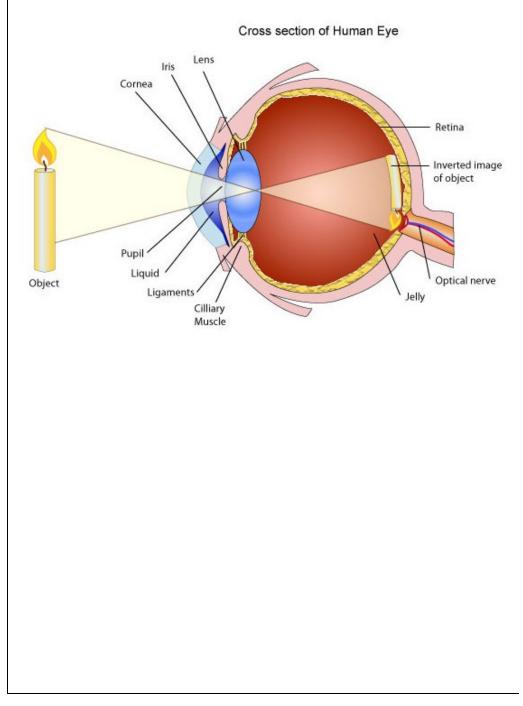
Concave Lenses

A concave lens causes light rays to diverge (bend away from each other). For a concave lens, the focus is on the same side of the lens as the object.



Physiology

In the human eye, the cornea and lens both act as lenses. However, because the action of the ciliary muscles changes the shape of the lens, the lens is responsible for the exact focal point, which determines what we are focusing our eyes on. When the ciliary muscles relax, the images of distant objects are focused on the retina. When these muscles contract, the focal point moves, and closer objects come into focus.



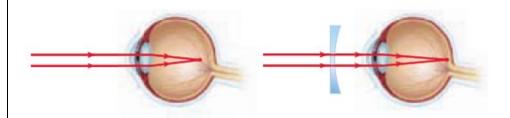
Big Ideas

Details

Details

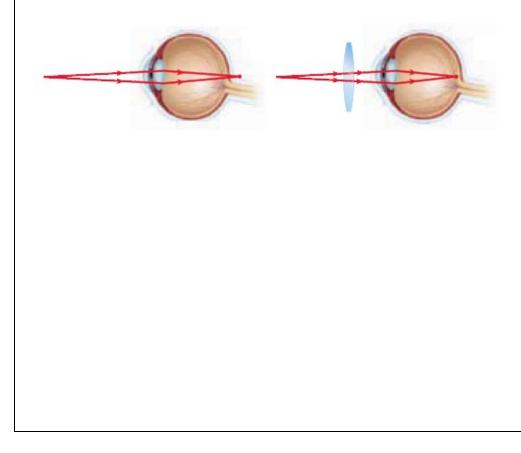
Nearsightedness and Farsightedness

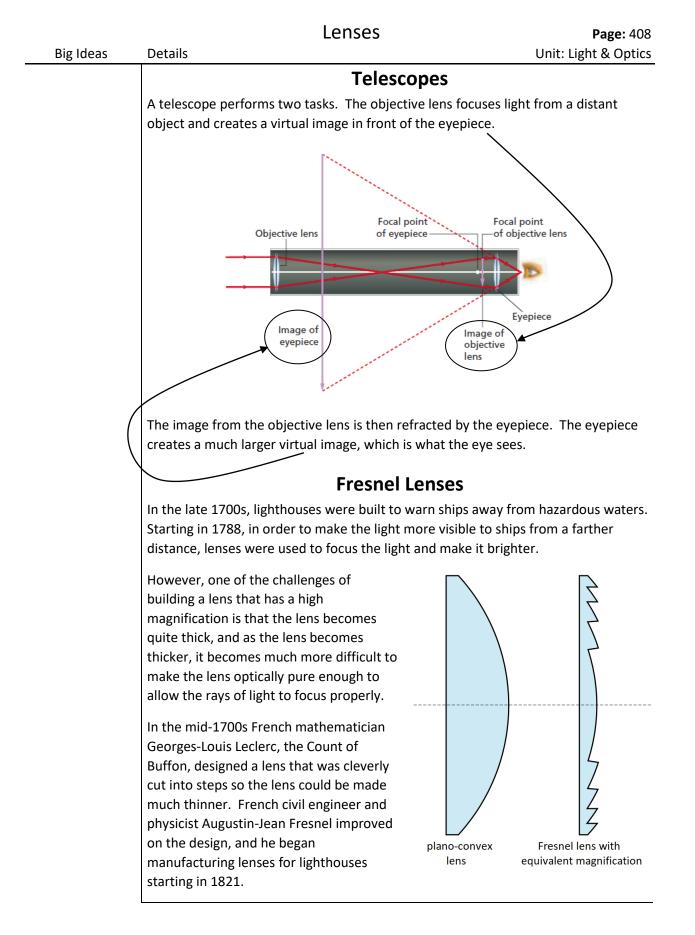
"Nearsighted" means only objects near the eye are in focus; the viewer is unable to focus on distant objects. This happens because the focus of the lens when the ciliary muscles are fully relaxed is in front of the retina. Nearsightedness is corrected by eyeglasses with concave lenses, which move the focal point back to the retina.

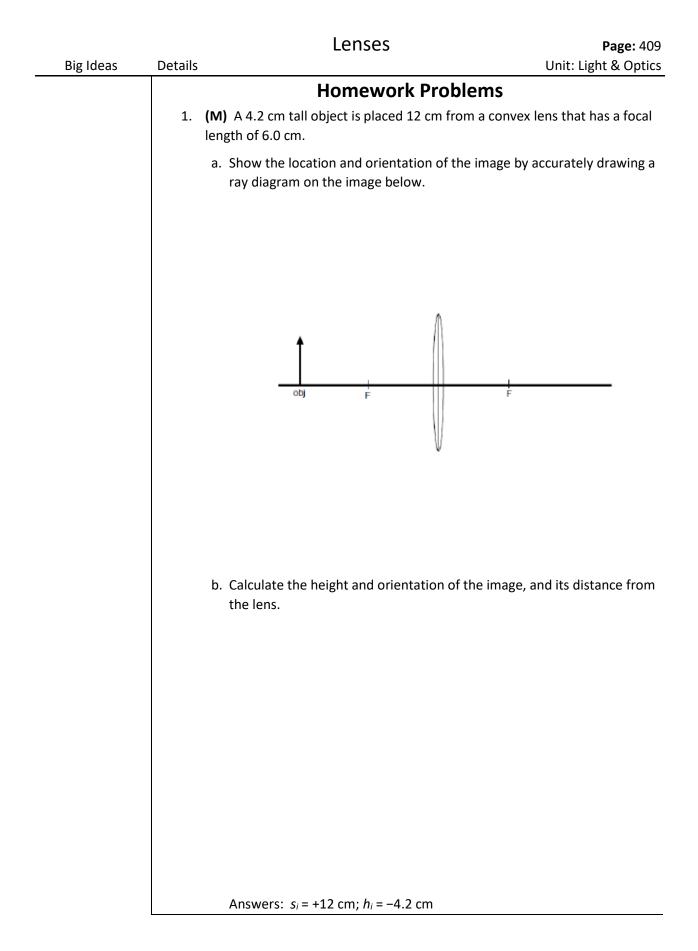


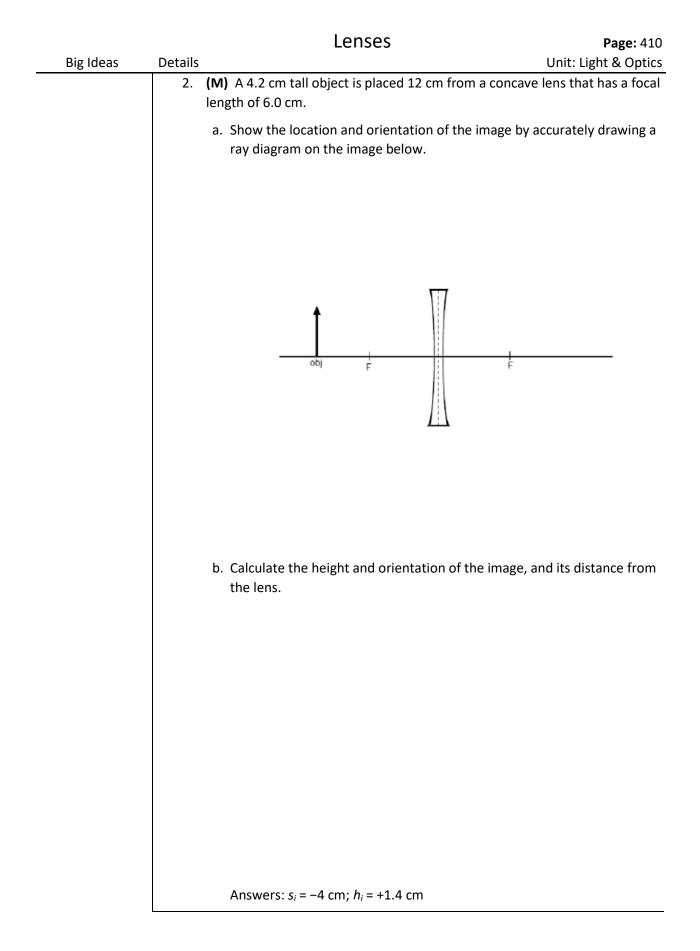
Notice that lenses that correct nearsightedness are concave only on the inside. This helps the lenses avoid the "Coke bottle" look.

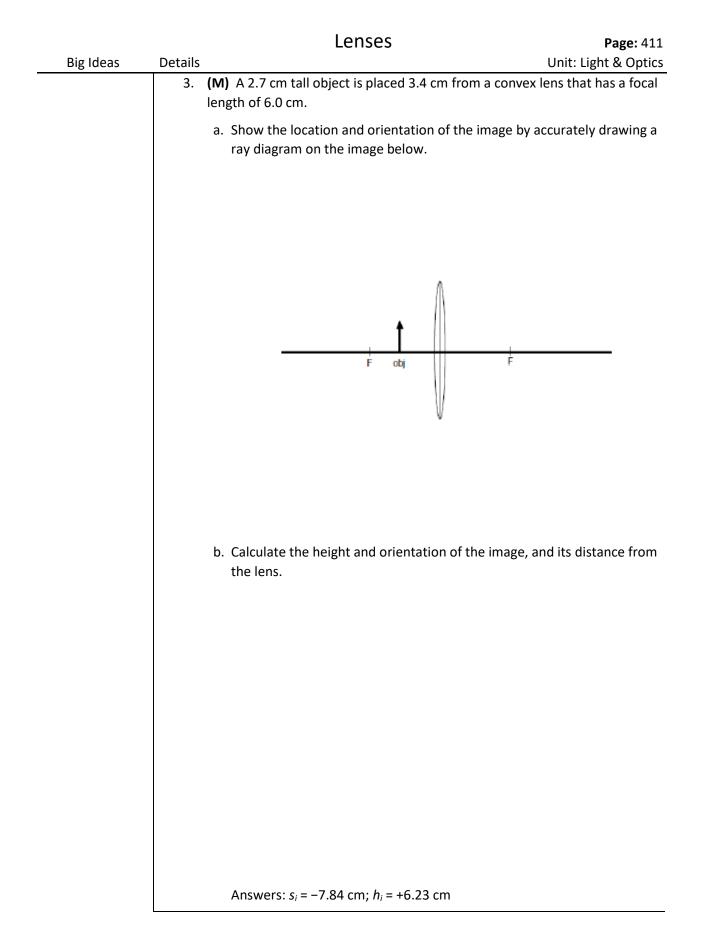
"Farsighted" means only objects far away from the eye are in focus; the viewer is unable to focus on close objects. This happens because the ciliary muscles cannot contract enough to bring the focal point of the lens for light coming from nearby objects onto the retina. Farsightedness is corrected by eyeglasses with convex lenses, which move the focal point forward to the retina.

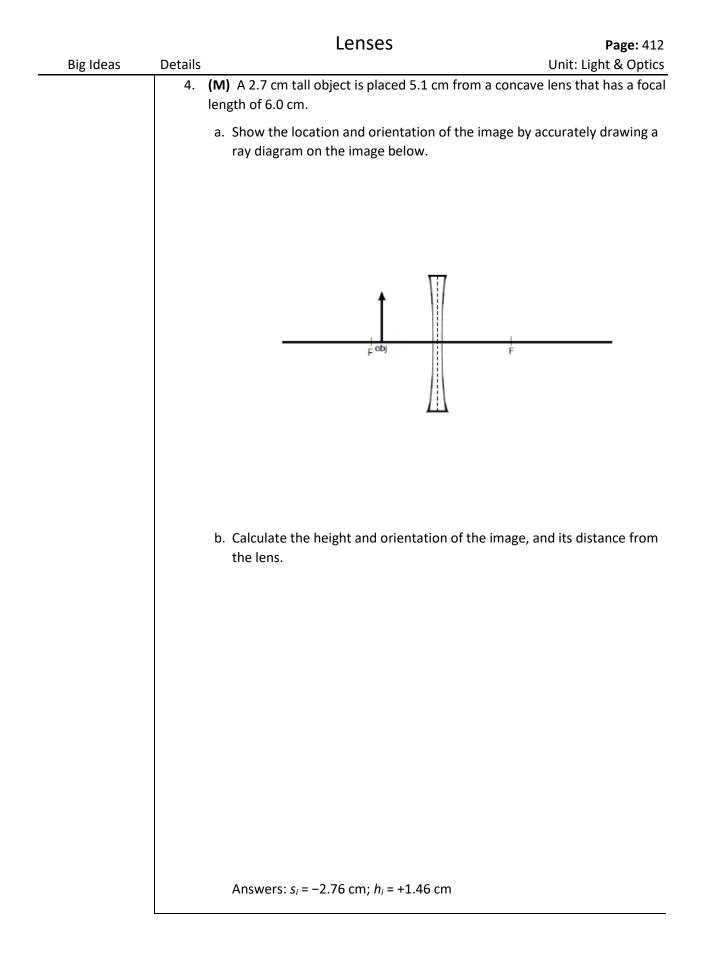








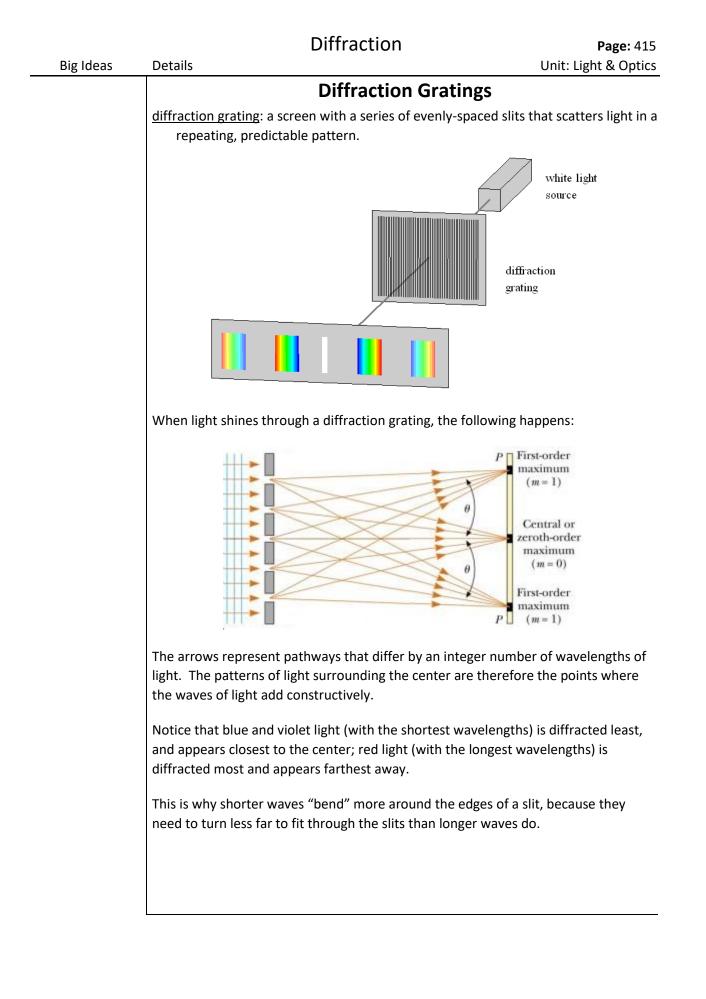




Big Ideas	Diffraction	Page: 413 Unit: Light & Optics
	Diffraction	onit. Light & Optics
	Unit: Light & Optics	
	NGSS Standards/MA Curriculum Frameworks (2016): N/A AP [®] Physics 2 Learning Objectives/Essential Knowledge (2024 14.8.A.1.i, 14.8.A.1.ii, 14.8.A.1.iii, 14.8.A.1.iv, 14.8.A.1.v, 1 14.8.A.3, 14.8.A.4, 14.8.A.5	
	Mastery Objective(s): (Students will be able to)	
	• Explain how light "spreads" beyond an opening or around	d an obstacle.
	 Perform calculations relating to the location of bright and light passes through a diffraction grating. Success Criteria: 	dim regions when
	• Explanations account for observed behavior.	
	 Calculations are correct with correct algebra. Language Objectives: 	
	Explain why looking through a diffraction grating produce	es a "rainhow"
	Tier 2 Vocabulary: light, diffraction, slit	
	 Labs, Activities & Demonstrations: thickness of human hair double slit experiment with laser & diffraction grating 	
	Notes:	
	<u>diffraction</u> : the slight bending of a wave as it passes around the edge of an object or through a slit: Wave M	otion Obstacle
	When light passes straight through a wide opening, the rays co- line. However, if we make the slit so narrow that the width is approximately equal to the wavelength, then the slit effectively becomes a point, and diffraction occurs in all directions from it.	ntinue in a straight

Diffraction

	Diffaction	Page: 414
Big Ideas	Details	Unit: Light & Optics
	If we shine light through a slit whose thickness is approxima	tely the same order of
	magnitude as the wavelength, the light can only hit the wall	in specific locations.
	In this diagram, light travels the same distance for paths 1 a	nd 2_the same number
	of wavelengths. Light waves hitting	nu z—the same number
	this point will add constructively,	
	which makes the light brighter.	3
		3
	However, for paths 3 and 4, path 4	4
	is ½ wavelength longer than path 3.	
	Light taking path 4 is ½ wavelength	2 2
	out of phase with light from path 3.	
	The waves add destructively	
	(cancel), and there is no light:	
	Farther up or down on the right side will be alternating loca	tions where the
	difference in path length (ΔD) results in waves that are diffe	rent by an exact multiple
	of the wavelength (in phase = constructive interference = br	ight spot), <i>vs</i> . by a
	multiple of the wavelength plus ½ (out-of-phase = destructive	ve interference = dark
	spot).	
	The difference in path length is given by the equation:	
	$\Delta D = a \sin \theta$	
	where:	
	ΔD = the difference in path length between light cor	ning from the center of
	the slit and its edge	
	a = the width of the opening	
	θ = the angle between a line normal to the opening	g and the direction of
	propagation of the actual wave	
	For small angles $(0 < 10^{\circ})$ the "small angle approximation"	aan ha usadu
	For small angles (θ < 10°), the "small-angle approximation" of	Lan be used:
	$a\left(\frac{y_{\min}}{l}\right) \approx m\lambda$	
	where:	
	a = the width of the slit	
	y_{min} = the distance from the central (bright) fringe to	the m th order of
	minimum brightness on the screen.	
		ad the cereen
	L = the distance between the diffraction grating ar	
	<i>m</i> = the number of waves that equals the difference	e in the lengths of the
	two paths (integer)	
	λ = the wavelength of the light	

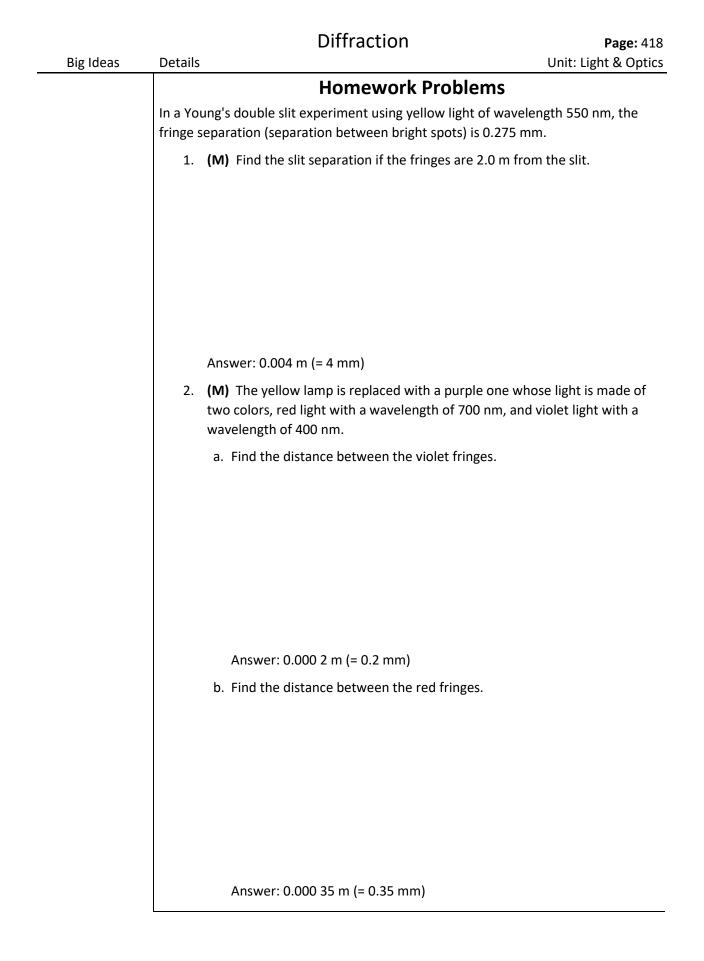


Diffraction

	Diffraction	Page: 416
Big Ideas	Details	Unit: Light & Optics
	In a diffraction grating that has multiple slits that are a distance	•
	difference in path length will be the same $\Delta D = d \sin \theta$ as we say	
	there will be maximum constructive interference when ΔD is a	n exact (integer)
	multiple of the wavelength. This gives the equation:	
	$d\sin\theta_m = m\lambda$	
	where:	
	d = the distance between the slits	
	θ_m = the angle of emergence (or angle of deviation) in ord slit to add constructively to light from a neighboring wavelengths away.	-
	 m = the number of waves that equals the difference in the paths (integer) 	e lengths of the two
	λ = the wavelength of the light	
	For small angles (θ < 10°), the "small-angle approximation" is sinabove:	nilar to what we saw
	$d\left(\frac{y_{max}}{L}\right) \approx m\lambda$	
	where:	
	<i>d</i> = the distance between the slits	
	y_{max} = the distance from the central (bright) fringe to the	m th order of
	maximum brightness on the screen.	
	L = the distance between the diffraction grating and the time the diffraction grating and the time time time time time time time tim	ne screen.
	m = the number of waves that equals the difference in	
	two paths (integer) λ = the wavelength of the light	
	λ = the wavelength of the light	
	Diffraction gratings are used in spectroscopes, which you have p chemistry and/or physics classes to see different wavelengths o light source.	

Diffraction

Big Ideas	De	tails		Unit: Light & Optics
	Sa	mple Problem:		
	Q:	laser with a wavelength of 5	32 nm, and a blue las hone through a diffra	ction grating with 5000 lines
	A:	For our diffraction grating, 5	000 lines per cm equ	als 500 000 lines per meter.
		$d = \frac{1}{500000} = 2 \times 10^{-6} \mathrm{m}$		
		For the red laser, 650 nm eq	uals $\lambda = 650 \text{nm} = 6.5$	0×10 ⁻⁷ m
		The equation is:		
			$d\sin\theta_m = m\lambda$	
		For the red laser at $m = 1$, th		_
		•	$\times 10^{-6}$)sin $\theta = (1)(6.50)$	•
		sin	$\theta = \frac{6.50 \times 10^{-7}}{2 \times 10^{-6}} = 0.32$	5
		heta =	= sin ⁻¹ (0.325) = 19.0°	
		For the green laser ($\lambda = 532$	nm=5.32×10 ⁻⁷ m) an	d the blue laser also at $m = 1$
		$(\lambda = 405 \mathrm{nm} = 4.05 \times 10^{-7} \mathrm{m}):$		-
		$\sin\theta = \frac{5.32 \times 10^{-7}}{2 \times 10^{-6}} = 0.266$	and	$\sin\theta = \frac{4.05 \times 10^{-7}}{2 \times 10^{-6}} = 0.203$
		$\theta = \sin^{-1}(0.266) = 15.4^{\circ}$		$\theta = \sin^{-1}(0.203) = 11.7^{\circ}$



Scattering

(not AP[®]) Unit: Light & Optics

Details

Big Ideas

honors

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): N/A

Mastery Objective(s): (Students will be able to ...)

• Explain why the sky is blue and the sun looks red at sunset.

Success Criteria:

• Explanations account for observed behavior.

Language Objectives:

• Explain why the beaker in the "sunset in a beaker" demo looks light blue, but the light coming through it looks yellow or red.

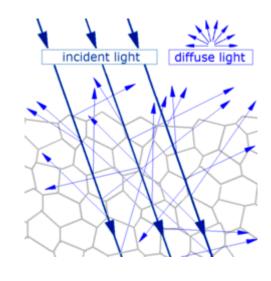
Tier 2 Vocabulary: light, scatter

Labs, Activities & Demonstrations:

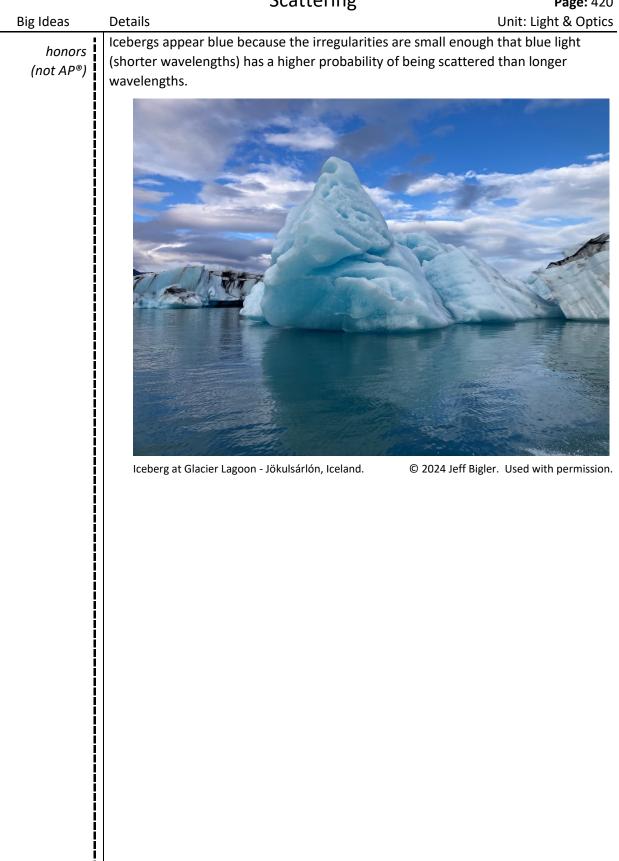
• sunset in a beaker

Notes:

<u>scattering</u>: a change in the direction of rays of light caused by irregularities in the propagation medium, collisions with small particles, or at the interface between two media.



Scattering



Scattering

0	
	honors
(n	ot AP®)

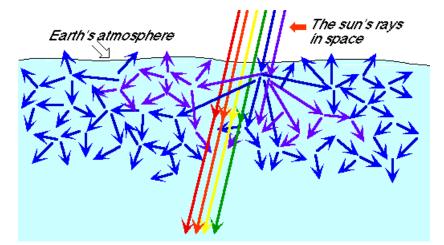
Details

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Big Ideas

<u>Rayleigh scattering</u>: scattering of light because of collisions with small particles in the medium. Rayleigh scattering is named after the British physicist Lord Rayleigh.

Rayleigh scattering is responsible for the color of the sky. Small particles (0.5–1 micron) scatter visible light as it passes through Earth's atmosphere. Because light at the blue and violet end of the spectrum is about five times as likely to be scattered as light at the red end of the spectrum, the majority of the scattered light in our atmosphere is blue.



This is also why the sun appears yellow during the day—the combination of red, orange, yellow and green light appears yellow to us.

Water vapor molecules are much larger—ranging in size from 2–5 microns. For these larger particles, the probability of scattering is approximately the same for all wavelengths, which is why clouds appear white.

At sunset, because the angle of the sun is much lower, the light must pass through much more of the atmosphere before we see it. By the time the light gets to our eyes, most of the colors are removed by scattering, except for the red end of the spectrum, which is why the sun appears red at sunset.

Sunlight goes through more of atmosphere. Higher probability of scattering longer wavelengths, leaving mostly red & orange. Sunlight goes through less of atmosphere. Low probability of scattering longer wavelengths, meaning mostly only blue is scattered.

Physics 2 In Plain English

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Unit: Quantum and Particle Physics

Topics covered in this chapter:
Atomic Structure (Review)429
Emission & Absorption431
Blackbody Radiation435
Photoelectric Effect440
Bohr Model of the Hydrogen Atom445
Wave-Particle Duality448
Quantum Mechanical Model of the Atom451
Compton Scattering453
Fundamental Forces455
Standard Model456
Particle Interactions

This chapter discusses the particles that atoms and other matter are made of, how those particles interact, and the process by which radioactive decay can change the composition of a substance from one element into another.

- *Photoelectric Effect* describes the observation that light of a sufficiently high frequency can remove electrons from an atom.
- *Bohr Model of the Hydrogen Atom* describes the development of quantum theory to describe the behavior of the electrons in an atom.
- *Wave-Particle Duality* and *Quantum Mechanical Model of the Atom* describe the idea that matter can behave like a wave as well as a particle, and the application of that idea to the modern quantum mechanical model of the atom.
- *Fundamental Forces* describes the four natural forces that affect everything in the universe: the strong and weak nuclear forces, the electromagnetic force, and the gravitational force.
- *The Standard Model* describes and classifies the particles that make up atoms.
- Particle Interactions describes interactions between subatomic particles.

Big Ideas	Details Unit: Quantum and Particle Physics
	One of the challenging aspects of this chapter is that it describes processes that happen on a scale that is much too small to observe directly. Another challenge is the fact that the Standard Model continues to evolve. Many of the connections between concepts that make other topics easier to understand have yet to be made in the realm of quantum & particle physics.
	Standards addressed in this chapter:
	Massachusetts Curriculum Frameworks (2016):
AP® only	HS-PS4-3. Evaluate the claims, evidence, and reasoning behind the idea that electromagnetic radiation can be described by either a wave model or a particle model, and that for some situations involving resonance, interference, diffraction, refraction, or the photoelectric effect, one model is more useful than the other.
	AP [®] Physics 2 Learning Objectives/Essential Knowledge (2024):
	15.1.A : Describe the properties and behavior of an object that exhibits both particle-like and wave-like behavior.
	15.1.A.1: Quantum theory was developed to explain observations of matter and energy that could not be explained using classical mechanics. These phenomena include, but are not limited to, atomic spectra, blackbody radiation, and the photoelectric effect.
	15.1.A.1.i : Quantum theory is necessary to describe the properties of matter at atomic and subatomic scales.
	15.1.A.1.ii: In quantum theory, fundamental particles can exhibit both particle-like and wave-like behavior.
	15.1.A.2: Light can be modeled both as a wave and as discrete particles, called photons.
	15.1.A.2.i: A photon is a massless, electrically neutral particle with energy proportional to the photon's frequency.
	15.1.A.2.ii : Photons travel in straight lines unless they interact with matter.
	15.1.A.3: The speed of a photon depends on the medium through which the photon travels.
	15.1.A.3.i : The speed of all photons in free space is equal to the speed of light, $c = 3.00 \times 10^8 \frac{\text{m}}{\text{s}}$.
	15.1.A.3.ii : In general, the speed of photons through a given medium is inversely proportional to the index of refraction of that medium.
	15.1.A.4: Particles can demonstrate wave properties, as shown by variations of Young's double-slit experiment.

Big Ideas	Details Unit: Quantum and Particle Physics
AP [®] only	15.1.A.4.i: A wave model of matter is quantified by the de Broglie wavelength, which increases as the momentum of a particle decreases.
	15.1.A.4.ii: Quantum theory is necessary to describe systems where the de Broglie wavelength is comparable to the size of the system.
	15.1.A.5: Values of energy and momentum have discrete, or quantized, values for bound systems described by quantum theory.
	15.2.A : Describe the properties of an atom.
	15.2.A.1: Atoms have internal structure.
	15.2.A.1.i: Atoms consist of a small, positively charged nucleus surrounded by one or more negatively charged electrons.
	15.2.A.1.ii: The nucleus of an atom is made up of protons and neutrons.
	15.2.A.1.iii: The number of neutrons and protons in an atom can be represented using nuclear notation.
	15.2.A.1.iv : An ion is an atom with a nonzero net electric charge.
	15.2.A.2 : Each atomic element has a unique number of protons.
	15.2.A.2.i: The number and arrangements of electrons affect how atoms interact.
	15.2.A.2.ii: The total number of neutrons and protons identifies the isotope of an element.
	15.2.A.2.iii: The mass of an atom is dominated by the total mass of the protons and neutrons in its nucleus.
	15.2.A.3: The Bohr model of the atom is based on classical physics and was the historical representation of the atom that led to the description of the hydrogen atom in terms of discrete energy states.
	15.2.A.3.i: In the Bohr model of the atom, electrons are modeled as moving around the nucleus in circular orbits determined by the electron's charge and mass, as well as the electric force between the electron and the nucleus.
	15.2.A.3.ii : The standing wave model of electrons accounts for the existence of specific allowed energy states of an electron in an atom, because the electron orbit's circumference must be an integer multiple of the electron's de Broglie wavelength.
	15.3.A : Describe the emission or absorption of photons by atoms.
	15.3.A.1: Energy transfer occurs when photons are absorbed or emitted by an atom, which is modeled as a system consisting of a nucleus and an electron.

Big Ideas	Details Unit: Quantum and Particle Physic
AP® only	15.3.A.2 : Energy can only be absorbed or emitted by an atom if the amount of energy being absorbed or emitted corresponds to the energy difference between two atomic energy states.
	15.3.A.2.i : An atom in a given energy state may absorb a photon of the appropriate energy and transition to a higher energy state.
1986 - 1986 - 1986 - 1986 - 1986 - 1986 - 1986	15.3.A.2.ii : An atom in an excited energy state may emit a photon of the appropriate energy to spontaneously move to a lower energy state.
	15.3.A.2.iii: Because an atom is modeled as a system consisting of an electron and a nucleus, a change in the energy state of an atom corresponds to a change in the interaction energy between the electro and the nucleus.
	15.3.A.3 : Transitions between two energy states of an atom correspond to the absorption or emission of a photon of a single frequency and, therefore, single wavelength.
	15.3.A.4: Atoms of each element have a unique set of allowed energy levels and thereby a unique set of absorption and emission frequencies. The unique set of frequencies determines the element's spectrum.
	15.3.A.4.i: An emission spectrum can be used to determine the elements in a source of light.
	15.3.A.4.ii: An absorption spectrum can be used to determine the element composing a substance by observing what light the substance has absorbed.
2 YORA - YORA - YORA - YORA - YORA - YORA - YORA - YORA - YORA - YORA - YORA - YORA - YORA - YORA - YORA - YORA	15.3.A.4.iii : Energy level diagrams are commonly used to visually represent the energy states of an atom.
	15.3.A.5 : Binding energy is the energy required to remove an electron from a atom, causing the atom to become ionized. An atom in the lowest energ level (ground state) will require the greatest amount of energy to remove the electron from the atom.
	15.4.A : Describe the electromagnetic radiation emitted by an object due to its temperature.
	15.4.A.1 : Matter will spontaneously convert some of its internal thermal energy into electromagnetic energy.
	15.4.A.2 : A blackbody is an idealized model of matter that absorbs all radiation that falls on the body. If the body is in equilibrium at a constan temperature, then it must in turn emit energy.

Big Ideas	Details Unit: Quantum and Particle Physics
AP [®] only	15.4.A.3 : A blackbody will emit a continuous spectrum that only depends on the body's temperature. The radiation emitted by a blackbody is often modeled by plotting intensity per unit wavelength as a function of wavelength.
	15.4.A.3.i: The distribution of the intensity of a blackbody's spectrum as a function of temperature cannot be modeled using only classical physics concepts. A blackbody's spectrum is described by Planck's law, which assumes that the energy of light is quantized.
	15.4.A.3.ii: The peak wavelength emitted by a blackbody (the wavelength at which the blackbody emits the greatest amount of radiation per unit wavelength) decreases with increasing temperature, as described by Wien's law.
	15.4.A.3.iii: The rate at which energy is emitted (power) by a blackbody is proportional to the surface area of the body and to the temperature of the body raised to the fourth power, as described by the Stefan-Boltzmann law.
	15.5.A : Describe an interaction between photons and matter using the photoelectric effect.
	15.5.A.1 : The photoelectric effect is the emission of electrons when electromagnetic radiation is incident upon a photoactive material.
	15.5.A.2 : The emission of electrons via the photoelectric effect requires a minimum frequency of incident light, called the threshold frequency.
	15.5.A.2.i: Light that is incident on a material and is at the threshold frequency or higher will induce electron emission, regardless of the number of photons that strike the material.
	15.5.A.2.ii : The energy of the emitted electrons is not dependent on the number of photons that are incident upon the material, which provides evidence that light is a collection of discrete, quantized energy packets called photons.

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Page: 427

Big Ideas	Details Unit: Quantum and Particle Physics
AP® only	15.5.A.3 : The maximum kinetic energy of an emitted electron is related to the frequency of the incident light and the work function of the material, ϕ .
	15.5.A.3.i : The work function of a material is the minimum energy required to emit an electron from atoms in the material.
	15.5.A.3.ii : The maximum kinetic energy of an emitted electron is given by the equation $K_{max} = hf - \phi$.
	15.5.A.3.iii : In a typical experimental setup to demonstrate the photoelectric effect and determine the work function of a metal, two metal plates are placed in a vacuum chamber and connected to a variable source of potential difference. One of the plates is illuminated by monochromatic light that causes electrons to be ejected and the potential difference between the plates is adjusted until no current is measured in the circuit.
	15.6.A : Describe the interaction between photons and matter using Compton scattering.
	15.6.A.1 : In Compton scattering, a photon interacts with a free electron. The Compton effect is when a photon that emerges from the interaction has a lower energy and longer wavelength than the incoming photon. The magnitude of the change is related to the direction of the photon after the collision.
	15.6.A.2 : Compton scattering provides evidence that light is a collection of discrete, quantized energy packets called photons.
	15.6.A.2.i: Compton scattering can be explained by treating a photon as a particle and applying conservation of energy and conservation of momentum to the collision between the photon and electron.
	15.6.A.2.ii : The transfer of a photon's energy to an electron results in the energy, momentum, frequency, and wavelength of the photon changing.
	15.6.A.3 : The change in wavelength experienced by a photon after colliding with an electron is related to how much the photon's direction changes.

Atomic Structure (Review)

Unit: Quantum and Particle Physics

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): 15.2.A, 15.2.A.1,

15.2.A.1.i, 15.2.A.1.ii, 15.2.A.1.iii, 15.2.A.1.iv, 15.2.A.2, 15.2.A.2.i, 15.2.A.2.ii, 15.2.A.2.iii

Mastery Objective(s): (Students will be able to...)

- Describe the basic subatomic particles (proton, neutron, electron)
- Describe various properties of subatomic particles, including their electrical charges, relative masses, and where they are found within an atom.

Success Criteria:

• Students demonstrate a correct understanding of the above objectives.

Language Objectives:

• Be able to explain and draw & label representations of an atom.

Tier 2 Vocabulary: atom, charge, nucleus

Notes:

Atomic & particle physics is concerned with the behaviors of atoms and the particles that they are made of. For this reason, it is useful to review some basic information about atoms that you should remember from your chemistry classes:

- Atoms have an internal structure consisting of a small, positively charged nucleus surrounded by negatively-charged electrons.
- The nucleus of an atom contains protons (which carry a positive charge) and neutrons (which do not carry an electrical charge). Each element has a unique number of protons, which means that the number of protons determines the element's identity.
- The number of protons and neutrons in an atom can be represented by nuclear notation. For example, $\frac{56}{26}$ Fe would denote an iron atom, with atomic number 26. This atom would have 26 protons and 56 26 = 30 neutrons.
- Protons carry a charge of 1.60×10^{-19} C = 1 elementary charge. Electrons carry a charge of -1.60×10^{-19} C = -1 elementary charge. An atom that has equal numbers of protons and electrons is electrically neutral.

Atomic Structure (Review)

	ALOMIC STRUCTURE (REVIEW) Page: 43
Big Ideas	Details Unit: Quantum and Particle Physic
	 Protons and neutrons remain in the nucleus of an atom, but electrons are outside of the nucleus and can be added to or removed from the atom by various processes (chemical, electrical, thermal). An atom that has a positive or negative charge due to its having gained or lost electrons is called an ion. For example, ⁵⁶₂₆Fe²⁺ would denote an iron ion with a +2 charge, indicating the it has 26 protons but only 24 electrons. Because electrons can be transferred between atoms, the chemical properties
	 of an atom are determined by the number and arrangements of its electrons The mass of an atom is dominated by the total mass of its protons and neutrons. Electrons have roughly ¹/₂₀₀₀ of the mass of a proton or neutron and contribute very little to the atom's mass.
	 Protons and neutrons have nearly identical masses. This means that the atomic mass of an element is determined by the number of protons + neutrons that it contains. The mass number of an element is called its isotop For example, ⁵⁶₂₆Fe (or just ⁵⁶Fe) would denote the isotope iron-56.

Emission & Absorption

Unit: Quantum and Particle Physics

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): 15.3.A, 15.3.A.1,

15.3.A.2, 15.3.A.2.i, 15.3.A.2.ii, 15.3.A.2.iii, 15.3.A.3, 15.3.A.4, 15.3.A.4.i, 15.3.A.4.ii, 15.3.A.4.iii

Mastery Objective(s): (Students will be able to...)

- Describe the emission or absorption of photons by atoms.
- Relate atomic emission and absorption spectra.
- Identify an element based on its emission or absorption spectra.
- Calculate the frequency/wavelength of light emitted using the Rydberg equation.

Success Criteria:

Details

Big Ideas

• Calculations are correct

Language Objectives:

• Be able to explain and draw & label representations of an atom.

Tier 2 Vocabulary: atom, charge, nucleus

Notes:

<u>energy state</u>: the position of an electron that corresponds to the interaction energy between that electron and the nucleus of the atom. In general, higher energy states correspond with greater distances from the nucleus.

<u>absorption</u>: when photons are absorbed (taken in) by an atom, pushing the atom to a higher energy state.

<u>emission</u>: when photons are emitted (given off) by an atom, causing the atom to spontaneously move to a lower energy state.

Absorption and emission are the processes by which an atom can take in or give off energy. The specific amount of energy that is absorbed or emitted corresponds to the difference in energy between the energy states of electrons in the atom before *vs.* after the absorption or emission.

Because the photons produced by these transitions have a specific amount of energy, those photons therefore have a specific frequency and wavelength:

$$E = hf$$
$$c = \lambda f$$

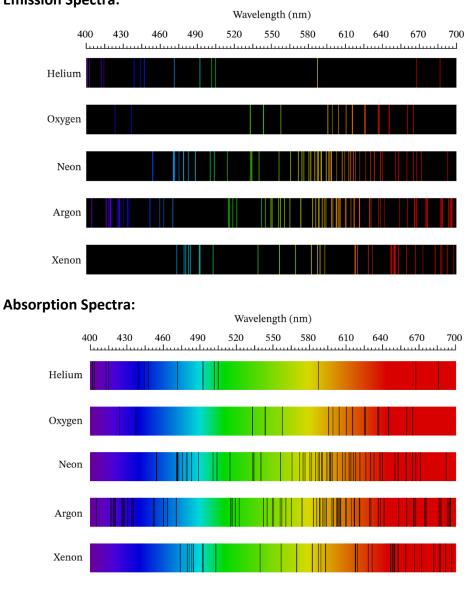
Emission & Absorption

Absorption and Emission Spectra

The set of electrons in an atom and their possible energy states define the specific frequencies and wavelengths that can be produced. In this way, the spectrum of wavelengths produced when energy is absorbed or emitted is a way of determining the elements in a source of light.

spectroscopy: the study and interpretation of wavelengths of light

Here are emission and absorption spectra for selected elements. Notice that for a given element, the wavelengths emitted and absorbed are the same.



Emission Spectra:

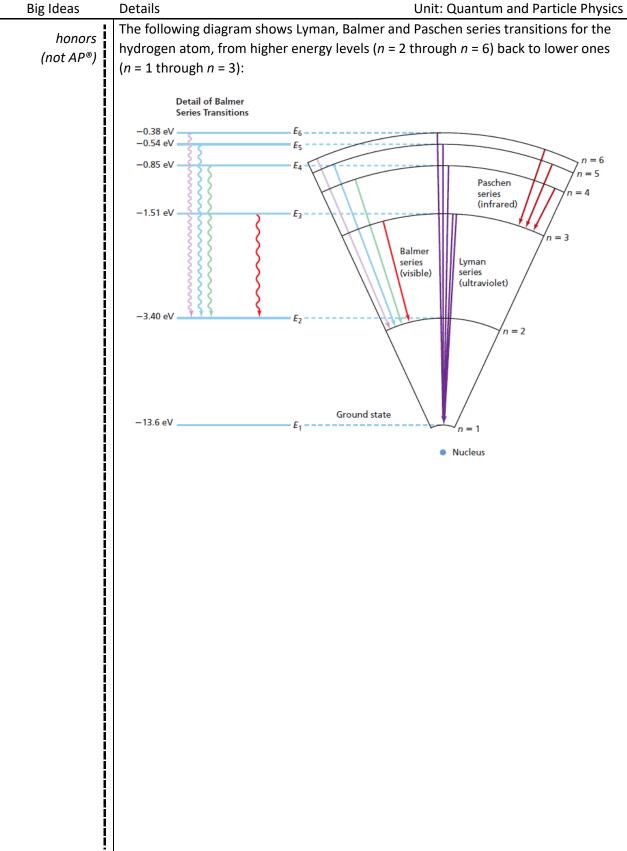
Details

Big Ideas

Emission & Absorption

		111331011 0	Absorption			Page: 433				
Big Ideas	Details			Unit:	Quantum	and Particle Physics				
	Development of Spectroscopy Spectroscopy was discovered in the 17 th century, when prisms were first used to separate light by wavelength. Isaac Newton performed the first experiments with optics and is generally considered to be the founder of modern spectroscopy.									
honors (not AP®)	In 1885, Johann Balmer studied the emission lines produced by the hydrogen atom. He devised an empirical equation to relate these emission lines.									
	<u>Rydberg Formula</u> (1888): Swedish physicist Johannes Rydberg developed a generalized formula that could describe the wave numbers of all of the spectral lines in hydrogen (and similar elements).									
	There are several series of spectral lines for hydrogen, each of which converge different wavelengths. Rydberg described the Balmer series in terms of a pair of integers (n_1 and n_2 , where $n_1 < n_2$), and devised a single formula with a single constant (now called the Rydberg constant) that relates them.									
			$\frac{1}{\lambda_{vac}} = R_H \left(\frac{1}{n_1^2} - \frac{1}{n_1^2} \right)$	$\left(\frac{1}{n_2^2}\right)$						
	The value of Rv	dberg's consta	ant. R _H . is							
	The value of Rydberg's constant, R_H , is $\frac{m_e e^4}{8 \varepsilon_o^2 h^3 c} = 10973731.6 \text{ m}^{-1} \approx 1.1 \times 10^7 \text{ m}^{-1}$, where m_e is the rest mass of the									
	0		charge, $arepsilon_{\circ}$ is the							
		-	e speed of light i	-	-	•				
	Rydberg's equation was found to be consistent with other series discovered later, including the Lyman series (in the ultraviolet region; first discovered in 1906) and the Paschen series (in the infrared region; first discovered in 1908). Those series and their converging wavelengths are:									
		Series	Wavelength	n ₁	n ₂					
		Lyman	91 nm	1	$2 \rightarrow \infty$					
		Balmer	365 nm	2	$3 \rightarrow \infty$					
		Paschen	820 nm	3	$4 \rightarrow \infty$					

Emission & Absorption



Details

Blackbody Radiation

Unit: Quantum and Particle Physics

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): 15.4.A, 15.4.A.1, 15.4.A.2, 15.4.A.3, 15.4.A.3.i, 15.4.A.3.ii, 15.4.A.3.iii

Mastery Objective(s): (Students will be able to...)

• Describe the electromagnetic radiation emitted by an object due to its temperature.

Success Criteria:

• Calculations are correct

Language Objectives:

• Be able to explain and draw & label representations of an atom.

Tier 2 Vocabulary: atom, charge, nucleus

Notes:

As discussed in the *Thermodynamics* topic starting on page 109, matter contains internal thermal energy, *U*, based on its temperature:

$$U = \frac{3}{2}nRT = \frac{3}{2}Nk_BT$$

where:

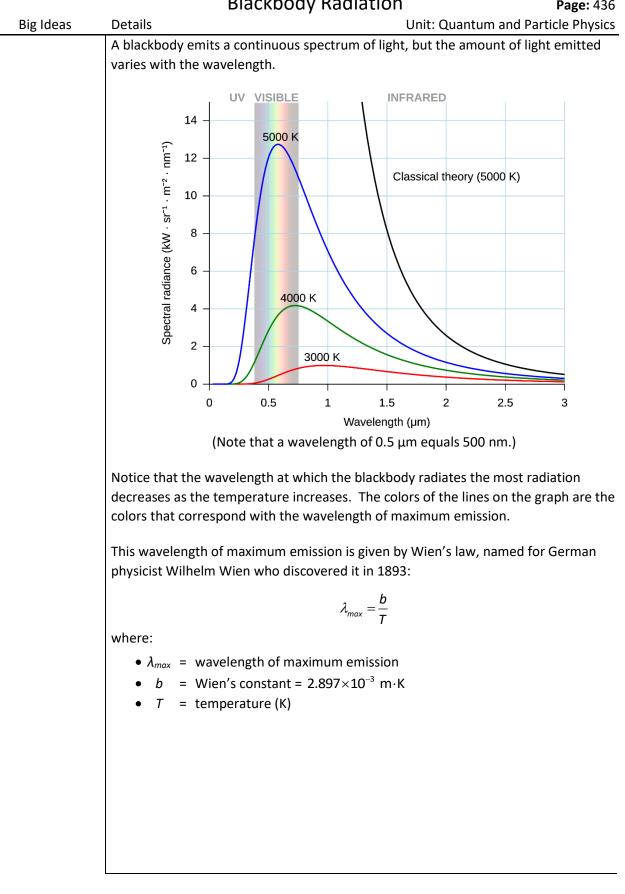
- U = internal thermal energy (J)
- n = number of moles of substance (mol)
- N = number of particles
- R = the gas constant = $8.31 \frac{J}{mol \cdot K}$
- K_B = Boltzmann's constant = $1.38 \times 10^{-23} \frac{J}{K}$
- T = temperature (K)

Matter spontaneously converts some of its internal thermal energy into electromagnetic energy, which radiates from it.

<u>blackbody</u>: an object that absorbs all of the heat energy that comes in contact with it (and reflects none of it).

<u>blackbody radiation</u>: the process of absorbed energy being emitted by a perfect blackbody.

Because a blackbody absorbs all of the radiation energy that falls onto it, if it is in thermal equilibrium (constant temperature), it must emit the same amount of energy as blackbody radiation.



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Big Ideas Details Unit: Quantum and Particle Physics The rate at which energy is emitted from a blackbody is proportional to the surface area of the body and to temperature to the fourth power, as described by the Stefan-Boltzmann law, which was derived theoretically by Ludwig Boltzmann and empirically by Josef Stephan in 1900: $P = \frac{Q}{t} = \sigma A T^4$ where: • P = power(W)• Q = heat (J) • *t* = time (s) • σ = Stefan-Boltzmann constant $\left(\sigma = 5.67 \times 10^{-8} \frac{W}{m^2 \cdot K^4}\right)$ • $A = area (m^2)$ • T = temperature (K) <u>Stefan-Boltzmann constant</u> (σ): the constant that makes the above equation come out in watts. Note that the Stefan-Boltzmann constant is defined from other constants: $\sigma = \frac{2\pi^5 k_B^4}{15h^3 c^2}$, where k_B is the Boltzmann constant, *h* is Planck's constant, and *c* is the speed of light in a vacuum. $j/W_{i} m^{-2}$ 5×10^{8} 4×10^{8} power per unit area (P/A) Stefan-Boltzmann Law 3×10^{8} 2×10^{8} Wien's Law approximation 1×10^{8} 0 2000 4000 6000 8000 1×10^{4} T/K

temperature

	Diackbody Natiation Page: 439
Big Ideas	Details Unit: Quantum and Particle Physics
honors	As described in the subsection "Calculating Heat Transfer by Radiation" on page 46,
(not AP [®])	when energy is radiated by a substance that is not an ideal blackbody, we define a
	material-specific constant called emissivity.
	emissivity (ε): a ratio of the amount of heat radiated by a substance to the amount
	of heat that would be radiated by a perfect "blackbody" of the same
	dimensions.
	Emissivity is a dimensionless number (meaning that it has no units, because the
	units cancel), and is specific to the substance.
ļ	This is a the second to favor disting for a second black back as here as
	This gives the equation for radiation from a non-blackbody substance:
l	$P = \frac{Q}{t} = \varepsilon \sigma A T^4$
ļ	where ε is the emissivity, and the other variables are as described above.
:	

Unit: Quantum and Particle Physics

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS4-3

AP® Physics 1 Learning Objectives/Essential Knowledge (2024): 15.5.A, 15.5.A.1, 15.5.A.2, 15.5.A.2.i, 15.5.A.2.ii, 15.5.A.3, 15.5.A.3.i, 15.5.A.3.ii, 15.5.A.3.iii

Mastery Objective(s): (Students will be able to...)

- Explain the photoelectric effect.
- Calculate the work function of an atom and the kinetic energy of electrons emitted.

Success Criteria:

Details

Big Ideas

- Descriptions & explanations account for observed behavior.
- Variables are correctly identified and substituted correctly into the correct equation.
- Algebra is correct with correct units and reasonable rounding.

Language Objectives:

• Explain why a minimum amount of energy is needed in order to emit an electron.

Tier 2 Vocabulary: work function

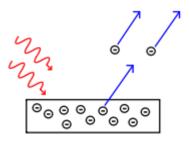
Labs, Activities & Demonstrations:

- threshold voltage to light an LED
- glow-in-the-dark substance and red vs. green vs. blue laser pointer

Notes:

<u>photoelectric effect</u>: the emission of electrons when electromagnetic radiation is incident upon a photoactive material.

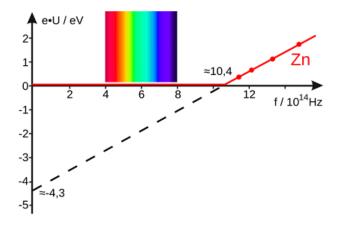
The photoelectric effect was discovered in 1887 when Heinrich Hertz discovered that electrodes emitted sparks more effectively when ultraviolet light was shone on them. We now know that the particles are electrons, and that ultraviolet light of sufficiently high frequency (which varies from element to element) causes the electrons to be emitted from the surface of the element.



The photoelectric effect requires light with a sufficiently high frequency, because the frequency of the light is related to the amount of energy it carries. The energy of the photons needs to be above a certain *threshold frequency* in order to have enough energy to ionize the atom.

Note that the emission of electrons depends only upon the energy of the photons, not on the number of photons.

For example, a minimum frequency of 10.4×10^{14} Hz is needed to dislodge electrons from a zinc atom:



The maximum kinetic energy of the emitted electron is equal to Planck's constant times the difference between the frequency of incident light (f) and the minimum threshold frequency of the element (f_o) :

$$K_{max} = h(f - f_o)$$

The quantity hf_o is called the "work function" of the atom, and is denoted by the variable ϕ . Thus, the kinetic energy equation can be rewritten as:

$$K_{max} = hf - \phi$$

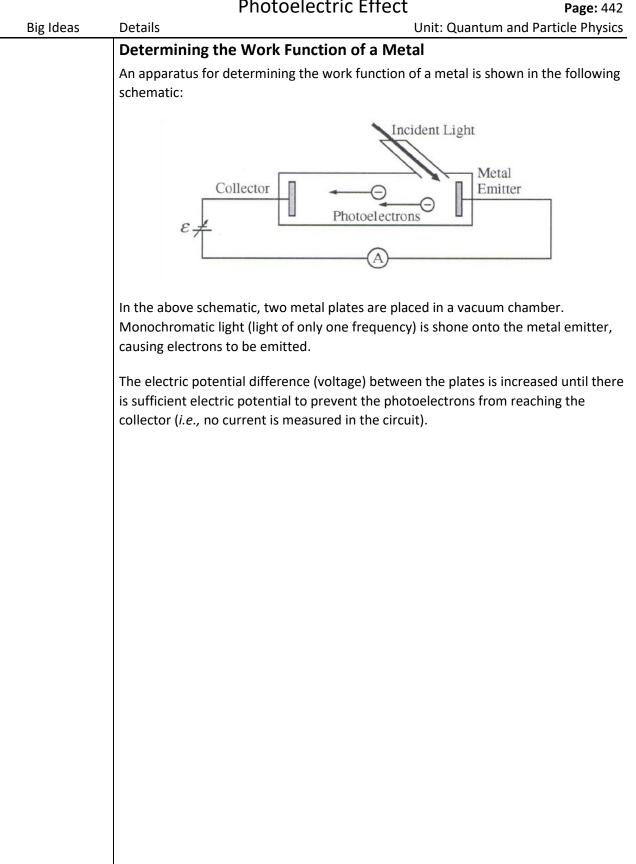
Values of the work function for different elements range from about 2.3–6 eV. (1 eV = 1.6×10^{-19} J)

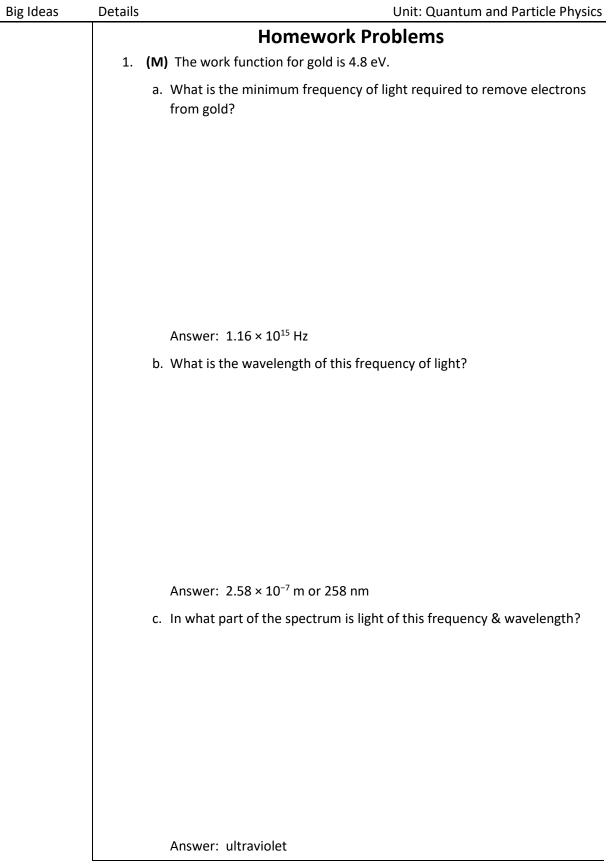
The importance of this discovery was that it gave rise to the idea that light can behave both as a wave and as a particle.

In 1905, Albert Einstein published a paper explaining that the photoelectric effect was evidence that energy from light was carried in discrete, quantized packets. This discovery, for which Einstein was awarded the Nobel prize in physics in 1921, led to the birth of the field of quantum physics.

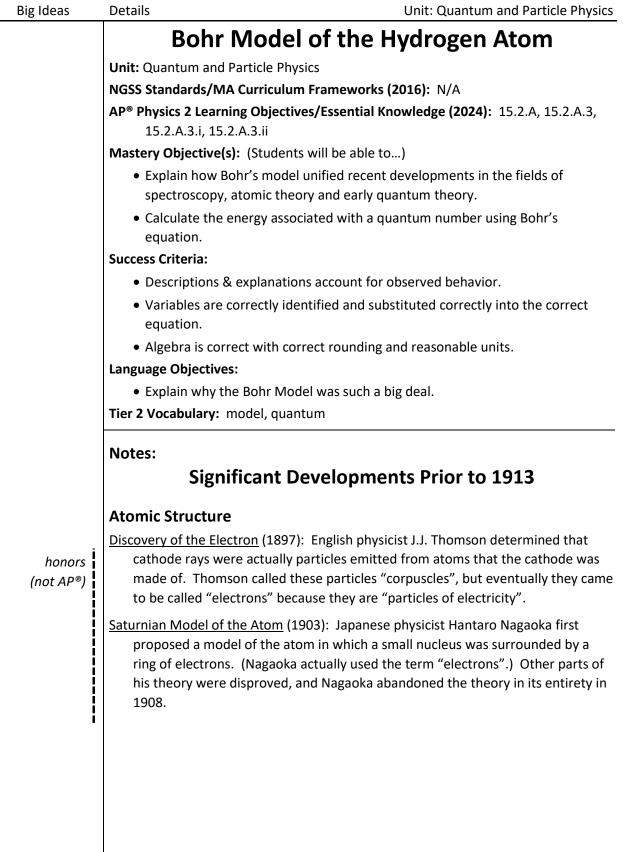
Big Ideas

Details





Big Ideas	Details	Unit: Quantum and Particle Physics
	2.	(S) A beam of light from a 445 nm blue laser pointer contains how much
		energy?
		Answer: 4.45×10^{-19} J or 2.78 eV
	3.	(M) Photons of energy 6 eV cause electrons to be emitted from an unknown metal with a kinetic energy of 2 eV. If photons of twice the wavelength are incident on this metal, what will be the energy of the emitted electrons 2. (If
		incident on this metal, what will be the energy of the emitted electrons? (If no electrons are emitted, explain why.)
		Answer: no electrons will be emitted.



Bohr Model of the Hydrogen Atom

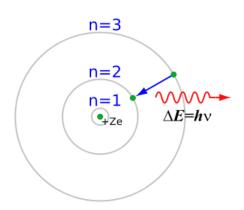
Big Ideas	Details Unit: Quantum and Particle Physics
	Discovery of the Atomic Nucleus (1906–1911): English physicists Hans Geiger and Ernest Marsden working under the direction Ernest Rutherford at the University of Manchester performed a series of scattering experiments that involved passing a beam of charged alpha particles through a thin sheet of gold foil. Most of the particles passed through unimpeded, but some were deflected, and a few were deflected sharply. These experiments confirmed the hypothesis that atoms contain a dense, positively charged nucleus that comprises most of the atom's mass, which is surrounded by negatively-charged electrons.
	Early Quantum Theory
	quantum: an elementary unit of energy.
	In 1900, German physicist Max Planck published the Planck postulate, stating that electromagnetic energy could be emitted only in quantized form, <i>i.e.</i> , only certain "allowed" energy states are possible.
	Plack determined the constant that bears his name as the relationship between the frequency of one quantum unit of electromagnetic wave and its energy. This relationship is the equation:
	E = hf
	where:
	E = energy(J) $h = \text{Planck's constant} = 6.626 \times 10^{-34} \text{ J} \cdot \text{s}$
	$f = \text{frequency}^* (\text{Hz} \equiv \text{s}^{-1})$
	* Most physics texts use the Greek letter v (nu) as the variable for frequency. However, high school texts and the College Board use f, presumably to avoid confusion with the letter "v".



Details

Bohr's Model of the Atom (1913)

In 1913, Danish physicist Niels Bohr combined atomic theory, spectroscopy, and quantum theory into a single unified theory. Bohr hypothesized that electrons moved around the nucleus as in Rutherford's model, but that these electrons had only certain allowed quantum values of energy, which could be described by a quantum number (n). The value of that quantum number was the same n as in Rydberg's equation, and that using quantum numbers in Rydberg's equation could predict the wavelengths of light emitted when the electrons gained or lost energy by moving from one quantum level to another.



Bohr's model gained wide acceptance, because it related several prominent theories of the time. He received a Nobel Prize in physics in 1922 for his work.

The Bohr model is often given short shrift in high school chemistry classes, because it has been superseded by modern quantum theory. However, because Bohr's model unified several fields within physics, it is perhaps one of the most pivotal theories of the early 20th century.

honors (not AP®) Bohr defined the energy associated with a given quantum number (*n*) in terms of Rydberg's constant:

$$E_n = -\frac{R_H}{n^2}$$

Although the model worked well for hydrogen, the equations could not be solved exactly for atoms with more than one electron, because of the additional effects that electrons exert on each other (*e.g.*, the Coulomb force,

$$F_e = \frac{1}{4\pi\varepsilon_o} \frac{q_1 q_2}{r^2}).$$

Details

Wave-Particle Duality

Unit: Quantum and Particle Physics

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS4-3

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 15.1.A, 15.1.A.2,

15.1.A.2.i, 15.1.A.2.ii, 15.1.A.4, 15.1.A.4.i, 15.1.A.4.ii

Mastery Objective(s): (Students will be able to...)

- Explain the de Broglie model of the atom.
- Calculate the de Broglie wavelength of a moving particle such as an electron.

Success Criteria:

• Descriptions & explanations are accurate and account for observed behavior.

Language Objectives:

• Explain the important features of each model of the atom.

Notes:

In 1924, French physicist Louis de Broglie determined that quanta of light could be considered to be particles with very small mass moving at relativistic speeds (*i.e.*, close to the speed of light.)

de Broglie proposed the idea that particles are actually bundles of waves that move with a group velocity and have an effective mass. He concluded that any moving particle or object must therefore be able to be characterized with some periodic

frequency, $f = \frac{E}{h}$, from Planck's equation. This means that the wavelength of any moving object is therefore:

moving object is therefore:

$$\lambda = \frac{h}{p} = \frac{h}{mv}$$

where:

- λ = de Broglie wavelength (m)
- $h = \text{Planck's constant} = 6.626 \times 10^{-34} \text{ J} \cdot \text{s}$
- $p = \text{momentum}(N \cdot s)$
- m = mass (kg)
- $v = \text{velocity}\left(\frac{\text{m}}{\text{s}}\right)$

Although every moving object has a de Broglie wavelength, wavelengths of macroscopic objects are far too small to be detectable.

Tier 2 Vocabulary: model, quantum

Wave-Particle Duality

Big Ideas Details Unit: Quantum and Particle Physics de Broglie theorized that if electrons behaved as waves as well as particles, then the reason that only certain wavelengths were possible was because the wave produced by an electron would only be stable if it were a standing wave, meaning that its path length as it orbited the nucleus must be an integer multiple of the wavelength. not allowed allowed Different quantum amounts of energy were possible with de Broglie's theory, but were restricted to amounts that produced an integer number of wavelengths. n = 6 n = 3 n = 4 n = 5 **Photons** photon: a particle of light. Photons have no mass and are electrically neutral. Photons move at a constant velocity, called the "speed of light". The speed of light, denoted by the variable c (because it is constant) depends on the medium that the photons are traveling through. In a vacuum, the speed of light is $c = 3.00 \times 10^8 \frac{\text{m}}{\text{s}}$. As described in the topic *Refraction*, starting on page 384, the speed of photons through other media is proportional to the index of refraction of the medium: $n = \frac{c}{v}$ Note that the idea that photons exhibit wave-like behavior did not originate with de Broglie. Recall that Thomas Young's double-slit experiment in 1801 demonstrated that light exhibited wave-like properties. (See Wave Interactions starting on page 321.)

Wave-Particle Duality

Big Ideas	Details	Unit: Quantum and Particle Physics
		Homework Problems
	1.	(M) What is the de Broglie wavelength associated with an electron moving at 0.5 <i>c</i> ? (You will need to look up the mass of the electron and the speed of light in a vacuum in <i>Table FF. Constants Used in Nuclear Physics</i> on page 513 of your Physics Reference Tables.)
		Answer: 4.8×10^{-12} m = 0.0048 nm
	2.	(M) How fast would that same electron need to be moving in order to produce a wavelength of visible light of 500 nm (which equals 5×10^{-7} m)?
		Answer: $1450\frac{m}{s}$

Details

Quantum Mechanical Model of the Atom

Unit: Quantum and Particle Physics

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS4-3

AP[®] Physics 2 Learning Objectives/Essential Knowledge (2024): 15.1.A, 15.1.A.1,

15.1.A.1.i, 15.1.A.1.ii, 15.1.A.2, 15.1.A.2.i, 15.1.A.2.ii, 15.1.A.3, 15.1.A.3.i, 15.1.A.3.ii

Mastery Objective(s): (Students will be able to ...)

- Explain the de Broglie model of the atom.
- Explain the Schrödinger model of the atom.
- Explain the wave-particle duality of nature.

Success Criteria:

• Descriptions & explanations are accurate and account for observed behavior.

Language Objectives:

• Explain the important features of each model of the atom.

Tier 2 Vocabulary: model, quantum

Notes:

In 1925, following de Broglie's research, Austrian physicist Erwin Schrödinger found that by treating each electron as a unique wave function, the energies of the electrons could be predicted by the mathematical solutions to this wave function.

Schrödinger used the wave function as the basis of an equation that defined a probability map for where the electrons could be found in an atom as a function of position and time. Schrödinger's work is the basis for the modern quantum-mechanical model of the atom.

Ouantum Mechanical Model of the Atom

	Quantum Mechanical I	Model of the Atom Page: 452
Big Ideas	Details	Unit: Quantum and Particle Physics
Big Ideas	Details To understand the probability map, it is important to realize that because the electron acts as a wave, it is detectable when the amplitude of the wave is nonzero, but not detectable when the amplitude is zero. This makes it appear as if the electron is teleporting from place to place around the atom. If you were somehow able to take a time-lapse picture of an electron as it moves around the nucleus, the picture might look something like the diagram to the right. Notice that there is a region close to the nucleus where the electron is unl where there is a high probability of fi As you get farther and farther from th different shapes for these probability are called "orbitals," because of their the planetary model. Schrödinger was awarded the Nobel p The implications of quantum theory a shapes and numbers of orbitals in an and physical properties and its location means quantum mechanics is respon	Unit: Quantum and Particle Physics

Compton Scattering

Unit: Quantum and Particle Physics

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 15.6.A, 15.6.A.1, 15.6.A.2, 15.6.A.2.ii, 15.6.A.2.ii, 15.6.A.3

Mastery Objective(s): (Students will be able to ...)

• Describe the interaction between photons and matter using Compton scattering.

Success Criteria:

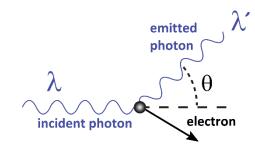
• Descriptions & explanations are accurate and account for observed behavior.

Language Objectives:

• Explain the important features of each model of the atom.

Notes:

In 1923, American physicist Arthur Compton performed an experiment in which a photon collided with an electron. The collision caused a transfer of momentum and energy to the electron, which therefore caused the photon to emerge with less momentum and less energy (and therefore a different frequency and wavelength).



This experiment proved that photons exhibit particle behavior and cannot be considered to be only waves.

Tier 2 Vocabulary: scattering

Compton Scattering

Applying the equations:

$$E = hf$$
 and $\lambda = \frac{h}{p} = \frac{h}{m_e c}$

gives the following equation:

$$\Delta \lambda = \frac{h}{m_e c} (1 - \cos \theta)$$

where:

Details

Big Ideas

- $\Delta \lambda$ = change in wavelength between the incident photon and the emitted photon
- $h = \text{Planck's constant} = 6.63 \times 10^{-34} \text{ J} \cdot \text{s}$
- m_e = mass of an electron = 9.11×10⁻³¹ kg
- c = speed of light = $3.00 \times 10^8 \frac{\text{m}}{\text{s}}$
- θ = angle of emitted photon relative to direction of incident photon

Unit: Quantum and Particle Physics

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 15.7.A.1

Mastery Objective(s): (Students will be able to ...)

• Name, describe, and give relative magnitudes of the four fundamental forces of nature.

Success Criteria:

Details

Big Ideas

• Descriptions & explanations are accurate and account for observed behavior.

Language Objectives:

• Explain why the gravitational force is more relevant than the electromagnetic force in astrophysics.

Tier 2 Vocabulary: model, quantum

Notes:

All forces in nature ultimately come from one of the following four forces:

strong force (or "strong nuclear force" or "strong interaction"): an attractive force between quarks. The strong force holds the nuclei of atoms together. The energy comes from converting mass to energy.

Effective range: about the size of the nucleus of an average-size atom.

<u>weak force</u> (or "weak nuclear force" or "weak interaction"): the force that causes protons and/or neutrons in the nucleus to become unstable and leads to beta nuclear decay. This happens because the weak force causes an up or down quark to change its flavor. (This process is described in more detail in the section on the *Standard Model* of Particle Physics, starting on page 456.) **Relative Strength**: 10^{-6} to 10^{-7} times the strength of the strong force. **Effective range**: about 1/3 the diameter of an average nucleus.

<u>electromagnetic force</u>: the force between electrical charges. If the charges are the same ("like charges")—both positive or both negative—the particles repel each other. If the charges are different ("opposite charges")—one positive and one negative—the particles attract each other.

Relative Strength: about $1/_{137}$ as strong as the strong force.

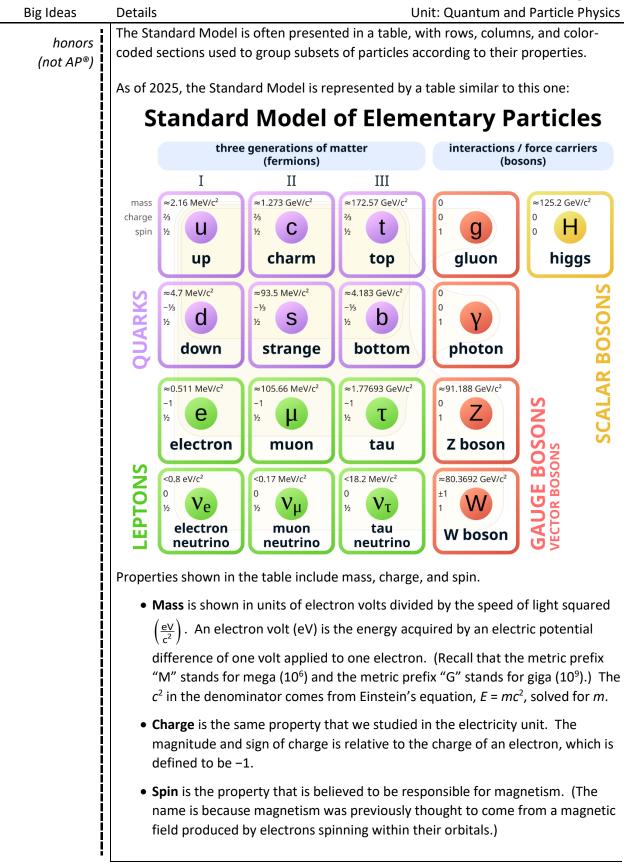
Effective range: ∞ , but gets smaller as (distance)².

<u>gravitational force</u>: the force that causes masses to attract each other. Usually only observable if one of the masses is very large (like a planet).

Relative Strength: only 10^{-39} times as strong as the strong force.

Effective range: ∞ , but gets smaller as (distance)².

Big Ideas	Standard ModelPage: 4DetailsUnit: Quantum and Particle Phys
big lueas	Standard Model
	Unit: Quantum and Particle Physics
	NGSS Standards/MA Curriculum Frameworks (2016): N/A
	AP [®] Physics 2 Learning Objectives/Essential Knowledge (2024): 15.8.A.1.ii, 15.8.A.1.iii
	Mastery Objective(s): (Students will be able to)
	 Name and describe the particles of the Standard Model.
	• Describe interactions between particles, according to the Standard Model.
	Success Criteria:
	• Descriptions & explanations are accurate and account for observed behavior Language Objectives:
	• Explain the important features of each model of the atom.
	Tier 2 Vocabulary: model, quantum
	Notes:
<u>.</u>	The Standard Model is a theory of particle physics that:
honors	 identifies the particles that matter is ultimately comprised of
(not AP®)	 describes properties of these particles, including their mass, charge, and spi
	 describes interactions between these particles
i	• describes interactions between these particles
	The Standard Model dates to the mid-1970s, when the existence of quarks was fir experimentally confirmed. Physicists are still discovering new particles and relationships between particles, so the model and the ways it is represented are evolving, much like atomic theory and the Periodic Table of the Elements was evolving at the turn of the twentieth century. The table and the model described these notes represent our understanding, as of 2025. By the middle of this centur the Standard Model may evolve into a form that is substantially different from the way we represent it today.
	The Standard Model in its present form does not incorporate dark matter, dark energy, or gravitational attraction.



Standard Model

Physics 2 In Plain English

Page: 457

honors (not AP®)

Big Ideas

Fundamental Particles

Quarks

Details

Quarks are particles that participate in strong interactions (sometimes called the "strong force") through the action of "color charge" (which will be described later). Because protons and neutrons (which make up most of the mass of an atom) are made of three quarks each, quarks are the subatomic particles that make up most of the ordinary matter^{*} in the universe.

- quarks have color charge (*i.e.*, they interact via the strong force)
- quarks have spin of $\pm \frac{1}{2}$
- "up-type" quarks carry a charge of $+\frac{2}{3}$; "down-type" quarks carry a charge of $-\frac{1}{3}$.

There are six flavors[†] of quarks: up and down, charm and strange, and top and bottom. (Originally, top and bottom quarks were called truth and beauty.)

Leptons

Leptons are the smaller particles that make up most matter. The most familiar lepton is the electron. Leptons participate in "electroweak" interactions, meaning combinations of the electromagnetic and weak forces.

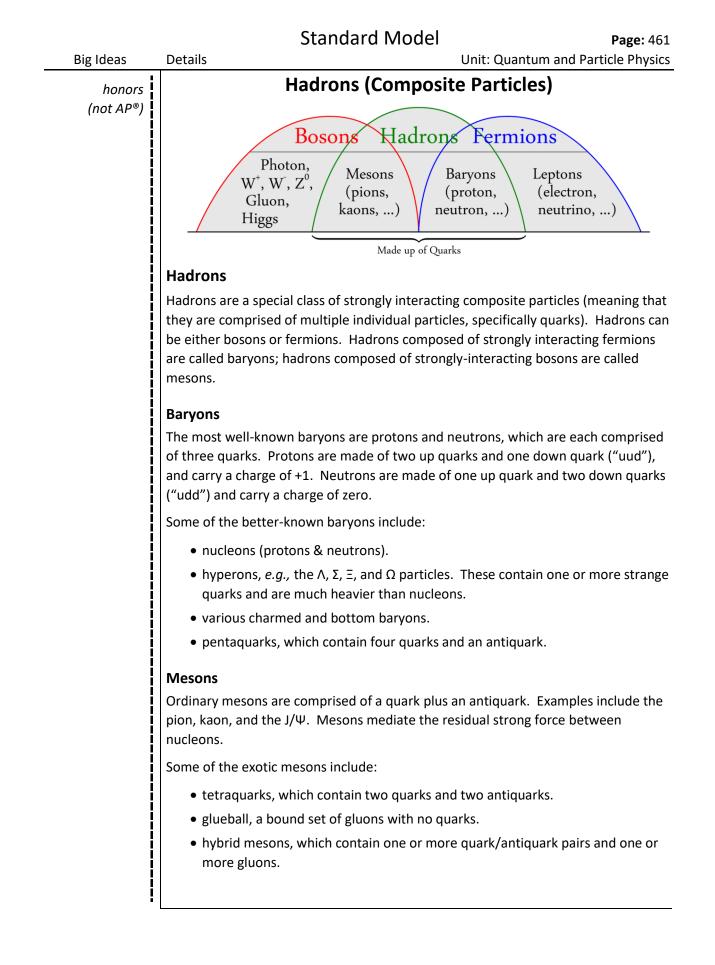
- leptons do not have color charge (*i.e.,* they do not interact via the strong force)
- leptons have spins of $+\frac{1}{2}$
- electron-type leptons have a charge of -1; neutrinos do not have a charge.
- neutrinos (v) and antineutrinos (v) have no electrical charge, and negligible mass. Moreover, neutrinos oscillate, which makes their mass indefinite. Because neutrinos are leptons (which do not interact with the strong force) and they have no charge, they interact with only the weak and gravitational forces, which means neutrinos have very little interaction with normal matter.

^{*} Matter that is not "ordinary matter" is called "dark matter", whose existence is theorized but not yet proven.

⁺ Yes, "flavors" really is the correct term.

Details Unit: Quantum and Particle Physics					
Gauge Bosons Gauge bosons are the particles that carry force—their interactions are responsible for the fundamental forces of nature: the strong force, the weak force, the electromagnetic force and the gravitational force. The hypothetical particle responsible for the gravitational force is the graviton, which has not yet been detected (as of 2025).					
 photons are responsible for the electromagnetic force. 					
 gluons are responsible for the strong interaction (strong force) 					
• W and Z bosons are responsible for the weak interaction (weak force)					
Scalar Bosons					
At present, the only scalar boson we know of is the Higgs boson, theorized in 1964 by Peter Higgs and discovered in 2012, which is responsible for mass.					
The Higgs boson interacts with a force field called the Higgs field. The Higgs field causes Higgs bosons to interact with other particles (such as quarks and electrons) to resist changes in their motion. We call this resistance "inertia", which is the basis for Newton's first law (which you studied in Physics 1). The more particles a substance has that can interact with Higgs bosons, the more inertia it has. Recall that translational inertia is the same thing as mass, which is why we say that the Higgs boson is responsible for particles having mass.					
Classes of Particles					
Bosons Fermions Photon, W ⁺ , W ⁻ , Z ⁰ , Gluon, Higgs Mesons (pions, kaons,) Baryons (proton, neutron,) Leptons (electron, neutrino,) Bosons Bosons (the right columns in the table of the Standard Model) are described by Bose-Einstein statistics, have integer spins and do not obey the Pauli Exclusion Principle. Interactions between bosons are responsible for forces and mass.					

	Standard Would Page: 460
Big Ideas	Details Unit: Quantum and Particle Physics
honors	Fermions
(not AP®)	Quarks and leptons (the left columns in the table of the Standard Model) are fermions. Fermions are described by Fermi-Dirac statistics and obey the Pauli exclusion principle (which states that no two particles in an atom may have the same exact set of quantum numbers—numbers that describe the energy states of the particle).
	Fermions are the building blocks of matter. They have a spin of ½, and each fermion has its own antiparticle (see below).
	Antiparticles
	Each particle in the Standard Model has a corresponding antiparticle. Like chemical elements in the Periodic Table of the Elements, fundamental particles are designated by their symbols in the table of the Standard Model. Antiparticles are designated by the same letter, but with a line over it. For example, an up quark would be designated "u", and an antiup quark would be designated " \overline{u} ".
	The antiparticle of a fermion has the same name as the corresponding particle, with the prefix "anti-", and has the opposite charge. <i>E.g.</i> , the antiparticle of a tau neutrino is a tau antineutrino. (However, for historical reasons an antielectron is usually called a positron.) <i>E.g.</i> , up quark carries a charge of $+\frac{2}{3}$, which means an antiup quark carries a charge of $-\frac{2}{3}$.
	Each of the fundamental bosons <i>is</i> its own antiparticle, except for the W ⁻ boson, whose antiparticle is the W ⁺ boson.
	When a particle collides with its antiparticle, the particles annihilate each other, and their mass is converted to energy ($E = mc^2$) and released.



Standard Model

honors	
(not AP®)	

Details

Big Ideas

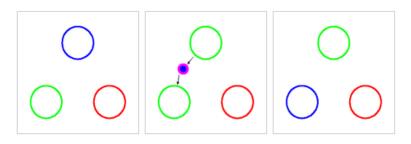
Color Charge and Quantum Chromodynamics (QCD)

Quantum chromodynamics (QCD) is the study of the strong interaction between quarks, which is mediated by gluons. Color charge is the property that is responsible for the strong nuclear interaction. All electrons and fermions (particles that have half-integer spin quantum numbers) must obey the Pauli Exclusion Principle, which states that no two particles within the same larger particle (such as a hadron or atom) can have identical sets of quantum numbers.

For electrons, (as you should have learned in chemistry), if two electrons share the same orbital, they need to have opposite spins. In the case of quarks, all quarks have a spin of $+\frac{1}{2}$, so in order to satisfy the Pauli Exclusion Principle, if a proton or neutron contains three quarks, there has to be some other quantum property that has different values for each of those quarks. This property is called "color charge" (or sometimes just "color^{*}").

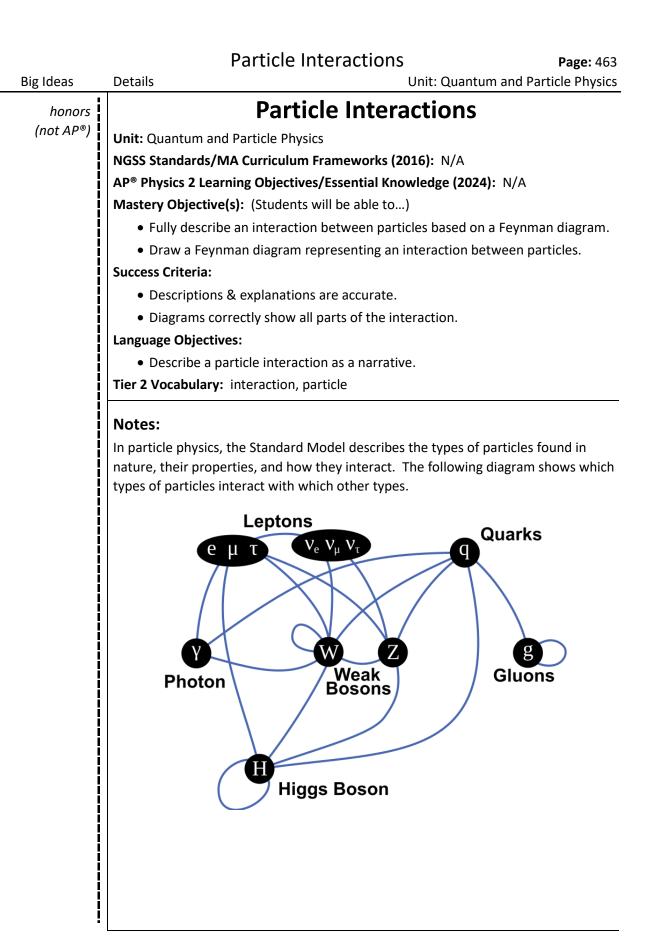
The "color" property has three values, which are called "red," "green," and "blue" (named after the primary colors of light). When there are three quarks in a subatomic particle, the colors have to be different and have to add up to "colorless". (Recall that combining each of the primary colors of light produces white light, which is colorless.)

Quarks can exchange color charge by emitting a gluon that contains one color and one anticolor. Another quark absorbs the gluon, and both quarks undergo color change. For example, suppose a blue quark emits a blue antigreen gluon:



You can imagine that the quark sent away its own blue color (the "blue" in the "blue antigreen" gluon). Because it also sent out antigreen, it was left with green, so it became a green quark. Meanwhile, the antigreen part of the gluon finds the green quark and cancels its color. The blue from the blue antigreen gluon causes the receiving quark to become blue. After the interaction, the particle once again has one red, one green, and one blue quark, which means color charge is conserved.

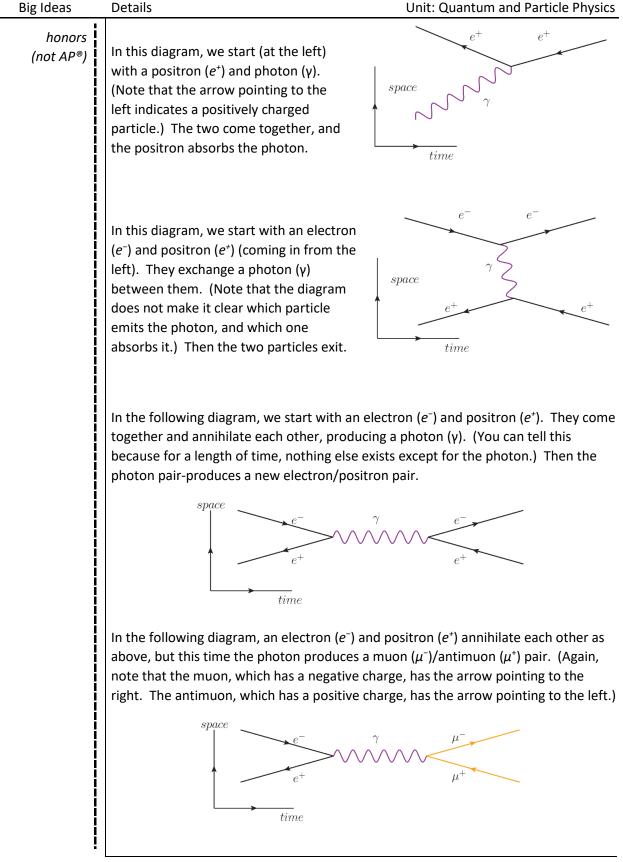
^{*} Just like "spin" is the name of a property of energy that has nothing to do with actual spinning, "color" is a property that has nothing to do with actual color. In fact, quarks couldn't possibly have actual color—the wavelengths of visible light are thousands of times larger than quarks!



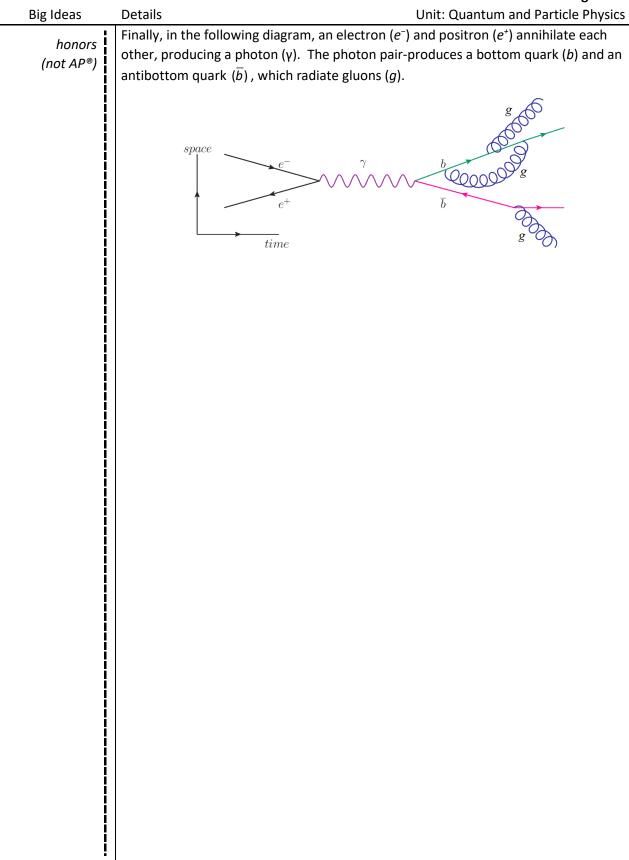
Particle Interactions

	Particle Interactions Page: 464
Big Ideas	Details Unit: Quantum and Particle Physics
honors (not AP®)	Specific interactions between particles can be shown pictorially in diagram called a Feynman diagram, named for American physicist Richard Feynman. The Feynman diagram tells the "story" of the interaction.
İ	The characteristics of a Feynman diagram are:
	 Straight lines represent the motion of a particle, such as an electron or positron. The arrow points to the right for a negatively charged particle, and to the left for a positively-charged particle.
İ	2. A wavy line represents a photon (γ).
İ	3. A coiled line (like a spring) represents a gluon (g).
	 The x-axis is time. The interaction starts (in terms of time) on the left and proceeds from left to right.
	 The y-axis represents space. Lines coming together represent particles coming together. Lines moving apart represent particles moving away from each other. (Note that <i>the diagram is not a map</i>; particles can move together or apart in any direction.)
	6. Each vertex, where two or more lines come together, represents an interaction.
	Probably the best way to explain the diagrams is with examples.
	In this diagram, we start (at the left) with an electron (e^-) and photon (γ). The two come together, and the electron absorbs the photon.
	In this diagram, we start (at the left) with an electron (e^{-}) by itself. The electron emits a photon (γ) but is otherwise unchanged.

Particle Interactions



Particle Interactions



	Introduction: Atomic and Nuclear Physics Page: 46
ig Ideas	Details Unit: Atomic and Nuclear Physic
	Introduction: Atomic and Nuclear Physics
	Unit: Atomic and Nuclear Physics
	Topics covered in this chapter:
	Radioactive Decay470
	Nuclear Equations475
	Binding Energies & Mass Defect478
	Half-Life
	Nuclear Fission & Fusion488
	Practical Uses for Nuclear Radiation491
	This chapter discusses the particles that atoms and other matter are made of, how those particles interact, and the process by which radioactive decay can change the composition of a substance from one element into another.
	 Radioactive Decay and Nuclear Equations describe the process of radioactive decay and how to predict the results.
	• Mass Defect & Binding Energy uses Einstein's equation $E = mc^2$ to determine the energy that was converted to mass in order to hold the nucleus of an ato together.
	 Half-Life explains how to calculate the rate at which radioactive decay happens and the amount of material remaining.
	 Nuclear Fission & Fusion and Practical Uses for Nuclear Radiation describe ways that radioactive materials are used to produce energy or otherwise provide benefits to society.
	One of the challenges of this chapter is remembering concepts from chemistry, including numbers of protons, neutrons and electrons, and how to use the Periodic Table of the Elements.
	Standards addressed in this chapter:
	Massachusetts Curriculum Frameworks (2016):
	HS-PS1-8 : Develop a model to illustrate the energy released or absorbed during the processes of fission, fusion, and radioactive decay.
AP [®] only	AP [®] Physics 2 Learning Objectives/Essential Knowledge (2024):
	15.7.A : Describe the physical properties that constrain the behavior of
	interacting nuclei, subatomic particles, and nucleons.

Introduction: Atomic and Nuclear Physics

conservation of nucleon number.

- 15.7.A.3: The behavior of the constituent particles of a nuclear reaction is constrained by laws of conservation of energy, energy-mass equivalence, and conservation of momentum.
- 15.7.A.4: For all nuclear reactions, mass and energy may be exchanged due to mass-energy equivalence.
- 15.7.A.5: Energy may be released in nuclear processes in the form of kinetic energy of the products or as photons.
- 15.7.A.6: Nuclear fusion is the process by which two or more smaller nuclei combine to form a larger nucleus, as well as subatomic particles.

15.7.A.7: Nuclear fission is the process by which the nucleus of an atom splits into two or more smaller nuclei, as well as subatomic particles.

15.7.A.8: Nuclear fission may occur spontaneously or may require an energy input, depending on the binding energy of the nucleus.

15.7.B: Describe the radioactive decay of a given sample of material consisting of a finite number of nuclei.

15.7.B.1: Radioactive decay is the spontaneous transformation of a nucleus into one or more different nuclei.

15.7.B.1.i: The time at which an individual nucleus undergoes radioactive decay is indeterminable, but decay rates can be described using probability

15.7.B.1.ii: The half-life, $t_{\frac{1}{2}}$, of a radioactive material is the time it takes for half of the initial number of radioactive nuclei to have spontaneously decayed.

15.7.B.1.iii: The decay constant can be related to the half-life of a

radioactive material with the equation $\lambda = \frac{\ln 2}{t_{\chi}}$.

- 15.7.B.2: A material's decay constant may be used to predict the number of nuclei remaining in a sample after a period of time, or the age of a material if the initial amount of material is known.
- 15.7.B.3: Different unstable elements and isotopes may have vastly different half-lives, ranging from fractions of a second to billions of years.

Big Ideas

AP[®] only

Details

Introduction: Atomic and Nuclear Physics

Introduction: Atomic and Nuclear PhysicsPage: 469DetailsUnit: Atomic and Nuclear Physics
15.8.A : Describe the processes by which individual nuclei decay.
15.8.A.1 : Some processes by which nuclei decay emit subatomic particles with unique properties.
15.8.A.1.i : An alpha particle, or helium nucleus, consists of two neutrons and two protons and is symbolized by α or He ²⁺ .
15.8.A.1.ii : Neutrinos and antineutrinos are subatomic particles that have no electrical charge, have negligible mass, and are symbolized by ν and $\overline{\nu}$, respectively.
15.8.A.1.iii : Neutrinos and antineutrinos only interact with matter via the weak force and the gravitational force, which results in very little interaction with normal matter.
15.8.A.1.iv : Positrons, or antielectrons, are subatomic particles that have an electric charge opposite that of an electron, have the same mass as an electron, and are symbolized by e^+ or β +.
15.8.A.2 : Nuclei can undergo radioactive decay via alpha decay, beta-minus decay (β –), beta-plus decay (β +), and gamma decay (γ).
15.8.A.2.i: In all nuclear decays, nucleon number (the number of neutrons and protons), lepton number (the number of electrons and neutrinos), and charge are conserved.
15.8.A.2.ii: Alpha decay occurs when a nucleus ejects an alpha particle.
15.8.A.2.iii : Beta-minus decay occurs when a neutron changes to a proton by emitting an electron and antineutrino.
15.8.A.2.iv: Beta-plus decay occurs when a proton changes to a neutron by emitting a positron and neutrino.
15.8.A.2.v: Gamma decay occurs after a nucleus has undergone alpha or beta decay and the excited nucleus decays to a lower energy state by emitting a photon.
15.8.A.3 : The type of decay exhibited by a given nucleus is determined by the isotope of the element.

Unit: Atomic, Particle, and Nuclear Physics

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS1-8

- AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 15.8.A, 15.8.A.1,
 - 15.8.A.1.i, 15.8.A.1.iv, 15.8.A.2, 15.8.A.2.i, 15.8.A.2.ii, 15.8.A.2.iii, 15.8.A.2.iv, 15.8.A.2.v, 15.8.A.3

Mastery Objective(s): (Students will be able to...)

- Describe the radioactive decay of a given sample of material consisting of a finite number of nuclei.
- Explain the causes of nuclear instability.
- Explain the processes of α , β -, and β + decay and electron capture.

Success Criteria:

Details

Big Ideas

• Descriptions & explanations are accurate and account for observed behavior.

Language Objectives:

• Explain what happens in each of the four types of radioactive decay.

Tier 2 Vocabulary: decay, capture

Labs, Activities & Demonstrations:

• (old) smoke detector & Geiger counter

Notes:

<u>nuclear instability</u>: When something is unstable, it is likely to change. If the nucleus of an atom is unstable, changes can occur that affect the number of protons and neutrons in the atom.

Note that when this happens, the nucleus ends up with a different number of protons. This causes the atom to literally turn into an atom of a different element. When this happens, the physical and chemical properties instantaneously change into the properties of the new element!

<u>radioactive decay</u>: the process by which the nucleus of an atom changes, transforming the element into a different element or isotope.

<u>nuclear equation</u>: an equation describing (through chemical symbols) what happens to an atom as it undergoes radioactive decay.

honors (not AP®)

Big Ideas

Causes of Nuclear Instability

Two of the causes of nuclear instability are:

Size

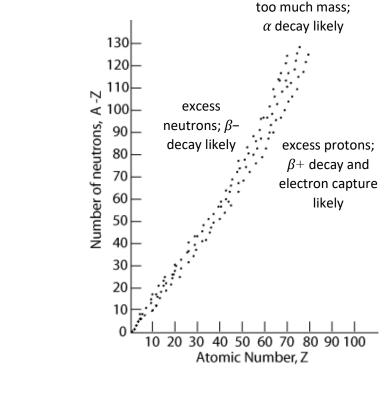
Details

Because the strong force acts over a limited distance, when nuclei get too large (more than 82 protons), it is no longer possible for the strong force to keep the nucleus together indefinitely. The form of decay that results from an atom exceeding its stable size is called alpha (α) decay.

The Weak Nuclear Force

The weak force is caused by the exchange (absorption and/or emission) of W and Z bosons. This causes a down quark to change to an up quark or vice versa. The change of quark flavor has the effect of changing a proton to a neutron, or a neutron to a proton. (Note that the action of the weak force is the only known way of changing the flavor of a quark.) The form of decay that results from the action of the weak force is called beta (θ) decay.

<u>band of stability</u>: isotopes with a ratio of protons to neutrons that results in a stable nucleus (one that does not spontaneously undergo radioactive decay). This observation suggests that the ratio of up to down quarks within the nucleus is somehow involved in preventing the weak force from causing quarks to change flavor.



	Radioactive Decay Page: 472
Big Ideas	Details Unit: Atomic and Nuclear Physics
	alpha (α) decay: a type of radioactive decay in which the nucleus loses two protons
	and two neutrons (an alpha particle). An alpha particle is a ${}^4_2\text{He}^{2+}$ ion (the
	nucleus of a helium-4 atom), with two protons, a mass of 4 amu, and a charge of +2. For example:
	$^{238}_{92}U \rightarrow ^{234}_{90}Th + ^{4}_{2}He$
	Atoms are most likely to undergo alpha decay if they have an otherwise stable proton/neutron ratio but a large atomic number.
	Alpha decay is rare in elements with an atomic number less than 73 (tantalum).
	<u>Net effects of α decay:</u>
	 Atom loses 2 protons and 2 neutrons (atomic number goes down by 2 and mass number goes down by 4)
	• An α particle (a ${}^{4}_{2}$ He $^{+2}$ ion) is ejected from the nucleus at high speed.
	beta minus (β -) decay: a type of radioactive decay in which a neutron is converted to a proton and the nucleus ejects a high speed electron (${}_{-1}^{0}e$).
	Note that a neutron consists of one up quark and two down quarks (udd), and a proton consists of two up quarks and one down quark (uud). When β - decay occurs, the weak force causes one of the quarks changes its flavor from down to up, which causes the neutron (uud) to change into a proton (udd). Because a proton was gained, the atomic number increases by one. However, because the proton used to be a neutron, the mass number does not change. For example:
	$^{32}_{15}P \rightarrow ^{32}_{16}S + ^{0}_{-1}e$
	Atoms are likely to undergo β - decay if they have too many neutrons and not enough protons to achieve a stable neutron/proton ratio. Almost all isotopes that are heavier than isotopes of the same element within the band of stability (because of the "extra" neutrons) undergo β - decay.
	<u>Net effects of β- decay:</u>
	 Atom loses 1 neutron and gains 1 proton (atomic number goes up by 1; mass number does not change)
	• A β - particle (an electron) is ejected from the nucleus at high speed.
	Note that a β - particle is assigned an atomic number of -1. This does not mean an electron is some sort of "anti-proton". The -1 is just used to make the

Big Ideas	Details	Unit: Atomic and Nuclear Physics
	beta plus (β +) decay: a type of rad	ioactive decay in which a proton is converted to a
	neutron and the nucleus ejects	a high speed antielectron (positron, $\int_{+1}^{0} e$).
	occurs, one of the quarks chan proton (uud) into a neutron (u	decay is the opposite of β - decay When β + decay ges its flavor from up to down, which changes the dd). Because a proton was lost, the atomic wever, because the neutron used to be a proton, nge. For example:
		$^{23}_{12}\text{Mg} \rightarrow ^{23}_{11}\text{Na} + ^{0}_{+1}e$
	enough neutrons to achieve a	decay if they have too many protons and not stable neutron/proton ratio. Almost all isotopes es of the same element that fall within the band ons") undergo β + decay.
	<u>Net effects of β+ decay:</u>	
	 Atom loses 1 proton an 1; mass number does not 	d gains 1 neutron (atomic number goes down by ot change)
	 A β+ particle (an antiele high speed. 	ctron or positron) is ejected from the nucleus at
	"captures" an electron from th into the nucleus. This process	f "K-capture"): when the nucleus of the atom e innermost shell (the K-shell) and incorporates it is exactly the reverse of β – decay; during electron r from up to down, which changes a proton (uud)
		$^{23}_{12}Mg + {}^{0}_{-1}e \rightarrow {}^{23}_{11}Na$
		In capture produce the same products. Electron of the often) occur without β + decay. However, β + by electron capture.
	have too many protons and no neutron/proton ratio. Almost	ectron capture (and usually also β + decay) if they t enough neutrons to achieve a stable all isotopes that are lighter than the isotopes of hin the band of stability undergo electron capture,
	Net effects of electron capture	<u>.</u>
	An electron is absorbed	
	 Atom loses 1 proton an 1; mass number does n 	d gains 1 neutron (atomic number goes down by ot change)

Big Ideas	Details	, Unit: Atomic	and Nuclear Physics
	electromagnetic radiation. (F of electromagnetic radiation. mass), they can penetrate far Because gamma rays are not the composition of the nucleo All of the types of radioactiv rays. This means to be comp	a rays, which are very high ener adio waves, visible light, and X-) Because gamma rays are wave into substances and can do a lo particles, emission of gamma ra us. e decay mentioned in these not plete, we would add gamma rad	rgy photons of rays are other types es (which have no ot of damage. ays does not change res also produce γ
	the radioactive decay equati ${}^{238}_{92}U \rightarrow {}^{234}_{90}Th + {}^{4}_{2}He +$ ${}^{23}_{12}Mg \rightarrow {}^{23}_{11}Na + {}^{0}_{+1}e +$	${}^{0}_{0}\gamma \qquad {}^{32}_{15}P \longrightarrow {}^{32}_{16}S + {}^{0}_{-1}\epsilon$	-
honors (not AP®)	(faster = more penetrating) a (heaver = less penetrating):	that radioactive particles can pence is directly related to the veloced ind inversely related to the mass beta particles	ocity of the emission
	gamma rays	beta particles	
	lightest		heaviest
	fastest		slowest
	most penetrating power	leas	t penetrating power
	α 🐩 🛛 🗍 🗍 Α	aper aluminium lead	
		nces (such as lead) do a better jo ons. This is why lead is common ioactive substances.	-

Unit: Atomic and Nuclear Physics

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS1-8

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 15.7.A, 15.7.A.2, 15.7.A.3, 15.7.A.4, 15.7.A.5

Mastery Objective(s): (Students will be able to...)

- Describe the radioactive decay of a given sample of material consisting of a finite number of nuclei.
- Determine the products of α , β -, and β + decay and electron capture.

Success Criteria:

• Equations give the correct starting material and products.

Language Objectives:

• Describe the changes to the nucleus during radioactive decay.

Tier 2 Vocabulary: decay, capture

Notes:

Details

Big Ideas

<u>nuclear equation</u>: a chemical equation describing the process of an isotope undergoing radioactive decay. For example:

 $^{238}_{92}U \rightarrow ^{234}_{90}Th + ^{4}_{2}He$

In a nuclear equation, the atomic number and mass number are conserved on both sides of the arrow. If you look at the bottom (atomic) numbers, and replace the arrow with an = sign, you will have the following:

92 = 90 + 2

Similarly, if you look at the top (mass) numbers, and replace the arrow with an = sign, you will have:

238 = 234 + 4

Nuclear Equations

Big Ideas	Details Unit: Atomic and Nuclear Physics
	Sample problems:
	Q: What are the products of beta-minus (β -) decay of ¹³¹ I?
	A: A β - particle is an electron, which we write as $_{-1}^{0}e$ in a nuclear equation. This
	means 131 I decays into some unknown particle plus ${}^{0}_{-1}e$. The equation is:
	$^{131}_{53}$ I $\rightarrow ^m_p$ X $+ ^0_{-1}$ e
	We can write the following equations for the atomic and mass numbers:
	Atomic #s: $53 = p + -1 \rightarrow p = 54$; therefore, X is Xe
	Mass #s: $131 = m + 0 \rightarrow m = 131$
	Therefore, particle X is $^{131}_{54}$ Xe So our final answer is:
	The two products of decay in this reaction are ${}^{131}_{54}$ Xe and ${}^{0}_{-1}e$.
	Q: Which particle was produced in the following radioactive decay reaction:
	$^{212}_{86}$ Rn $\rightarrow ^{208}_{84}$ Po $+ ^m_p X$
	A: The two equations are:
	Atomic #s: $86 = 84 + p \rightarrow p = 2$; therefore X is He
	Mass #s: $212 = 208 + m \rightarrow m = 4$
	Therefore, particle X is ${}_{2}^{4}$ He, which means it is an α particle.

Nuclear Equations

Homework	Problems
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For these problems, you will need to use a Figure CC. Periodic Table of the Elements (on page 512 of your Physics Reference Tables) and radioactive decay information from *Table EE. Selected Radioisotopes* on page 513 of your Physics Reference Tables.

Give the nuclear equation(s) for radioactive decay of the following:

1. **(M)** ²²²Rn

Details

Big Ideas

2. **(M)** ⁸⁵Kr

3. **(S)** ²²⁰Fr

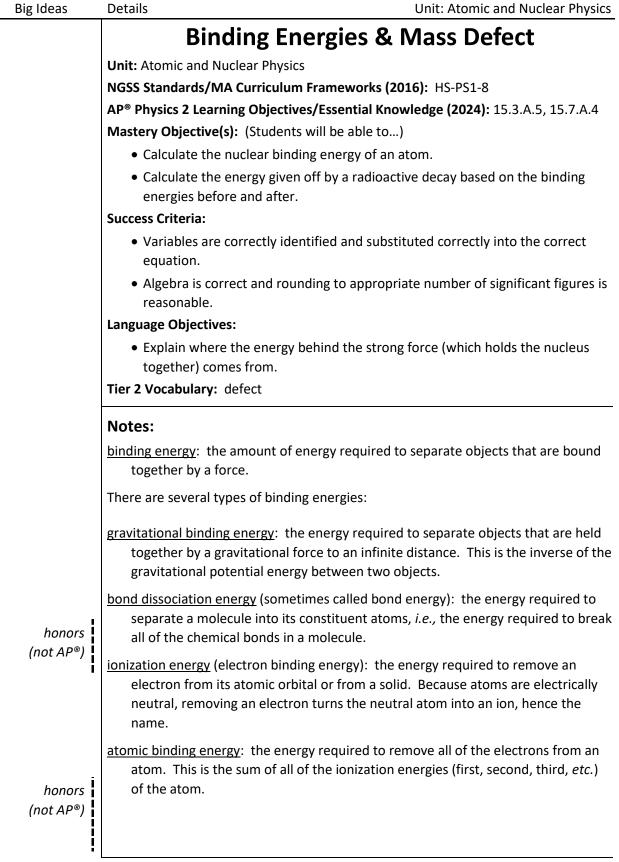
4. **(S)** ³⁷K

5. **(S)** ³H

Give the starting material for the following materials produced by radioactive decay:

6. **(M)** Alpha (α) decay resulting in $\frac{267}{108}$ Hs

7. **(M)** Beta-minus (β -) decay resulting in $\frac{185}{75}$ Re



2: 11	Binding Energies & Mass Defect Page: 479
Big Ideas	Details Unit: Atomic and Nuclear Physics nuclear binding energy: the energy that holds the nucleus of an atom together through the strong nuclear force
	The nuclear binding energy comes from the small amount of mass (the mass defect) that was released as energy when the nucleus was formed, given by the equation:
	$E = mc^2$
	where <i>E</i> is the nuclear binding energy, <i>m</i> is the mass defect, and <i>c</i> is the speed of light $(3 \times 10^8 \frac{\text{m}}{\text{s}})$, which means c^2 is $9 \times 10^{16} \frac{\text{m}^2}{\text{s}^2}$ (a very large number)!
	You can figure out how much energy is produced by spontaneous radioactive decay by calculating the difference in the sum of the nuclear binding energies of the atoms before and after the decay.
honors (not AP®)	<u>quantum chromodynamics (QCD) binding energy</u> : the energy binding quarks together into hadrons. It is the energy of the field of the strong nuclear force, which is mediated by gluons. Most of the mass of hadrons (which include protons and neutrons, and therefore most of the matter in the universe) is actually QCD binding energy.
	<u>mass defect</u> : the difference between the actual mass of an atom, and the sum of the masses of the protons, neutrons, and electrons that it contains. The mass defect is the amount of "missing" mass that was turned into binding energy.
	• A proton has a mass of 1.6726×10^{-27} kg = 1.0073 amu
	 A neutron has a mass of 1.6749×10⁻²⁷ kg = 1.0087 amu
	 An electron has a mass of 9.1094×10⁻³¹ kg = 0.0005486 amu
	To calculate the mass defect, total up the masses of each of the protons, neutrons, and electrons in an atom. The actual (observed) atomic mass of the atom is always <i>less</i> than this number. The "missing mass" is called the mass defect.
4	

Binding Energies & Mass Defect Page: 480

D ¹	Diffulling Effergies & Widss Defect Page: 4	
Big Ideas	Details Unit: Atomic and Nuclear Phys	ICS
honors	ample problem:	
(not AP®)	: Calculate the mass defect of 1 mole of uranium-238.	
	: $\frac{^{238}}{_{92}}$ U has 92 protons, 146 neutrons, and 92 electrons. This means the total ma	ISS
	of one atom of $^{238}_{92}$ U should theoretically be:	
	92 protons × 1.0073 amu = 92.6704 amu	
ļ	146 neutrons × 1.0087 amu = 147.2661 amu	
ł	92 electrons × 0.000 5486 amu = 0.0505 amu	
	92.6704 + 147.2661 + 0.0505 = 239.9870 amu	
	The actual observed mass of one atom of $\frac{238}{92}$ U is 238.0003 amu.	
ļ	The mass defect of one atom of $\frac{^{238}}{_{92}}$ U is therefore	
	239.9870 – 238.0003 = 1.9867 amu.	
	One mole of $\frac{238}{92}$ U would have a mass of 238.0003 g, and therefore a total mass defect of 1.9867 g, or 0.0019867 kg.	S
	Because $E = mc^2$, that means the binding energy of one mole of $^{238}_{92}$ U is:	
	$0.0019867 \text{ kg} \times (3.00 \times 10^8)^2 = 1.79 \times 10^{14} \text{ J}$	
	In case you don't realize just how large that number is, the binding energy of just 238 g (1 mole) of $^{238}_{92}$ U would be enough energy to heat every house on Earth for an entire winter!	
į		
-		

Half-Life

Unit: Atomic and Nuclear Physics

NGSS Standards/MA Curriculum Frameworks (2016): N/A

AP Physics 2 Learning Objectives/Essential Knowledge (2024): 15.7.B, 15.7.B.1,

15.7.B.1.i, 15.7.B.1.ii, 15.7.B.1.iii, 15.7.B.2, 15.7.B.3

Mastery Objective(s): (Students will be able to...)

- Calculate the amount of material remaining after an amount of time.
- Calculate the elapsed time based on the amount of material remaining.

Success Criteria:

- Variables are correctly identified and substituted correctly into the correct equation.
- Algebra is correct and rounding to appropriate number of significant figures is reasonable.

Language Objectives:

• Explain why the mass of material that decays keeps decreasing.

Tier 2 Vocabulary: life, decay

Labs, Activities & Demonstrations:

• half-life of dice or M & M candies

Notes:

The atoms of radioactive elements are unstable, and they spontaneously decay (change) into atoms of other elements.

For any given atom, there is a certain probability, *P*, that it will undergo radioactive decay in a given amount of time. The half-life, τ , is how much time it would take to have a 50% probability of the atom decaying. If you start with *n* atoms, after one half-life, half of them (0.5*n*) will have decayed.

If we started with 32 g of 53 Fe, which has a half-life (7) of 8.5 minutes, we would observe the following:

# minutes	0	8.5	17	25.5	34
# half-lives	0	1	2	3	4
amount left	32 g	16 g	8 g	4 g	2 g

	Half-Life	Page: 482
Big Ideas		omic and Nuclear Physics
	Amount of Material Remain Most half-life problems in a first-year high school physics co number of half-lives and can be solved by making a table like However, on the AP [®] exam you can expect problems that do number of half-lives, and you need to use the exponential do	urse involve a whole e the one above. o not involve a whole
	Because <i>n</i> is decreasing, the number of atoms (and consequence remaining after any specific period of time follows the exponence $N = N_o (\frac{1}{2})^n$	
	where N is the amount you have now, N_o is the amount you the number of half-lives that have elapsed.	u started with, and <i>n</i> is
	Because the number of half-lives equals the total time elaps	ed (t) divided by the
	half-life $t_{\frac{1}{2}}$, we can replace $n = \frac{t}{t_{\frac{1}{2}}}$ and rewrite the equation	on as:
	$N = N_o \left(\frac{1}{2}\right)^{\frac{t}{t_{2}}} \text{ or } \frac{N}{N_o} = \left(\frac{1}{2}\right)^{\frac{t}{t_{2}}}$	
	If you want to find either N or N_o , you can plug the values for	or t and $t_{\frac{1}{2}}$ into the
	above equation.	

Big Ideas	Details Unit: Atomic and Nuclear Physics							
	Sample Problem:							
	Q: If you start with 228 g of ⁹⁰ Sr, how much would remain after 112.4 years?							
	A: $N_0 = 228 \text{ g}$							
	N = N							
	$t_{1/2}$ = 28.1 years (from the "Selected Radioisotopes" table in your reference							
	tables)							
	<i>t</i> = 1	112.4 years						
		$N = N_{\rm o}$,	(.)4			
		N = (22)	$8)\left(\frac{1}{2}\right)$ ²	^{.8.1} = (228)	$\left(\frac{1}{2}\right)^2 = (228)$	$3)\left(\frac{1}{16}\right) = 14$.25 g	
		if the decay happ mple), you can us	ens to occ					in this
		# years	0	28.1	56.2	84.3	112.4	
		# half-lives	0	1	2	3	4	
		amount left	228 g	114 g	57 g	28.5 g	14.25 g	

Big Ideas	Details	Unit: Atomic and Nuclear Physics		
	Finding	the Time that has Passed		
	Integer Number of Half-Lives			
If the amount you started with divided by the amount left is an exact you have an integer number of half-lives and you can just make a tab				
	Sample problem:			
	Q: If you started with 64 g of remaining? The half-life (¹³¹ I, how long would it take until there was only 4 g $t_{1/2}$) of ¹³¹ I is 8.07 days.		

A: $\frac{64}{4} = 16$ which is a power of 2, so we can simply make a table:

# half-lives	0	1	2	3	4
amount remaining	64 g	32 g	16 g	8 g	4 g

From the table, after 4 half-lives, we have 4 g remaining.

The half-life ($t_{1/2}$) of ¹³¹I is 8.07 days.

8.07 × 4 = 32.3 days

Sig Ideas	Details Unit: Atomic and Nuclear Physics					
	Non-Integer Number of Half-Lives					
	If you need to find the elapsed time and it is not an exact half-life, you need to use logarithms.					
	In mathematics, the only reason you ever need to use logarithms is when you need to solve for a variable that's in an exponent. For example, suppose we have the expression of the form $a^{b} = c$.					
	If b is a constant, we can solve for either a or c , as in the expressions:					
	$a^3 = 21$ ($\sqrt[3]{a^3} = \sqrt[3]{21} = 2.76$)					
	$6^2 = c$ ($6^2 = 36$)					
	However, we can't do this if a and c are constants and we need to solve for b , as in the expression:					
	3 ^{<i>b</i>} = 17					
	To solve for <i>b</i> , we need to get <i>b</i> out of the exponent. We do this by taking the logarithm of both sides:					
	<i>b</i> log(3) = log(17)					
	$b = \frac{\log(17)}{\log(3)} = \frac{1.23}{0.477} = 2.58$					
	It doesn't matter which base you use. Using In instead of log gives the same result:					
	<i>b</i> ln(3)=ln(17)					
	$b = \frac{\ln(17)}{\ln(3)} = \frac{2.83}{1.10} = 2.58$					
	We can apply this same logic to the half-life equation:					
	$\frac{N}{N_o} = \left(\frac{1}{2}\right)^{\frac{t}{T_{\frac{1}{2}}}}$					
	$\ln N - \ln N_o = \frac{t}{t_{\frac{1}{2}}} \ln\left(\frac{1}{2}\right)$					
	The College Board prefers to define a decay constant $\lambda = \frac{\ln 2}{t_{\frac{1}{2}}}$, which gives					
	$N = N_o e^{-\lambda t}$ and $\ln \frac{N}{N_o} = -\lambda t$					

Half-Life

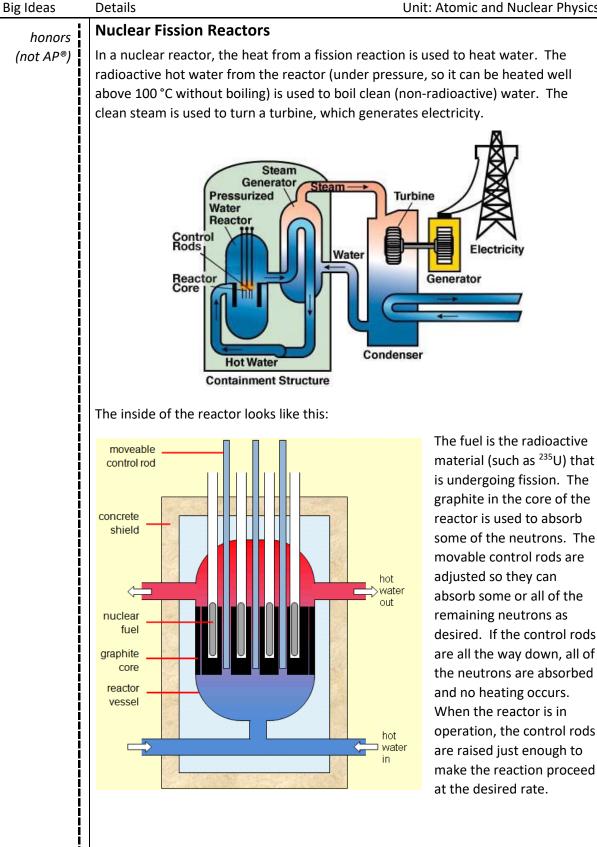
Page: 485

	Hall-Life	Page: 486
Big Ideas	Details	Unit: Atomic and Nuclear Physics
	Sample problem:	
	Q: If you started with 64 g of ¹³¹ I, how lon	g would it take until there was only 5.75 g
	remaining? The half-life (\mathcal{T}) of ¹³¹ I is 8.	07 days.
	A: We have 5.75 g remaining. However,	$\frac{64}{5.75} = 11.13$, which is not a power of two.
	This means we don't have an integer n logarithms:	umber of half-lives, so we need to use
	$\frac{N}{N_o} = \left($	
	ln N – ln N _o =	$=\frac{t}{t_{\frac{1}{2}}}\ln\left(\frac{1}{2}\right)$
	ln 5.75 – ln 64	$=\frac{t}{8.07}\ln\left(\frac{1}{2}\right)$
	1 7402 4 1590	t (0.6021)
	1.7492-4.1589=	=-1000000000000000000000000000000000000
	-2.4097 =	-0.0859 t
	28.1 da	ays = t
	Homework	x Problems
	For these problems, you will need to use has Selected Radioisotopes on page 513 of you	
	 (M) If a lab had 128 g of ³H waste 4 today? (Note: you may round off t 	49 years ago, how much of it would be left to a whole number of half-lives.)
	Anoviori 8 a	
	Answer: 8g	

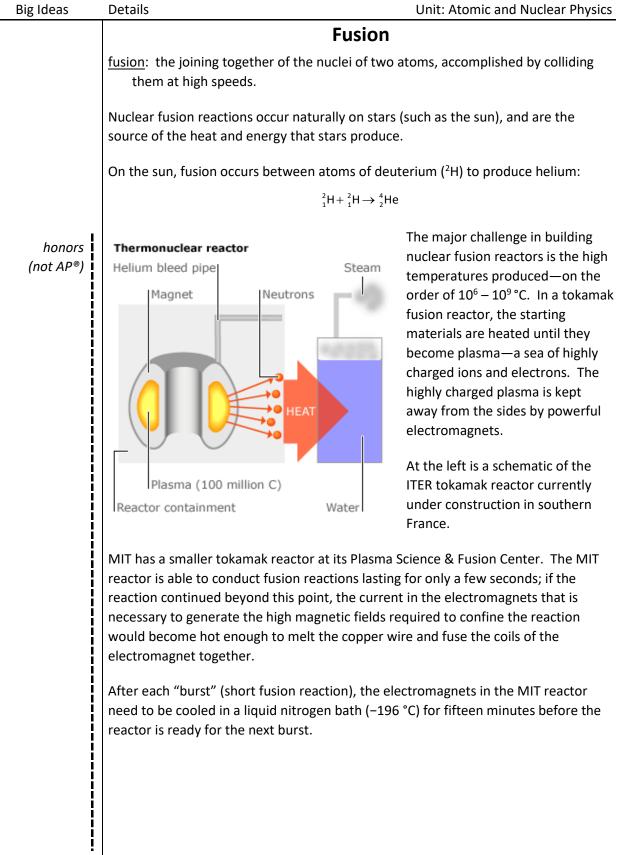
Big Ideas [Details	Unit: Atomic and Nuclear Physics
	2.	(S) Suppose you set aside a 20. g sample of ⁴² K at 5:00pm on a Friday for an experiment, but you are not able to perform the experiment until 9:00am on Monday (64 hours later). How much of the ⁴² K will be left?
		Answer: 0.56 g
	3.	(M) If a school wants to dispose of small amounts of radioactive waste, they can store the materials for ten half-lives and then dispose of the materials as regular trash.
		a. If we had a sample of ³² P, how long would we need to store it before disposing of it?
		Answer: 143 days
		b. If we had started with 64 g of ³² P, how much ³² P would be left after ten half-lives? Approximately what fraction of the original amount would be left?
		Answer: 0.063 g; approximately $\frac{1}{1000}$ of the original amount.
	4.	(M) If the carbon in a sample of human bone contained 30. % of the expected amount of 14 C, approximately how old is the sample?
		Answer: 9 950 years

	Nuclear Fission & Fusion Page: 488							
Big Ideas	Details Unit: Atomic and Nuclear Physics							
	Nuclear Fission & Fusion							
	Unit: Atomic and Nuclear Physics							
	NGSS Standards/MA Curriculum Frameworks (2016): HS-PS1-8							
	AP [®] Physics 2 Learning Objectives/Essential Knowledge (2024): 15.7.A, 15.7.A.4, 15.7.A.5, 15.7.A.6, 15.7.A.7, 15.7.A.8							
	Mastery Objective(s): (Students will be able to)							
	 Identify nuclear processes as "fission" or "fusion". 							
	 Describe the basic construction and operation of fission-based and fusion- based nuclear reactors. 							
	Success Criteria:							
	 Descriptions account for how the energy is produced and how the radiation is contained. 							
	Language Objectives:							
	 Explain how fission-based and fusion-based nuclear reactors work. 							
	Tier 2 Vocabulary: fusion, nuclear							
	Notes:							
	Fission							
	fission: splitting of the nucleus of an atom							
	Nuclear fission can occur naturally, or it can be caused by bombarding the nucleus of an atom with a high-speed neutron.							
	When atoms are split by bombardment with neutrons, they can divide in hundreds of ways. For example, when ²³⁵ U is hit by a neutron, it can split more than 200 ways. Three examples that have been observed are:							
	$^{1}_{0}n + ^{235}_{32}U \rightarrow ^{90}_{37}Rb + ^{144}_{55}Cs + 2^{1}_{0}n$							
	$\int_{0}^{1} n + \frac{235}{92} U \rightarrow \frac{87}{35} Br + \frac{146}{57} La + 3 \int_{0}^{1} n$							
	$\int_{0}^{1} n + \frac{235}{30} U \rightarrow \frac{72}{30} \text{Br} + \frac{160}{62} \text{Sm} + 4 \int_{0}^{1} n$							
	Note that each of these bombardments produces more neutrons. A reaction that produces more fuel (in this case, neutrons) than it consumes will accelerate. This self-propagation is called a <u>chain reaction</u> .							
	Note also that the neutron/proton ratio of ²³⁵ U is about 1.5. The stable neutron/proton ratio of each of the products would be approximately 1.2. This means that almost all of the products of fission reactions have too many neutrons to be stable, which means they will themselves undergo β - decay.							

Nuclear Fission & Fusion



Nuclear Fission & Fusion



Practical Uses for Nuclear Radiation

Practical Uses for Nuclear Radiation
Unit: Atomic and Nuclear Physics
NGSS Standards/MA Curriculum Frameworks (2016): HS-PS1-8
NGSS Standards/MA Curriculum Frameworks (2006): N/A
Mastery Objective(s): (Students will be able to)
Identify & describe practical (peaceful) uses for nuclear radiation.
Success Criteria:
 Descriptions give examples and explain how radiation is essential to the particular use.
Language Objectives:
• Explain how radiation makes certain scientific procedures possible. Tier 2 Vocabulary: radiation
Notes:
While most people think of the dangers and destructive power of nuclear radiation, there are a lot of other uses of radioactive materials:
Power Plants : nuclear reactors can generate electricity in a manner that does not produce CO ₂ and other greenhouse gases.
Cancer Therapy : nuclear radiation can be focused in order to kill cancer cells in patients with certain forms of cancer. Radioprotective drugs are now available that can help shield non-cancerous cells from the high-energy gamma rays.
Radioactive Tracers : chemicals made with radioactive isotopes can be easily detected in complex mixtures or even in humans. This enables doctors to give a patient a chemical with a small amount of radioactive material and track the progress of the material through the body and determine where it ends up. It also enables biologists to grow bacteria with radioactive isotopes and follow where those isotopes end up in subsequent experiments.
Irradiation of Food: food can be exposed to high-energy gamma rays in order to kill germs. These gamma rays kill all of the bacteria in the food, but do not make the food itself radioactive. (Gamma rays cannot build up inside a substance.) This provides a way to create food that will not spoil for months on a shelf in a store. There is a lot of irrational fear of irradiated food in the United States, but irradiation is commonly used in Europe. For example, irradiated milk will keep for months on a shelf at room temperature without spoiling.

Practical Uses for Nuclear Radiation

Big Ideas	Details Unit: Atomic and Nuclear Physics
honors (not AP®)	Carbon Dating : Because ¹⁴ C is a long-lived isotope (with a half-life of 5 700 years), the amount of ¹⁴ C in archeological samples can give an accurate estimate of their age. One famous use of carbon dating was its use to prove that the Shroud of Turin (the supposed burial shroud of Jesus Christ) was fake, because it was actually made between 1260 c.E. and 1390 c.E.
	Smoke Detectors : In a smoke detector, ²⁴¹ Am emits positively charged alpha particles, which are directed towards a metal plate. This steady flow of positive charges completes an electrical circuit. If there is a fire, smoke particles neutralize positive charges. This makes the flow of charges through the electrical circuit stop, which is used to trigger the alarm.

Appendix: AP® Physics 2 Equation Tables Advanced placement physics 2, EFFECTIVE 2017

CONSTANTS AND CONVERSION FACTORS							
Proton mass,	$m_p = 1.67 \times 10^{-27} \text{ kg}$	Electron charge magnitude,	$e = 1.60 \times 10^{-19} \text{ C}$				
Neutron mass,	$m_n = 1.67 \times 10^{-27} \text{ kg}$	1 electron volt,	$1 eV {=} 1.60 {\times} 10^{-19} J$				
Electron mass,	$m_e = 9.11 \times 10^{-31} \mathrm{kg}$	Speed of light,	$c = 3.00 \times 10^8 \text{ m/s}$				
Avogadro's number,	$N_o = 6.02 \times 10^{23} \text{ mol}^{-1}$	Universal gravitational constant,	$G = 6.67 \times 10^{-11} \text{ m}^3/\text{kg} \cdot \text{s}^2$				
Universal gas constant,	$R = 8.31 \frac{J}{\text{mol-K}}$	Acceleration due to gravity at Earth's surface,	$g = 9.8 \mathrm{m/s^2}$				
Boltzmann's constant,	$k_{B} = 1.38 \times 10^{-23} \frac{J}{K}$						
1 ur	nified atomic mass unit,	$1 u = 1.66 \times 10^{-27} kg = 931 \frac{MeV}{c^2}$					
	Planck's constant,	$h = 6.63 \times 10^{-34} \text{J} \cdot \text{s} = 4.14 \times 10^{-34} \text{J} \cdot \text{s}$	$0^{-15} \mathrm{eV} \cdot \mathrm{s}$				
		$hc = 1.99 \times 10^{-25} \text{J} \cdot \text{m} = 1.24 \times 10^{-25} \text{J} \cdot \text{m}$	$0^{-3} eV \cdot nm$				
	Vacuum permittivity,	$\mathcal{E}_o = 8.85 \times 10^{-12} \frac{\text{C}^2}{\text{N} \cdot \text{m}^2}$					
С	oulomb's law constant,	$k = \frac{1}{4\pi\varepsilon_o} = 9.0 \times 10^9 \frac{\text{N} \cdot \text{m}^2}{\text{C}^2}$					
	Vacuum permeability,	$\mu_o=4\pi imes 10^{-7}~{ m rac{T\cdot m}{A}}$					
	Magnetic constant,	$k' = \frac{\mu_o}{4\pi} = 1 \times 10^{-7} \frac{\text{T} \cdot \text{m}}{\text{A}}$					
	1 atmosphere pressure,	$1 \text{ atm} = 1.0 \times 10^5 \frac{N}{m^2} = 1.0 \times 10^5$	Pa				

	meter,	m	mole	mol	watt,	W	farad,	F
	kilogram,	k	hertz,	Hz	coulomb,	С	tesla,	Т
UNIT SYMBOLS	second,	s	newton,	N	volt,	V	degree Celsius,	°C
SINDULS	ampere,	А	pascal,	Pa	ohm,	Ω	electron volt,	eV
	kelvin,	Κ	joule,	J	henry,	Н		

P	PREFIXES					
Factor	Prefix	Symbo l		θ		
1012	tera	Т		sin		
10 ⁹	giga	G		cos		
106	mega	М		tan		
10 ³	kilo	k				
10 ⁻²	centi	с		The		
10 ⁻³	milli	m				
10-6	micro	μ				
10 ⁻⁹	nano	n				
10 ⁻¹²	pico	р				

	VALUES OF TRIGONOMETRIC FUNCTIONS FOR COMMON ANGLES						
θ	0°	30°	37°	45°	53°	60°	90°
$\sin \theta$	0	1/2	3/5	$\sqrt{2} / 2$	4/5	$\sqrt{3}/2$	1
$\cos \theta$	1	$\sqrt{3}/2$	4/5	$\sqrt{2} / 2$	3/5	1/2	0
$\tan \theta$	0	$\sqrt{3}/3$	3/4	1	4/3	$\sqrt{3}$	8

The following conventions are used in this exam.

- I. The frame of reference of any problem is assumed to be inertial unless otherwise stated.
- II. In all situations, positive work is defined as work done <u>on</u> a system.
- III. The direction of current is conventional current: the direction in which positive charge would drift.
- IV. Assume all batteries and meters are ideal unless otherwise stated.
- V. Assume edge effects for the electric field of a parallel plate capacitor unless otherwise stated.
- VI. For any isolated electrically charged object, the electric potential is defined as zero at infinite distance from the charged object.

MECH	ANICS	ELECTRICITY AND MAGNETISM		
$v_x = v_{xo} + a_x t$	<i>a</i> = acceleration <i>A</i> = amplitude	$\left \vec{F}_{E}\right = \frac{1}{4\pi\varepsilon_{o}} \frac{\left q_{1}q_{2}\right }{r^{2}}$	A = area B = magnetic field	
$x = x_o + v_{xo}t + \frac{1}{2}a_xt^2$	d = distance E = energy	$\vec{E} = rac{\vec{F}_E}{q}$	C = capacitance d = distance	
$v_x^2 = v_{xo}^2 + 2a_x(x - x_o)$	f = frequency F = force I = rotational inertia	$\left \vec{E}\right = \frac{1}{4\pi\varepsilon_o} \frac{ q }{r^2}$	$E = \text{electric field}$ $\mathcal{E} = \text{emf}$ $F = \text{force}$	
$\vec{a} = \frac{\sum \vec{F}}{m} = \frac{\vec{F}_{net}}{m}$	K = kinetic energy k = spring constant	$\Delta U_E = q \Delta V$	$I = \text{current}$ $\ell = \text{length}$	
$\left \vec{F}_{f}\right \leq \mu \left \vec{F}_{n}\right $	L = angular momentum $\ell =$ length m = mass	$V = \frac{1}{4\pi\varepsilon_o} \frac{q}{r}$	P = power Q = charge	
$a_c = \frac{v^2}{r}$	P = power p = momentum	$\left \vec{E}\right = \left \frac{\Delta V}{\Delta r}\right $	q = point charge R = resistance r = separation	
$\vec{p} = m\vec{v}$	r = radius or separation T = period	$\Delta V = \frac{Q}{C}$	t = time U = potential (stored)	
$\Delta \vec{p} = \vec{F} \Delta t$	t = time U = potential energy	$C = \kappa \varepsilon_o \frac{A}{d}$	energy $V =$ electric potential	
$K = \frac{1}{2}mv^2$	V = volume v = speed W = work done on a system	$E = \frac{Q}{\varepsilon_o A}$	v = speed $\kappa =$ dielectric constant	
$\Delta E = W = F_{\parallel}d = Fd\cos\theta$ $P = \frac{\Delta E}{\Delta t}$	x = position y = height	$U_{C} = \frac{1}{2}Q\Delta V = \frac{1}{2}C(\Delta V)^{2}$ $I = \frac{\Delta Q}{\Delta t}$	$\theta = angle$ $\Phi = flux$	
$\begin{aligned} \Delta t \\ \theta &= \theta_a + \omega_a t + \frac{1}{2}\alpha t^2 \end{aligned}$	α = angular acceleration μ = coefficient of friction	$R = \frac{\rho \ell}{4}$	$\vec{F}_{M} = q\vec{v} \times \vec{B}$	
$\omega = \omega_0 + \alpha t$	θ = angle ρ = density	$R = \frac{1}{A}$ $P = I\Delta V$	$\left \vec{F}_{M}\right = \left q\vec{v}\right \left \sin\theta\right \left \vec{B}\right $	
$x = A\cos(\omega t) = A\cos(2\pi f t)$		$I = \frac{\Delta V}{R}$	$\vec{F}_M = \vec{I} \ell \times \vec{B}$	
$x_{cm} = \frac{\sum m_i x_i}{\sum m_i}$	$\Delta U_g = mg\Delta y$	$R_s = \sum_i R_i$	$\left \vec{F}_{M} \right = \left \vec{I} \ell \right \sin \theta \left \vec{B} \right $	
$\vec{\alpha} = \frac{\sum \vec{\tau}}{I} = \frac{\vec{\tau}_{net}}{I}$	$T = \frac{2\pi}{\omega} = \frac{1}{f}$	$\frac{1}{R_p} = \sum_i \frac{1}{R_i}$ $C_p = \sum_i C_i$ $\frac{1}{C_s} = \sum_i \frac{1}{C_i}$	$\Phi_{\scriptscriptstyle B}=\vec{B}\bullet\vec{A}$	
$\tau = r_{\perp}F = rF\sin\theta$	$T_s = 2\pi \sqrt{\frac{m}{k}}$	$C_p = \sum_i C_i$	$\Phi_{B} = \left \vec{B} \right \cos \theta \left \vec{A} \right $	
$L = I\omega$	$T_p = 2\pi \sqrt{\frac{\ell}{g}}$	$\frac{1}{C_s} = \sum_i \frac{1}{C_i}$	$\mathcal{E} = -\frac{\Delta \Phi_{B}}{\Delta t}$	
$\Delta L = \tau \Delta t$		$B = \frac{\mu_o}{2\pi} \frac{I}{R}$		
$K = \frac{1}{2}I\omega^2$	$\left \vec{F}_{g}\right = G \frac{m_{1}m_{2}}{r^{2}}$	$B = \frac{1}{2\pi} \frac{1}{R}$	$\mathcal{E} = B\ell v$	
$\left \vec{F}_{s}\right = k \left \vec{x}\right $	$\vec{g} = \frac{\vec{F}_g}{m}$			
$U_s = \frac{1}{2}kx^2$	$U_g = G \frac{m_1 m_2}{r}$			

FLUID MECHANICS A	ND THERMAL PHYSICS	WAVES AND OPTICS		
$\rho = \frac{m}{V}$ $P = \frac{F}{A}$ $P = P_o + \rho g h$ $F_b = \rho V g$ $A_1 v_1 = A_2 v_2$ $P_1 + \rho g v_1 + \frac{1}{2} \rho v_1^2 = P_2 + \rho g v_2 + \frac{1}{2} \rho v_2$ $\frac{Q}{\Delta t} = \frac{kA \Delta T}{L}$	A = area $F = force$ $h = depth$ $k = thermal conductivity$ $K = kinetic energy$ $L = thickness$ $m = mass$ $n = number of moles$ $N = number of molecules$ $P = pressure$ $Q = energy transferred to a$ $system by heating$ $T = temperature$ $t = time$	$\lambda = \frac{v}{f}$ $n = \frac{c}{v}$ $n_{1} \sin \theta_{1} = n_{2} \sin \theta_{2}$ $\frac{1}{s_{i}} + \frac{1}{s_{o}} = \frac{1}{f}$ $ M = \left \frac{h_{i}}{h_{o}}\right = \left \frac{s_{i}}{s_{o}}\right $ $\Delta L = m\lambda$ $d \sin \theta = m\lambda$	d = separation f = frequency or focal length h = height L = distance M = magnification m = an integer n = index of refraction s = distance v = speed $\lambda = \text{wavelength}$ $\theta = \text{angle}$	
$\Delta t \qquad L$ $PV = nRT = Nk_BT$ $K = \frac{3}{2}k_BT$ $W = -P\Delta V$	U = internal energy V = volume v = speed W = work done on a system	GEOMETRY AN Rectangle A = bh	ND TRIGONOMETRY A = area C = circumference	
$\Delta U = Q + W$	y = height $\rho = \text{density}$	Triangle $A = bh$	V = volume S = surface area b = base h = height $\ell = \text{length}$	
MODER	N PHYSICS	Circle $A = \frac{1}{2}bh$	w = width r = radius	
$E = hf$ $K_{\max} = hf - \phi$	E = energy f = frequency K = kinetic energy m = mass	Rectangular solid $V = \ell w h$	Right triangle $c^2 = a^2 + b^2$ $\sin \theta = \frac{a}{c}$	
$\lambda = \frac{h}{p}$ $E = mc^{2}$	$m = mass$ $p = momentum$ $\lambda = wavelength$ $\phi = work function$	Cylinder $V = \pi r^2 \ell$ $S = 2\pi r \ell + 2\pi r^2$	$\cos \theta = \frac{b}{c}$ $\tan \theta = \frac{a}{b}$	
		Sphere $V = \frac{4}{3}\pi r^3$ $S = 4\pi r^2$	e^{c} a b a	

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actor		Prefix	Symbol
1 000 000 000 000 000 000 000 000 000 0	10 ³⁰	quetta	Q
1 000 000 000 000 000 000 000 000 000	10 ²⁷	ronna	R
1 000 000 000 000 000 000 000 000	1024	yotta	Y
1 000 000 000 000 000 000 000	1021	zeta	Z
1 000 000 000 000 000 000	1018	exa	Е
1 000 000 000 000 000			Р
1 000 000 000 000	1012	tera	Т
1 000 000 000	10 ⁹	giga	G
1 000 000	106	mega	М
1 000	10 ³	kilo	k
100	10 ²	hecto	h
10	10 ¹	deca	da
1	10 ⁰	—	—
0.1	10-1	deci	d
0.01	10-2	centi	С
0.001	10-3	milli	m
0.000 001	10-6	micro	μ
0.000 000 001	10-9	nano	n
0.000 000 000 001	10-12	pico	р
0.000 000 000 000 001	10-15	femto	f
0.000 000 000 000 000 001	10 ⁻¹⁸	atto	а
0.000 000 000 000 000 000 001	10-21	zepto	z
0.000 000 000 000 000 000 000 001	10 ⁻²⁴	yocto	У
0.000 000 000 000 000 000 000 000 001	10 ⁻²⁷	ronto	r
0.000 000 000 000 000 000 000 000 000 0	10-30	quecto	q

Table B. Physical Constants			
Description	Symbol	Precise Value	Common Approximation
acceleration due to gravity on Earth		9.7639 $\frac{m}{s^2}$ to 9.8337 $\frac{m}{s^2}$	9.8 $\frac{m}{s^2} \equiv 9.8 \frac{N}{kg}$
strength of gravity field on Earth	g	average value at sea level is 9.806 65 $\frac{m}{s^2}$	or $10 \frac{m}{s^2} \equiv 10 \frac{N}{kg}$
universal gravitational constant	G	$6.67384(80) \times 10^{-11} \frac{Nm^2}{kg^2}$	$6.67 \times 10^{-11} \frac{Nm^2}{kg^2}$
speed of light in a vacuum	с	299 792 458 m/s *	$3.00 \times 10^8 \frac{m}{s}$
elementary charge (proton or electron)	е	$\pm 1.602176634{\times}10^{-19}~{ m C}^*$	$\pm 1.60 \times 10^{-19}$ C
1 coulomb (C)		$6.241509074 \times 10^{18}$	6.24×10 ¹⁸ elementary
		elementary charges	charges
(electric) permittivity of a vacuum	ε _o	$8.85418782 \times 10^{-12} \frac{\text{A}^2 \text{-s}^4}{\text{kg m}^3}$	$8.85 \times 10^{-12} \frac{A^2 s^4}{kgm^3}$
(magnetic) permeability of a vacuum	μ_o	$4\pi \times 10^{-7} = 1.25663706 \times 10^{-6}\frac{Tm}{A}$	$1.26 \times 10^{-6} \frac{T.m}{A}$
electrostatic constant	k	$\frac{1}{4\pi\varepsilon_o} = 8.9875517873681764\times10^9\frac{\text{Nm}^2}{\text{C}^2} ^*$	$8.99 \times 10^9 \frac{Nm^2}{C^2}$
1 electron volt (eV)		$1.602176565(35) \times 10^{-19}$ J	$1.60 \times 10^{-19} \text{ J}$
Planck's constant	h	$6.62607015 \times 10^{-34}$ J·s [*]	6.63×10 ^{−34} J⋅s
		931.494 061(21) MeV/ c ²	931 MeV/c ²
1 universal (atomic) mass unit (u)		1.660 538 921(73)×10 ⁻²⁷ kg	$1.66 \times 10^{-27} \text{ kg}$
Avogadro's constant	N _A	$6.02214076 \times 10^{23}mol^{-1}$ *	$6.02 \times 10^{23} \text{ mol}^{-1}$
Boltzmann constant	k _B	$1.380649 \times 10^{-23} \frac{J}{\kappa} *$	$1.38 \times 10^{-23} \frac{J}{K}$
universal gas constant	R	8.314 4621(75) <u>J</u> molK	8.31 J mol-K
Rydberg constant	R _H	$\frac{m_e e^4}{8\varepsilon_o^2 h^3 c} = 10973731.6\frac{1}{m}$	$1.10 \times 10^7 \text{ m}^{-1}$
Stefan-Boltzmann constant	σ	$\frac{2\pi^5 R^4}{15h^3 c^2} = 5.670374419 \times 10^{-8}\frac{J}{m^2 \cdot s \cdot K^4}$	$5.67 \times 10^{-8} \frac{J}{m^2 \cdot s \cdot \kappa^4}$
standard atmospheric pressure at sea level		101 325 Pa ≡ 1.01325 bar*	100 000 Pa ≡ 1.0 bar
rest mass of an electron	m _e	$9.10938215(45)\times10^{-31}\mathrm{kg}$	$9.11 \times 10^{-31} \text{kg}$
mass of a proton	m _p	1.672 621 777(74)×10 ⁻²⁷ kg	$1.67{ imes}10^{-27}$ kg
mass of a neutron	mn	$1.674927351(74) \times 10^{-27}\mathrm{kg}$	$1.67 \times 10^{-27} \text{ kg}$

*denotes an exact value (by definition)

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Table C. Quantities, Variable	s and Units			
Quantity	Variable	MKS Unit Name	MKS Unit Symbol	S.I. Base Unit
position	x	meter*	m	m
distance/displacement, (length, height)	d, d , (L, h)	meter*	m	m
angle	θ	radian, degree	—, °	_
area	A	square meter	m ²	m ²
volume	V	cubic meter, liter	m ³	
time	<u>t</u> →	second*	S	S
velocity	V	meter/second	<u>m</u> s	<u>m</u> s
speed of light	<i>c</i>			
angular velocity	ŵ	radians/second	$\frac{1}{s^2}$, s^{-1}	$\frac{1}{s^2}$, s^{-1}
acceleration	ä	meter/second ²	<u>m</u>	<u>m</u>
acceleration due to gravity	ġ	meterysecond	s ²	s ²
angular acceleration	α	radians/second ²	$\frac{1}{s^2}$, s^{-2}	$rac{1}{s^2}$, s^{-2}
mass	т	kilogram*	kg	kg
force	Ē	newton	Ν	$\frac{\text{kg·m}}{\text{s}^2}$
gravitational field	ġ	newton/kilogram	N	m
gravitational neid	y	newtonykilogram	kg	s ²
pressure	Р	pascal	Ра	$\frac{\text{kg}}{\text{m}\cdot\text{s}^2}$
energy (generic)	E	_		
potential energy	U	joule	J	$\frac{\text{kg·m}^2}{\text{s}^2}$
kinetic energy	К, Е _к	jouie	J	s ²
heat	Q			
work	W	joule , newton-meter	J , N∙m	$\frac{\text{kg·m}^2}{\text{s}^2}$
torque	τ	newton-meter	N∙m	$\frac{\text{kg·m}^2}{\text{s}^2}$
power	Р	watt	W	$\frac{\text{kg·m}^2}{\text{s}^3}$
momentum	p		NLa	kg·m
impulse	Ĵ	newton-second	N∙s	S
moment of inertia	Ι	kilogram-meter ²	kg∙m²	kg∙m²
angular momentum	Ĺ	newton-meter-second	N∙m∙s	$\frac{\text{kg}\cdot\text{m}^2}{\text{s}}$
frequency	f	hertz	Hz	s ⁻¹
wavelength	λ	meter	m	m
period	Т	second	S	S
index of refraction	n	_	_	_
electric current	Ī	ampere*	A	A
electric charge	q	coulomb	С	A∙s
electric potential	V	1.	.,	kg·m²
potential difference (voltage) electromotive force (emf)	ΔV ε	volt	V	A·s ³
electrical resistance	ε R	ohm	Ω	$\frac{\text{kg·m}^2}{\text{A}^2 \cdot \text{s}^3}$
				$A^2 \cdot s^4$
capacitance	С	farad	F	m²·kg
electric field	Ē	newton/coulomb volt/meter	$\frac{N}{C}$, $\frac{V}{m}$	$\frac{\text{kg·m}}{\text{A·s}^3}$
magnetic field	B	tesla	Т	$\frac{\text{kg}}{\text{A} \cdot \text{s}^2}$
temperature	Т	kelvin*	К	К
amount of substance	п	mole*	mol	mol
luminous intensity	I_{v}	candela*	cd	cd

Variables representing vector quantities are typeset in **bold italics** with **arrows**. * = S.I. base unit

Kinematics (Distance, Velocity & Acceleration) Forces & Dynamics Circular/ Centripetal Motion & Force	$\frac{chanics \text{ Formulas and Equa}}{\vec{d} = \Delta \vec{x} = \vec{x} - \vec{x}_{o}}$ $\frac{\vec{d}}{t} = \frac{\vec{v}_{o} + \vec{v}}{2} (= \vec{v}_{ave.})$ $\vec{v} - \vec{v}_{o} = \vec{a}t$ $\vec{d} = \vec{v}_{o}t + \frac{1}{2}\vec{a}t^{2}$ $\vec{v}^{2} - \vec{v}_{o}^{2} = 2\vec{a}\vec{d}$ $\sum \vec{F} = \vec{F}_{net} = m\vec{a}$ $F_{f} \le \mu_{s}F_{N} \qquad F_{f} = \mu_{k}F_{N}$ $\vec{F}_{g} = m\vec{g} = \frac{Gm_{1}m_{2}}{r^{2}}$ $a_{c} = \frac{v^{2}}{r}$	var. = name of quantity (unit) Δ = change in something(E.g., Δx means change in x) Σ = sum d = distance (m) \vec{d} = displacement (m) \vec{x} = position (m) t = time (s) \vec{v} = velocity $\left(\frac{m}{s}\right)$ $\vec{v}_{ave.}$ = average velocity $\left(\frac{m}{s}\right)$	$\mu = \text{co\"efficient of friction"} (dimensionless) \theta = angle (°, radians) k = spring constant \left(\frac{N}{m}\right)\vec{x} = displacement of spring (m)L = length of pendulum (m)E = energy (J)K = E_k = kinetic energy (J)U = potential energy (J)$
(Distance, Velocity & Acceleration) Forces & Dynamics Circular/ Centripetal Motion &	$\vec{v} - \vec{v}_o = \vec{a}t$ $\vec{d} = \vec{v}_o t + \frac{1}{2}\vec{a}t^2$ $\vec{v}^2 - \vec{v}_o^2 = 2\vec{a}\vec{d}$ $\sum \vec{F} = \vec{F}_{net} = m\vec{a}$ $F_f \le \mu_s F_N \qquad F_f = \mu_k F_N$ $\vec{F}_g = m\vec{g} = \frac{Gm_1m_2}{r^2}$	(E.g., Δx means change in x) $\Sigma = \text{sum}$ d = distance (m) $\vec{d} = \text{displacement (m)}$ $\vec{x} = \text{position (m)}$ t = time (s) $\vec{v} = \text{velocity } \left(\frac{\text{m}}{\text{s}}\right)$ $\vec{v}_{ave.} = \text{average velocity } \left(\frac{\text{m}}{\text{s}}\right)$	(dimensionless) $\theta = \text{angle } (^\circ, \text{ radians})$ $k = \text{spring constant } \left(\frac{N}{m}\right)$ $\vec{x} = \text{displacement of spring } (m)$ L = length of pendulum (m) E = energy (J) $K = E_k = \text{kinetic energy } (J)$ U = potential energy (J)
Dynamics Circular/ Centripetal Motion &	$\vec{F}_{f} \le \mu_{s} F_{N} \qquad F_{f} = \mu_{k} F_{N}$ $\vec{F}_{g} = m\vec{g} = \frac{Gm_{1}m_{2}}{r^{2}}$	t = time (s) $\vec{v} = \text{velocity } \left(\frac{m}{s}\right)$ $\vec{v}_{ave.} = \text{average velocity } \left(\frac{m}{s}\right)$	E = energy (J) $K = E_k = \text{kinetic energy (J)}$ U = potential energy (J)
Centripetal Motion &	$a = \frac{v^2}{v}$		<i>TME</i> = total mechanical energy (J)
	$a_c - \frac{r}{r}$ $F_c = ma_c$	$\vec{a} = \text{acceleration} \left(\frac{m}{s^2}\right)$ $f = \text{frequency} \left(\text{Hz} = \frac{1}{s}\right)$ $\vec{F} = \text{force} (N)$	h = height (m) Q = heat (J) P = power (W) W = work (J, N·m)
Simple Harmonic Motion	$T = \frac{1}{f}$ $T_{s} = 2\pi \sqrt{\frac{m}{k}} T_{p} = 2\pi \sqrt{\frac{L}{g}}$ $\vec{F}_{s} = -k\vec{x}$ $U_{s} = \frac{1}{2}kx^{2}$	\vec{F}_{net} = net force (N) F_f = force due to friction (N) \vec{F}_g = force due to gravity (N) \vec{F}_{N} = normal force (N) m = mass (kg) \vec{g} = strength of gravity field	$T = (\text{time}) \text{ period (Hz)}$ $\vec{p} = \text{momentum (N \cdot s)}$ $\vec{J} = \text{impulse (N \cdot s)}$ $\pi = \text{pi (mathematical constant)}$ $= 3.141592653589793$
Energy, Work & Power	$U_{g} = mgh = \frac{Gm_{1}m_{2}}{r}$ $K = \frac{1}{2}mv^{2} = \frac{p^{2}}{2m}$ $W = \Delta E = \Delta(U_{g} + K)$ $W = F_{\parallel}d = \vec{F}_{net} \cdot \vec{d} = Fd \cos\theta$ $TME = U_{g} + K$ $TME_{i} + W = TME_{f}$ $P = \frac{W}{t} = \vec{F} \cdot \vec{v} = Fv\cos\theta$	= aceleration due to gravity = $10 \frac{N}{kg} = 10 \frac{m}{s^2}$ on Earth G = gravitational constant = $6.67 \times 10^{-11} \frac{N \cdot m^2}{kg^2}$ r = radius (m)	
Momentum	$\vec{\boldsymbol{p}} = \sum m \vec{\boldsymbol{v}}$ $\sum m_i \vec{\boldsymbol{v}}_i + \vec{\boldsymbol{J}} = \sum m_f \vec{\boldsymbol{v}}_f$ $\vec{\boldsymbol{J}} = \Delta \vec{\boldsymbol{p}} = \vec{\boldsymbol{F}}_{net} t$	*characteristic property of a substa	nce (to be looked up)

Substance	Static (µ _s)	Kinetic (μ_k)	Substance	Static (µ₅)	Kinetic (μ_k)
rubber on concrete (dry)	0.90	0.68	wood on wood (dry)	0.42	0.30
rubber on concrete (wet)		0.58	wood on wood (wet)	0.2	
rubber on asphalt (dry)	0.85	0.67	wood on metal	0.3	
rubber on asphalt (wet)		0.53	wood on brick	0.6	
rubber on ice		0.15	wood on concrete	0.62	
steel on ice	0.03	0.01	Teflon on Teflon	0.04	0.04
waxed ski on snow	0.14	0.05	Teflon on steel	0.04	0.04
aluminum on aluminum	1.2	1.4	graphite on steel	0.1	
cast iron on cast iron	1.1	0.15	leather on wood	0.3–0.4	
steel on steel	0.74	0.57	leather on metal (dry)	0.6	
copper on steel	0.53	0.36	leather on metal (wet)	0.4	
diamond on diamond	0.1		glass on glass	0.9–1.0	0.4
diamond on metal	0.1–0.15		metal on glass	0.5–0.7	

Table F. Angular/Rotational Mechanics Formulas and Equations						
	$\Delta \vec{\theta} = \vec{\theta} - \vec{\theta}_o$	var. = name of quantity (unit)				
Angular Kinematics (Distance, Velocity & Acceleration)	$\frac{\Delta \vec{\theta}}{t} = \frac{\vec{\omega}_o + \vec{\omega}}{2} (= \vec{\omega}_{ave.})$ $\vec{\omega} - \vec{\omega}_o = \vec{\alpha}t$ $\Delta \vec{\theta} = \vec{\omega}_o t + \frac{1}{2}\vec{\alpha}t^2$ $\vec{\omega}^2 - \vec{\omega}_o^2 = 2\vec{\alpha}(\Delta \vec{\theta})$	$\Delta = \text{change in something } (E.g., \Delta x = \text{change in } x)$ $\Sigma = \text{sum}$ s = arc length (m) t = time (s) $\sigma_c = \text{centripetal acceleration } \left(\frac{\text{m}}{\text{s}^2}\right)$				
Circular/ Centripetal Motion	$s = r\Delta\theta$ $v_{\tau} = r\omega$ $a_{\tau} = r\alpha$ $a_{c} = \frac{v^{2}}{r} = \omega^{2}r$	$F_c = \text{centripetal force (N)}$ m = mass (kg) r = radius (m)				
Rotational Dynamics	$x_{cm} = \frac{\sum m_i x_i}{\sum m_i}$ $I = _mr^2 = \int_0^m r^2 dm$ $F_c = ma_c = mr\omega^2$ $\vec{\tau} = \vec{r} \times \vec{F} \qquad \tau = rF \sin\theta = r_\perp F$ $\sum \vec{\tau} = \vec{\tau}_{net} = I\vec{\alpha}$	\vec{r} = radius (vector) θ = angle (°, radians) $\vec{\omega}$ = angular velocity $\left(\frac{rad}{s}\right)$ $\vec{\alpha}$ = angular velocity $\left(\frac{rad}{s^2}\right)$ $\vec{\tau}$ = torque (N·m) x = position (m) f = forguency (Uz)				
Simple Harmonic Motion	$T = \frac{1}{f} = \frac{2\pi}{\omega}$ $x = A\cos(2\pi ft) + \phi$	f = frequency (Hz) A = amplitude (m) $\phi =$ phase offset (°, rad) E = energy (J)				
Angular Momentum	$\vec{\boldsymbol{L}} = \vec{\boldsymbol{r}} \times \vec{\boldsymbol{p}} = I \vec{\boldsymbol{\omega}} \boldsymbol{L} = rp \sin\theta = I\omega$ $\Delta \vec{\boldsymbol{L}} = \vec{\boldsymbol{\tau}} \Delta t$	$K = E_k$ = kinetic energy (J) K_t = translational kinetic energy (J) K_r = rotational kinetic energy (J)				
Angular/ Rotational Energy, Work & Power	$K_r = \frac{1}{2}I\omega^2$ $K = K_t + K_r = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$ $W_r = \tau\Delta\theta$ $P = \frac{W}{t} = \tau\omega$	$P = \text{power (W)}$ $W = \text{work (J, N \cdot m)}$ $\vec{p} = \text{momentum (N \cdot s)}$ $\vec{L} = \text{angular momentum (N \cdot m \cdot s)}$				

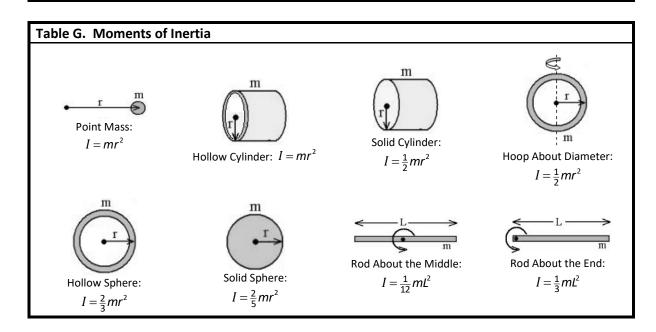
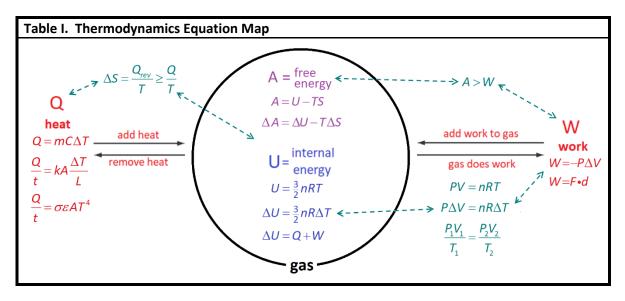


Table H.	Heat and Thermal Physics	Formulas and Equations	
Temperat	$T_{o_{\rm F}} = 1.8(T_{o_{\rm C}}) + 32$	var. = name of quantity (unit)	
ure	$T_{\rm K} = T_{\rm oc} + 273.15$	$\Delta =$ change in something	P = pressure (Pa) n = number of moles (mol)
Heat	$Q = mC \Delta T$ $Q_{melt} = m \Delta H_{fus}$ $Q_{boil} = m \Delta H_{vap}$ $C_p - C_v = R$ $\Delta L = \alpha L_i \Delta T$ $\Delta V = \beta V_i \Delta T$ $P = \frac{Q}{t} = (\pm) kA \frac{\Delta T}{L}$ $P = \frac{Q}{t} = \varepsilon \sigma A T^4$ (in this section, P = power)	(E.g., $\Delta x = \text{change in } x$) $T = T_{\text{K}} = \text{Kelvin temperature (K)}$ $T_{\circ_{\text{F}}} = \text{Fahrenheit temperature (°F)}$ $T_{\circ_{\text{C}}} = \text{Celsius temperature (°C)}$ Q = heat (J, kJ) m = mass (kg) $C = \text{specific heat capacity*} \left(\frac{\text{kJ}}{\text{kg.°C}}, \frac{J}{\text{g.°C}}\right)$ t = time (s) L = length (m) k = coefficient of thermal $\text{conductivity*} \left(\frac{J}{\text{m.°C}}, \frac{\text{W}}{\text{m.°C}}\right)$	$N = \text{number of molecules}$ $R = \text{gas constant} = 8.31 \frac{\text{J}}{\text{mol} \cdot \text{K}}$ $k_{\text{g}} = \text{Boltzmann constant}$ $= 1.38 \times 10^{-23} \frac{\text{J}}{\text{K}}$ $U = \text{internal energy (J)}$ $W = \text{work (J, N \cdot m)}$ $v_{\text{rms}} = \text{root mean square speed (}\frac{\text{m}}{\text{s}}\text{)}$ $\mu = \text{molecular mass}^* (\text{kg})$ $M = \text{molar mass}^* (\frac{\text{kg}}{\text{mol}})$ $K = \text{kinetic energy (J)}$ $Q_{\text{rev}} = \text{"reversible" heat (J)}$
Thermo- dynamics	$\frac{P_{1}V_{1}}{T_{1}} = \frac{P_{2}V_{2}}{T_{2}}$ $PV = nRT = Nk_{B}T$ $P\Delta V = nR\Delta T = Nk_{B}\Delta T$ $\Delta U = Q + W$ $U = \frac{3}{2}nRT \Delta U = \frac{3}{2}nR\Delta T$ $W = -P\Delta V = -\int_{V_{1}}^{V_{2}}PdV$ $K_{(molecular)} = \frac{3}{2}RT$ $U = \frac{3}{2}nR\Delta T = \frac{3}{2}Nk_{B}T$ $\Delta U = \frac{3}{2}nR\Delta T = \frac{3}{2}Nk_{B}\Delta T$ $v_{rms} = \sqrt{\frac{3RT}{M}} = \sqrt{\frac{3k_{B}T}{\mu}}$ $\Delta S = \frac{Q_{rev}}{T} \ge \frac{Q}{T}$ $A = U - TS$ $\Delta A = \Delta U - T\Delta S$ (in this section, P = pressure)	$\varepsilon = \text{emissivity}^* (dimensionless)$ $H_{fus} = \text{latent heat of fusion} \left(\frac{\text{kj}}{\text{kg}}, \frac{\text{j}}{\text{g}}\right)$ $H_{vop} = \text{heat of vaporization} \left(\frac{\text{kj}}{\text{kg}}, \frac{\text{j}}{\text{g}}\right)$ $\sigma = \text{Stefan-Boltzmann constant}$ $= 5.67 \times 10^{-8} \frac{\text{j}}{\text{m}^2 \cdot \text{s} \cdot \text{K}^4}$ $V = \text{volume (m^3)}$ $\alpha = \text{linear coëfficient of thermal}$ $expansion^* (^{\circ}\text{C}^{-1})$ $\beta = \text{volumetric coëfficient of}$ $\text{thermal expansion}^* (^{\circ}\text{C}^{-1})$ $P = \text{power (W)}$ *characteristic property of a substance ($S = \text{entropy}\left(\frac{1}{K}\right)$ A = Helmholtz free energy (J) to be looked up)



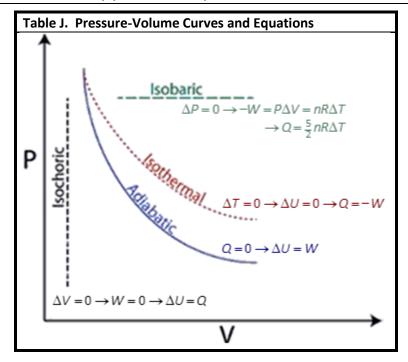


Table K. Thermal Properties of Selected Materials									
Substance	Melting Point (°C)	Boiling Point (°C)	Heat of Fusion ΔH_{fus} $\left(\frac{kJ}{kg}, \frac{J}{g}\right)$	Heat of Vaporiz- ation ΔH_{vap} $\left(\frac{kj}{kg}, \frac{j}{g}\right)$	Specific Heat Capacity C $\left(\frac{kJ}{kg.^{\circ}C}\right)$ at 25°C	Thermal Conduct- ivity	Emissivi ty	Coefficients of Expansion at 20°C	
						$k \left(\frac{J}{m \cdot s^{\circ} C}\right)$ at 25°C	E black body = 1	Linear α(°C ⁻¹)	Volumetric β(°C ⁻¹)
air (gas)	_	_	_	_	1.012	0.024	_	_	_
aluminum (solid)	659	2467	395	10460	0.897	250	0.09*	2.3×10 ⁻⁵	6.9×10 ⁻⁵
ammonia (gas)	-75	-33.3	339	1369	4.7	0.024	_	_	_
argon (gas)	-189	-186	29.5	161	0.520	0.016	_	_	_
carbon dioxide (gas)	-78		57	74	0.839	0.0146	_	_	_
copper (solid)	1086	1187	134	5063	0.385	401	0.03*	1.7×10^{-5}	5.1×10 ⁻⁵
brass (solid)	_	_	_	_	0.380	120	0.03*	1.9×10 ⁻⁵	5.6×10 ⁻⁵
diamond (solid)	3550	4827	10 000	30 000	0.509	2200	_	1×10 ⁻⁶	3×10 ⁻⁶
ethanol (liquid)	-117	78	104	858	2.44	0.171	_	2.5×10^{-4}	7.5×10^{-4}
glass (solid)	_	—	_	_	0.84	0.96-1.05	0.92	8.5×10 ⁻⁶	2.55×10 ⁻⁵
gold (solid)	1063	2660	64.4	1577	0.129	310	0.025*	1.4×10^{-5}	4.2×10^{-5}
granite (solid)	1240	_		—	0.790	1.7-4.0	0.96	_	_
helium (gas)	-	-269	-	21	5.193	0.142	-	-	_
hydrogen (gas)	-259	-253	58.6	452	14.30	0.168	—	—	—
iron (solid)	1535	2750	289	6360	0.450	80	0.31	1.18×10^{-5}	3.33×10 ⁻⁵
lead (solid)	327	1750	24.7	870	0.160	35	0.06	2.9×10 ⁻⁵	8.7×10 ⁻⁵
mercury (liquid)	-39	357	11.3	293	0.140	8	—	6.1×10^{-5}	1.82×10^{-4}
paraffin wax (solid)	46–68	~300	~210	—	2.5	0.25	—	—	—
silver (solid)	962	2212	111	2360	0.233	429	0.025*	1.8×10^{-5}	5.4×10^{-5}
zinc (solid)	420	906	112	1760	0.387	120	0.05*	$\sim 3 \times 10^{-5}$	8.9×10 ⁻⁵
steam (gas) @ 100°C			_	2260	2.080	0.016	—	—	_
water (liq.) @ 25°C	0	100	334	2200	4.181	0.58	0.95	6.9×10 ⁻⁵	2.07×10^{-4}
ice (solid) @ -10°C			554	—	2.11	2.18	0.97	—	—
*polished surface									

Table L. Electricity Formulas & Equations				
	•	var. = name of quantity (unit)		
	$\boldsymbol{F}_{e} = \frac{kq_{1}q_{2}}{r^{2}} = \frac{1}{4\pi\varepsilon_{o}}\frac{q_{1}q_{2}}{r^{2}}$	$\Delta =$ change in something. (<i>E.g.</i> , $\Delta x =$ change in x) $\vec{F}_{\rho} =$ force due to electric field (N)		
	$\vec{F}_{a} Q = kq 1 q \Delta V$	ε_e = electric permittivity of a vacuum		
Electrostatic	$\vec{E} = \frac{\vec{F}_e}{q} = \frac{Q}{\varepsilon_o A} \vec{E} = \frac{kq}{r^2} = \frac{1}{4\pi\varepsilon_o} \cdot \frac{q}{r^2} = \frac{\Delta V}{\Delta r}$			
Charges &	$W = q\vec{E} \bullet \vec{d} = qEd_{\parallel} = qEd\cos\theta$	$= 8.85 \times 10^{-12} \frac{\text{A}^2 \cdot \text{s}^4}{\text{kg} \cdot \text{m}^3}$		
Electric Fields	"	k = electrostatic constant		
	$\Delta V = \frac{W}{q} = \vec{E} \bullet \vec{d} = Ed_{\parallel} = \frac{1}{4\pi\varepsilon_o} \frac{q}{r}$	$=\frac{1}{4\pi\varepsilon_o}=9.0\times10^9\frac{\mathrm{N}\cdot\mathrm{m}^2}{\mathrm{c}^2}$		
	$\Delta U_E = q \Delta V \qquad U_E = \frac{kq_1q_2}{r}$	q = point charge (C) Q = charge (C)		
		\vec{E} = electric field $\left(\frac{N}{C}, \frac{V}{m}\right)$		
	$\Delta V = IR \qquad I = \frac{\Delta Q}{\Delta t} = \frac{\Delta V}{R}$	V = electric potential (V)		
		$\Delta V = $ voltage = electric potential difference (V)		
	$\mathcal{E} = IR$	$\mathcal{E} = emf = electromotive force (V)$		
	$P = I\Delta V = I^2 R = \frac{(\Delta V)^2}{R}$	W = work (J, N·m)		
	R $W = Pt = I\Delta Vt$	$\kappa = \varepsilon_r$ = relative permittivity* (<i>dimensionless</i>)		
Circuits and		d = distance (m)		
Electrical	$R = \frac{\rho L}{\Delta}$	r = radius (m)		
Components	· · ·	\vec{I} = current (A)		
	$C = \kappa \varepsilon_o \frac{A}{d}$	t = time (s)		
	$Q = C \Delta V$	$R = resistance (\Omega)$ P = power (W)		
	$U_{capacitor} = \frac{1}{2}Q\Delta V = \frac{1}{2}C(\Delta V)^2$	$\rho = \text{resistivity} (\Omega \cdot \text{m})$		
	$P_{\text{total}} = P_1 + P_2 + P_3 + \ldots = \sum_i P_i$	L = length (m)		
	$U_{total} = U_1 + U_2 + U_3 + \dots = \sum U_i$	$A = \text{cross-sectional area} (\text{m}^2)$		
		C = capacitance (F)		
	$I_{total} = I_1 = I_2 = I_3 = \dots$	U = potential energy (J)		
Series Circuits	$\Delta V_{total} = \Delta V_1 + \Delta V_2 + \Delta V_3 + \ldots = \sum \Delta V_i$	$\pi=$ pi (mathematical constant)		
(or Series	$R_{equiv.} = R_1 + R_2 + R_3 + \ldots = \sum R_i$	= 3.14159 26535 89793		
Sections of Circuits)	$\boldsymbol{Q}_{total} = \boldsymbol{Q}_1 = \boldsymbol{Q}_2 = \boldsymbol{Q}_3 = \dots$	<i>e</i> = Euler's number (mathematical constant)		
	$\frac{1}{C_{total}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots = \sum \frac{1}{C_i}$	= 2.78182 81812 84590		
	$I_{totol} = I_1 + I_2 + I_3 + \ldots = \sum I_i$	*characteristic property of a substance (to be		
	$\Delta V_{total} = \Delta V_1 = \Delta V_2 = \Delta V_3 = \dots$	looked up)		
Parallel Circuits				
(or Parallel Sections	$\frac{1}{R_{equiv.}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \ldots = \sum \frac{1}{R_i}$			
of Circuits)	$Q_{total} = Q_1 + Q_2 + Q_3 + \ldots = \sum Q_i$			
	$C_{total} = C_1 + C_2 + C_3 + \dots = \sum C_i$			
	charging: $\frac{I}{I_o} = e^{-t/RC}$			
Resistor- Capacitor (RC) Circuits	charging: $\frac{Q}{Q_{max}} = 1 - e^{-t/RC}$			
	discharging: $\frac{I}{I_o} = \frac{V}{V_o} = \frac{Q}{Q_{max}} = e^{-t/RC}$			

Table M. El	Table M. Electricity & Magnetism Formulas & Equations					
		<i>var.</i> = name of quantity (unit)				
Magnetism and Electro- magnetism	$\vec{F}_{M} = q (\vec{v} \times \vec{B}) \qquad F_{M} = qvB\sin\theta$ $\vec{F}_{M} = \ell(\vec{I} \times \vec{B}) \qquad F_{M} = \ell IB\sin\theta$ $\Delta V = \ell(\vec{v} \times \vec{B}) \qquad \Delta V = \ell vB\sin\theta$ $B = \frac{\mu_{o}}{2\pi} \frac{I}{r}$ $\Phi_{B} = \vec{B} \cdot \vec{A} = BA\cos\theta$ $\mathcal{E} = \frac{\Delta \Phi_{B}}{\Delta t} = BLv$	$\Delta = \text{change in something. } (E.g., \Delta x = \text{change in } x)$ $\vec{F}_e = \text{force due to electric field (N)}$ $\vec{v} = \text{velocity (of moving charge or wire) } \left(\frac{\text{m}}{\text{s}}\right)$ q = point charge (C) $\Delta V = \text{voltage} = \text{electric potential difference (V)}$ $\mathcal{E} = \text{emf} = \text{electromotive force (V)}$ r = radius (m) = distance from wire $\vec{I} = \text{current (A)}$ L = length (m)				
Electro- magnetic Induction	$\frac{\#turns_{in}}{\#turns_{out}} = \frac{V_{in}}{V_{out}} = \frac{I_{out}}{I_{in}}$ $P_{in} = P_{out}$	t = time (s) A = cross-sectional area (m2) $\vec{B} = \text{magnetic field (T)}$ $\mu_{o} = \text{magnetic permeability of a vacuum} = 4\pi \times 10^{-7} \frac{\text{T-m}}{\text{A}}$ $\Phi_{B} = \text{magnetic flux (T \cdot m^{2})}$				

Table N. Resistor Color						
Code						
Color	Digit	Multiplier				
black	0	× 10 ⁰				
brown	1	× 10 ¹				
red	2	× 10 ²				
orange	3	× 10 ³				
yellow	4	× 10 ⁴				
green	5	× 10 ⁵				
blue	6	× 10 ⁶				
violet	7	× 10 ⁷				
gray	8	× 10 ⁸				
white	9	× 10 ⁹				
gold	± 5%					
silver	ilver ± 10%					

Table O. Symbols Used in Electrical Circuit Diagrams					
Component	Symbol	Component	Symbol		
wire		battery	÷		
switch	- ~ -	ground			
fuse		resistor			
voltmeter	-V-	variable resistor (rheostat, potentiometer, dimmer)			
ammeter	-A-	lamp (light bulb)			
ohmmeter	-R- -Ω-	capacitor	$\dashv \vdash$		
		diode			

Table P. R	Table P. Resistivities at 20°C					
(Conductors	Semic	onductors	In	sulators	
Substance	Resistivity $\left(\boldsymbol{\Omega} \cdot \boldsymbol{m} \right)$	Substance	Resistivity $\left(\mathbf{\Omega}\cdot\mathbf{m} ight)$	Substance	Resistivity $\left(\boldsymbol{\Omega} \cdot \boldsymbol{m} \right)$	
silver	1.59×10^{-8}	germanium	0.001 to 0.5	deionized water	1.8×10 ⁵	
copper	1.72×10 ⁻⁸	silicon	0.1 to 60	glass	$1{\times}10^{9}$ to $1{\times}10^{13}$	
gold	2.44×10 ⁻⁸	sea water	0.2	rubber, hard	$1{\times}10^{\scriptscriptstyle 13}$ to $1{\times}10^{\scriptscriptstyle 13}$	
aluminum	2.82×10^{-8}	drinking water	20 to 2000	paraffin (wax)	$1{\times}10^{13}$ to $1{\times}10^{17}$	
tungsten	5.60×10^{-8}			air	1.3×10^{16} to 3.3×10^{16}	
iron	9.71×10 ⁻⁸			quartz, fused	7.5×10^{17}	
nichrome	1.50×10^{-6}					
graphite	$3{\times}10^{^{-5}}$ to $6{\times}10^{^{-4}}$					

Table Q. Wa	Table Q. Waves & Optics Formulas & Equations				
	· · · · ·	var. = name of quantity (unit)			
	$v = \lambda f$	$\Delta =$ change in something (<i>E.g.</i> , $\Delta x =$ change in <i>x</i>)			
	$f = \frac{1}{\tau}$	$v = velocity of wave \left(\frac{m}{s}\right)$			
	,	$\vec{\mathbf{v}} = $ velocity of source or detector $\left(\frac{m}{s}\right)$			
Waves	$V_{\text{wave on a string}} = \sqrt{\frac{F_T}{\mu}}$	f = frequency (Hz)			
		$\lambda =$ wavelength (m)			
	$f_{\text{doppler shifted}} = f\left(rac{ec{m{v}}_{\text{wave}} + ec{m{v}}_{\text{detector}}}{ec{m{v}}_{\text{wave}} + ec{m{v}}_{\text{source}}} ight)$	A = amplitude (m)			
	$\vec{v}_{\text{doppler shifted}} = \vec{v}_{\text{wave}} + \vec{v}_{\text{source}}$	x = position (m)			
	$x = A\cos(2\pi ft + \phi)$	T = period (of time) (s)			
		F_{τ} = tension (force) on string (N)			
	$\theta_i = \theta_r$	$\mu = \text{elastic modulus of string } \left(\frac{\text{kg}}{\text{m}}\right)$			
	C C	$\theta = $ angle (°, rad)			
	$n = \frac{c}{v}$	$\phi =$ phase offset (°, rad)			
	$n_1 \sin \theta_1 = n_2 \sin \theta_2$	θ_i = angle of incidence (°, rad)			
Reflection, Refraction &	$\theta_c = \sin^{-1} \left(\frac{n_2}{n_1} \right)$ $\frac{n_2}{n_1} = \frac{v_1}{v_2} = \frac{\lambda_1}{\lambda_2}$	θ_r = angle of reflection (°, rad)			
Diffraction &		$\theta_c = \text{critical angle}$ (°, rad)			
		<pre>n = index of refraction* (dimensionless)</pre>			
		$c =$ speed of light in a vacuum = $3.00 \times 10^8 \frac{\text{m}}{\text{s}}$			
	$\Lambda_1 \nu_2 \Lambda_2$ $\Delta L = m\lambda = d\sin\theta$	$f = s_f = d_f$ = distance to focus of mirror/lens (m)			
	$\Delta L = m\lambda = d\sin\theta$	$r_c =$ radius of curvature of spherical mirror (m)			
		$s_i = d_i$ = distance from mirror/lens to image (m)			
		$s_o = d_o$ = distance from mirror/lens to object (m)			
	$f - r_c$	$h_i = \text{height of image} (m)$			
	$f = \frac{r_c}{2}$	$h_o = \text{height of object (m)}$			
Mirrors &	$\frac{1}{2}$ $+$ $\frac{1}{2}$ $ \frac{1}{2}$	M = magnification (<i>dimensionless</i>)			
Lenses	$\frac{1}{s_i} + \frac{1}{s_o} = \frac{1}{f}$	d = separation (m)			
	$h_i - s_i$	L = distance from the opening (m)			
	$M = \frac{h_i}{h_o} = -\frac{s_i}{s_o}$	m = an integer			
		*characteristic property of a substance (to be looked up)			

Table R. Absolute Indices of Refraction					
Measured using $f = 5.89 \times 10^{14}$ Hz (yellow light) at 20 °C unless otherwise specified					
Substance	Index of Refraction	Substance	Index of Refraction		
air (0 °C and 1 atm)	1.000293	silica (quartz), fused	1.459		
ice (0 °C)	1.309	Plexiglas	1.488		
water	1.3330	Lucite	1.495		
ethyl alcohol	1.36	glass, borosilicate (Pyrex)	1.474		
human eye, cornea	1.38	glass, crown	1.50-1.54		
human eye, lens	1.41	glass, flint	1.569–1.805		
safflower oil	1.466	sodium chloride, solid	1.516		
corn oil	1.47	PET (#1 plastic)	1.575		
glycerol	1.473	zircon	1.777–1.987		
honey	1.484-1.504	cubic zirconia	2.173-2.21		
silicone oil	1.52	diamond	2.417		
carbon disulfide	1.628	silicon	3.96		

Figure S. The Electromagnetic Spectrum	
Wavelength in a vacuum (m)	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
<x rays=""> Microwaves></x>	← Long Radio Waves
Gamma Rays	TV. FM AM
<	Radio Waves
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Frequency (Hz)	I.
← Higher Energy Visible Light (not to scale)	Lower Energy>
7.69 × 10 ¹⁴ 6.59 × 10 ¹⁴ Ariot × 10 ¹⁴ 6.10 × 10 ¹⁴ <u>Ariot × 10¹⁴ 6.10 × 10¹⁴ 8.03 × 10¹⁴ 1.82 × 10¹⁴ 9.83 × 10¹⁴ 3.84 × 10¹⁴</u>	

Table T. Pla	Table T. Planetary Data								
	Mercury	Venus	Earth	Mars	Jupiter	Saturn	Uranus	Neptune	Pluto
Distance from Sun (m)	5.79 × 10 ¹⁰	1.08×10^{11}	1.50×10^{11}	2.28 × 10 ¹¹	7.79 × 10 ¹¹	1.43 × 10 ¹²	2.87 × 10 ¹²	4.52 × 10 ¹²	5.91 × 10 ¹²
Radius (m)	2.44×10^{6}	6.05×10^{6}	6.38×10^{6}	3.40×10^{6}	7.15×10^{7}	6.03×10^{7}	2.56×10^{7}	2.48×10^{7}	1.19×10^{6}
Mass (kg)	3.30×10^{23}	4.87×10^{24}	5.97×10^{24}	6.42×10^{23}	1.90×10^{27}	5.68×10^{26}	8.68 × 10 ²⁵	1.02×10^{26}	1.30×10^{22}
Density $\left(\frac{kg}{m^3}\right)$	5429	5243	5514	3934	1326	687	1270	1638	1850
Orbit (years)	0.24	0.61	1.00	1.88	11.8	29	84	164	248
Rotation Period (hours)	1408	-5833	23.9	24.6	9.9	10.7	-17.2	16.1	-153.3
Tilt of axis	0.034°	177.4°	23.4°	25.2°	3.1°	26.7°	97.8°	28.3°	122.5°
# of observed satellites	0	0	1	2	92	83	27	14	5
Mean temp. (°C)	167	464	15	-65	-110	-140	-195	-200	-225
Global magnetic field	Yes	No	Yes	No	Yes	Yes	Yes	Yes	Yes

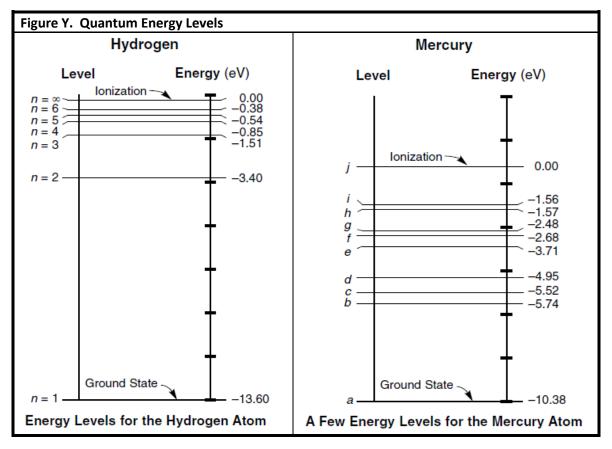
Data from NASA Planetary Fact Sheet, https://nssdc.gsfc.nasa.gov/planetary/factsheet/ last updated 11 February 2023.

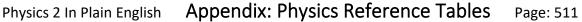
Table U. Sun & Moon Data				
Radius of the sun (m)	6.96 × 10 ⁸			
Mass of the sun (kg)	1.99 × 10 ³⁰			
Radius of the moon (m)	1.74×10^{6}			
Mass of the moon (kg)	7.35 × 10 ²²			
Distance of moon from Earth (m)	3.84×10^{8}			

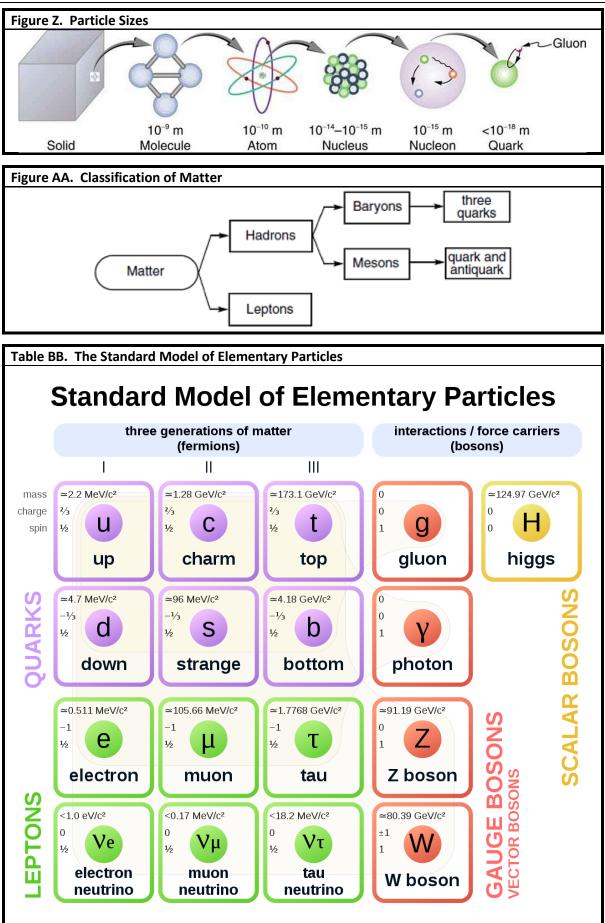
Table V.	Fluids Formulas and Equations		
	m	<i>var.</i> = name of quantity (unit)	
	$\rho = \frac{m}{V}$	$\Delta =$ change in something. (E.g., $\Delta x =$ change in x)	
	$P = \frac{F}{A}$	$\rho = \text{density}\left(\frac{\text{kg}}{\text{m}^3}\right)$	
		<i>m</i> = mass (kg)	
	$\frac{F_1}{A_1} = \frac{F_2}{A_2}$ $P_{\text{hydrostatic}} = P_H = \rho g h$ $F_B = \rho V_d g$ $P_{\text{dynamic}} = P_D = \frac{1}{2} \rho v^2$ $A_1 v_1 = A_2 v_2$ $P_{total} = P_{ext.} + P_H + P_D$ $P_1 + P_{H,1} + P_{D,1} = P_2 + P_{H,2} + P_{D,2}$	V = volume (m³) P = presure (Pa)	
Fluids		$g = \text{gravitational field} = 9.8 \frac{\text{N}}{\text{kg}} \approx 10 \frac{\text{N}}{\text{kg}}$	
		h = height or depth (m)	
		A=area (m²)	
		$v = velocity$ (of fluid) $\left(\frac{m}{s}\right)$	
		F = force (N)	
	$P_1 + \rho g h_1 + \frac{1}{2} \rho v_1^2 = P_2 + \rho g h_2 + \frac{1}{2} \rho v_2^2$	*sharastaristic property of a substance (to be looked up)	
		*characteristic property of a substance (to be looked up)	

Table V	Table W. Properties of Water and Air					
	Water			Water Air		
Temp. (°C)	$\frac{\text{Density}}{\binom{\text{kg}}{\text{m}^3}}$	Speed of Sound $\left(\frac{\mathbf{m}}{\mathbf{s}}\right)$	Vapor Pressur e (Pa)	$\frac{\text{Density}}{\left(\frac{\text{kg}}{\text{m}^3}\right)}$	Speed of Sound $\left(\frac{\mathbf{m}}{\mathbf{s}}\right)$	
0	999.78	1 403	611.73	1.288	331.30	
5	999.94	1 427	872.60	1.265	334.32	
10	999.69	1 447	1 228.1	1.243	337.31	
20	998.19	1 481	2 338.8	1.200	343.22	
25	997.02	1 496	3 169.1	1.180	346.13	
30	995.61	1 507	4 245.5	1.161	349.02	
40	992.17	1 526	7 381.4	1.124	354.73	
50	990.17	1 541	9 589.8	1.089	360.35	
60	983.16	1 552	19 932	1.056	365.88	
70	980.53	1 555	25 022	1.025	371.33	
80	971.79	1 555	47 373	0.996	376.71	
90	965.33	1 550	70 117	0.969	382.00	
100	954.75	1 543	101 325	0.943	387.23	

Table X. Atomi	c & Particle Physics (Moder	n Physics)		
		<i>var.</i> = name of quantity (unit)		
		$\Delta =$ change in something. (<i>E.g.</i> , $\Delta x =$ change in <i>x</i>)		
	$E_{photon} = hf = \frac{hc}{\lambda} = pc = \hbar\omega$	E = energy (J)		
	,,	$h = Planck's constant = 6.63 \times 10^{-34} J \cdot s$		
	$E_{k,\max} = hf - \phi$	$\hbar =$ reduced Planck's constant $= \frac{h}{2\pi} = 1.05 \times 10^{-34} \text{ J} \cdot \text{s}$		
Energy	$\lambda = \frac{h}{\rho}$	f = frequency (Hz)		
LIICIBY	$E_{photon} = E_i - E_f$	$v = velocity\left(\frac{m}{s}\right)$		
	$E^2 = (pc)^2 + (mc^2)^2$	$c = s \text{peed of light} = 3.00 \times 10^8 \frac{\text{m}}{\text{s}}$		
	1 (1 1)	$\lambda =$ wavelength (m)		
	$\frac{1}{\lambda} = R_{H} \left(\frac{1}{n_{\star}^{2}} - \frac{1}{n_{\star}^{2}} \right)$	$p = momentum (N \cdot s)$		
		m = mass (kg)		
		K = kinetic energy (J)		
		$\phi =$ work function* (J)		
		$R_{\rm H} = \text{Rydberg constant} = 1.10 \times 10^7 \text{ m}^{-1}$		
	1	$\gamma =$ Lorentz factor (dimensionless)		
	$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$	<i>L</i> = length in moving reference frame (m)		
Special Relativity	$\sqrt{1-v^{2}/c^{2}}$	$L_o = $ length in stationary reference frame (m)		
	·	$\Delta t'$ = time in stationary reference frame (s)		
	$\gamma = \frac{L_o}{L} = \frac{\Delta t'}{\Delta t} = \frac{m_{rel}}{m}$	$\Delta t =$ time in moving reference frame (s)		
	' $L \Delta t m_a$	$m_o =$ mass in stationary reference frame (kg)		
		$m_{rel} =$ apparent mass in moving reference frame (kg)		
		*characteristic property of a substance (to be looked up)		







1																		,
Period	1 1 1																I	18 VIII A
۲	H t	2											13	4	15	16		² He
-	hydrogen 1.008	∀ ∥											ΑШ	×≥	۲ ×	A I A	A II A	helium 4.003
_	3	4											2	9				10
2	:	Be											ш	ပ	z	0	ш	Pe
_	lithium 6.968	beryllium 9.012											boron 10.81	carbon 12.01	nitrogen 14.01	oxygen 16.00	fluorine 19.00	neon 20.18
_	11	12										_				16		18
3	Na	Mg	e l	4	5	9	7	8	6	10	£ ;	12	A	Si	٩	S	ច	Ā
_	sodium 22 00	magnesium 24.21	8	≤ 2	< B	AI B	VII B	VIII B	VIII B	VIII B	8	8	aluminum 26.08	silicon 28.00	phosphorus 30 07	sulfur 32.07	chlorine 3도 A도	argon 30 05
_	19		21	22	23	24	25	26	27	28	29	30						36
4	¥	Ca	Sc	Ξ	>	ŗ	ЧЛ	Fe	ပိ	ïŻ	Cu	Zn	Ga	Ge	As	Se	Br	۲ ۲
•	potassium	calcium 40.00	scandium	titanium 47 07	vanadium 50.04	chromium 52,00	manganese	iron EE oE	cobalt Ee oo	nickel Eo 60	copper	zinc	gallium	germanium	arsenic	selenium	bromine	krypton 82.80
_	37 33.10			40.07								48						00.00 54
LC.	Rb	Sr	≻	Zr	qN	Мо	Tc	Ru	Rh	Ъd	Ag	Cd	ŋ	Sn	Sb	Те	_	Xe
,	rubidium	strontium	yttrium	zirco nium	niobium	molybdenum	technetium	ruthenium	rhodium	palladium	silver	cadmium	indium	ti	antimony	tellurium	iodine	nonex
	85.47	87.62	88.91	91.22	92.91	95.95	88	101.1	102.9	106.4	107.9	112.4	114.8	118.7	121.8	127.6	126.9	131.3
_	55 C			72 LIF		74	75	76	-			80 L ~	8 F	82 Dh				86 D
9	Cosium		LLU Iutetium	hafnium	tantalum	VV tunasten	rhenium	osmium osmium	iridium	platinum			thallium		D Dismuth	polonium minolog	astatine	
_	132.9	137.3	175.0	178.5	180.9	183.8	186.2	190.2	192.2	195.1	197.0	200.6	204.4	207.2	209.0	209		222
_	87		103	104	105	106	107	108	109		111	112			-	116		118
7	Fr	Ra		Rf rutherfordium	Db	Sg	Bh	HSseium	Mt	DS darmstadtium	Rg	Cnemicum	Nh	FI flerovium	Mc	Lv	TS tennessine	Og
_	223	226	262	267	268	271	272	270	276	281	280	285	284	289	288	293	292	294
			57					62	63							70		
	5	lanthanides			Pr		Pm	Sm	Eu	Gd	Ч	D	운	ц.	E	۲b		
	(rare ex	(rare earm metals)	lanthanum 138 q	cerium 140 1	praseodymium 140 Q	neodymium 144.2	promethium 145	samarium 150.4	europium 152 0	gadolinium 1573	158 q	dysprosium 162 5	holmium 16.4 9	erbium 167.3	thulium 16.8 Q	ytterbium 173 1		
					91	92		94				98	66			102		
		actinides		Тh	Ра		Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No		
			actinium	thorium	protactinium	uranium	neptunium	plutonium	americium	curium	berkelium	californium	einsteinium	fermium 25-7	mendelevium	nobelium		
		_	177	V.262	231.0	0.062	107	744	243	241	247	107	707	107	807	ACZ		

Figure CC. Periodic Table of the Elements

Table DD. Symbols Used	in Nuclear Phys	sics
Name	Notation	Symbol
alpha particle	${}^{4}_{2}$ He or ${}^{4}_{2}\alpha$?
beta particle (electron)	$_{\scriptscriptstyle -1}^{\scriptscriptstyle 0} e$ or $_{\scriptscriptstyle -1}^{\scriptscriptstyle 0} eta$	2 -
gamma radiation	°γ	?
neutron	¹ ₀ <i>n</i>	n
proton	${}_1^1H$ or ${}_1^1p$	p
positron	$^{0}_{_{+1}}\!e$ or $^{0}_{_{+1}}\!eta$? +

Table FF. Constants Us	ed in Nuclear Physics
Constant	Value
mass of an electron (m_e)	0.00055 amu
mass of a proton (m_p)	1.00728 amu
mass of a neutron (m _n)	1.00867 amu
Becquerel (Bq)	1 disintegration/second
Curie (Ci)	3.7 x 10 ¹⁰ Bq

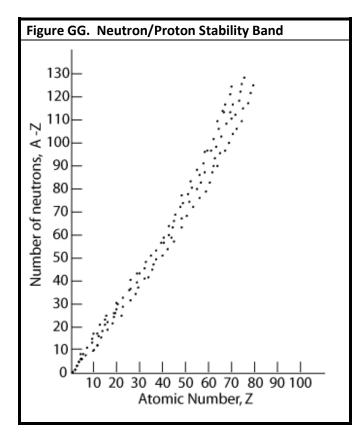


Table EE.	able EE. Selected Radioisotopes						
Nuclide	Half-Life	Decay Mode					
³ Н	12.26 y	? -					
¹⁴ C	5730 y	? -					
¹⁶ N	7.2 s	2 -					
¹⁹ Ne	17.2 s	? +					
²⁴ Na	15 h	? -					
²⁷ Mg	9.5 min	? -					
³² P	14.3 d	? -					
³⁶ Cl	3.01 × 10 ⁵ y	? -					
³⁷ K	1.23 s	? +					
⁴⁰ K	1.26 × 10 ⁹ у	? +					
⁴² K	12.4 h	? -					
³⁷ Ca	0.175 s	2 -					
⁵¹ Cr	27.7 d	?					
⁵³ Fe	8.51 min	[] -					
⁵⁹ Fe	46.3 d	? -					
⁶⁰ Co	5.26 y	? -					
⁸⁵ Kr	10.76 y	2 -					
⁸⁷ Rb	4.8 × 10 ¹⁰ y	2 -					
⁹⁰ Sr	28.1 y	2 -					
⁹⁹ Tc	2.13 x 10⁵ y	2 -					
131	8.07 d	? -					
¹³⁷ Cs	30.23 y	2 -					
¹⁵³ Sm	1.93 d	[?] -					
¹⁹⁸ Au	2.69 d	[?] -					
²²² Rn	3.82 d	?					
²²⁰ Fr	27.5 s	?					
²²⁶ Ra	1600 y	2					
²³² Th	1.4 x 10 ¹⁰ y	2					
²³³ U	1.62 x 10⁵ y	2					
²³⁵ U	7.1 x 10 ⁸ y	2					
²³⁸ U	4.51 x 10 ⁹ y	2					
²³⁹ Pu	2.44 x 10 ⁴ y	2					
²⁴¹ Am	432 y	?					

Table HH. Mathematics	Formulas				
		$0 2 \times 10^{-3} = 2 \times 0.001 = 0.002$			
Scientific Notation					
	$(3 \times 10^{4})(2 \times 10^{-3}) = (3 \cdot 2)(10^{-3})$	$(4 \cdot 10^{-3}) = 6 \times 10^{4 + (-3)} = 6 \times 10^{1} = 60$			
Rounding	15 <u>3</u> 54 → 15 <u>4</u> 00	27 <mark>2</mark> 49.99 → 27 <mark>2</mark> 00			
(to underlined place)	0.037 5	$00 \rightarrow 0.037\frac{5}{2}$			
	$\frac{a}{c} + \frac{c}{c} = \frac{a}{c}$	$\frac{d}{d} + \frac{c}{d} \cdot \frac{b}{b} = \frac{ad + cb}{bd}$			
Algebra with Fractions	$\frac{a}{b} \cdot \frac{c}{c} = \frac{ac}{bc}$	$\frac{a}{\frac{b}{c}} = a \cdot \frac{c}{b}$			
	$\frac{a}{x} = b \rightarrow x \cdot \frac{a}{x} = b \cdot x \rightarrow x$	$\Rightarrow a = bx \rightarrow \frac{a}{b} = \frac{bx}{b} \rightarrow \frac{a}{b} = x$			
Quadratic Equation	$ax^2 + bx + c = 0$	$\rightarrow x = \frac{-b \pm \sqrt{b^2 - 4ac}}{ac}$			
		2a			
	$A = \frac{1}{2}bh$	C			
All Triangles	a _ b _ c				
, in triangles	$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$				
	$c^2 = a^2 + b^2 - 2ab\cos C$	$\sim A \qquad r \rightarrow b \qquad c$			
	$c^2 = a^2 + b^2$				
	$\sin\theta = \frac{a}{1} = \frac{\text{opposite}}{1}$				
	<i>c</i> hypotenuse	e^{c} $g_{0} = a$			
	$\cos\theta = \frac{b}{c} = \frac{\text{adjacent}}{\text{hypotenuse}}$				
Right Triangles					
	$\tan\theta = \frac{\sin\theta}{\cos\theta} = \frac{a}{b} = \frac{\text{opposite}}{\text{adjacent}}$	b			
	$\cos\theta$ b adjacent b=c cos θ				
	$a = c \cos \theta$				
		<i>a</i> , <i>b</i> , <i>c</i> = length of a side of a triangle			
Rectangles, Parallelograms and Trapezoids	$A = \overline{b}h$	$\theta = $ angle			
- P		A = area			
Rectangular Solids	V = Lwh	<i>C</i> = circumference			
		S = surface area			
Circles	$C=2\pi r$	V = volume			
	$A = \pi r^2$	b = base			
	$S = 2\pi r L + 2\pi r^2 = 2\pi r (L+r)$	$\overline{b} = \text{average base } = \frac{b_1 + b_2}{2}$			
Cylinders	$V = \pi r^2 L$	2 h=height			
	$S=4\pi r^2$	L = length			
Spheres	$V = \frac{4}{3}\pi r^3$	<i>w</i> = width			
	$v = -\frac{\pi}{3}\pi r$	r = radius			

Table II.	Values of	f Trigonon	netric Fun	ctions					
degree	radian	sine	cosine	tangent	degree	radian	sine	cosine	tangent
0°	0.000	0.000	1.000	0.000					
1°	0.017	0.017	1.000	0.017	46°	0.803	0.719	0.695	1.036
2°	0.035	0.035	0.999	0.035	47°	0.820	0.731	0.682	1.072
3°	0.052	0.052	0.999	0.052	48°	0.838	0.743	0.669	1.111
4°	0.070	0.070	0.998	0.070	49°	0.855	0.755	0.656	1.150
5°	0.087	0.087	0.996	0.087	50°	0.873	0.766	0.643	1.192
6°	0.105	0.105	0.995	0.105	51°	0.890	0.777	0.629	1.235
7°	0.122	0.122	0.993	0.123	52°	0.908	0.788	0.616	1.280
8°	0.140	0.139	0.990	0.141	53°	0.925	0.799	0.602	1.327
9°	0.157	0.156	0.988	0.158	54°	0.942	0.809	0.588	1.376
10°	0.175	0.174	0.985	0.176	55°	0.960	0.819	0.574	1.428
11°	0.192	0.191	0.982	0.194	56°	0.977	0.829	0.559	1.483
12°	0.209	0.208	0.978	0.213	57°	0.995	0.839	0.545	1.540
13°	0.227	0.225	0.974	0.231	58°	1.012	0.848	0.530	1.600
14°	0.244	0.242	0.970	0.249	59°	1.030	0.857	0.515	1.664
15°	0.262	0.259	0.966	0.268	60°	1.047	0.866	0.500	1.732
16°	0.279	0.276	0.961	0.287	61°	1.065	0.875	0.485	1.804
17°	0.297	0.292	0.956	0.306	62°	1.082	0.883	0.469	1.881
18°	0.314	0.309	0.951	0.325	63°	1.100	0.891	0.454	1.963
19°	0.332	0.326	0.946	0.344	64°	1.117	0.899	0.438	2.050
20°	0.349	0.342	0.940	0.364	65°	1.134	0.906	0.423	2.145
21°	0.367	0.358	0.934	0.384	66°	1.152	0.914	0.407	2.246
22°	0.384	0.375	0.927	0.404	67°	1.169	0.921	0.391	2.356
23°	0.401	0.391	0.921	0.424	68°	1.187	0.927	0.375	2.475
24°	0.419	0.407	0.914	0.445	69°	1.204	0.934	0.358	2.605
25°	0.436	0.423	0.906	0.466	70°	1.222	0.940	0.342	2.747
26°	0.454	0.438	0.899	0.488	71°	1.239	0.946	0.326	2.904
27°	0.471	0.454	0.891	0.510	72°	1.257	0.951	0.309	3.078
28°	0.489	0.469	0.883	0.532	73°	1.274	0.956	0.292	3.271
29°	0.506	0.485	0.875	0.554	74°	1.292	0.961	0.276	3.487
30°	0.524	0.500	0.866	0.577	75°	1.309	0.966	0.259	3.732
31°	0.541	0.515	0.857	0.601	76°	1.326	0.970	0.242	4.011
32°	0.559	0.530	0.848	0.625	77°	1.344	0.974	0.225	4.331
33°	0.576	0.545	0.839	0.649	78°	1.361	0.978	0.208	4.705
34°	0.593	0.559	0.829	0.675	79°	1.379	0.982	0.191	5.145
35°	0.611	0.574	0.819	0.700	80°	1.396	0.985	0.174	5.671
36°	0.628	0.588	0.809	0.727	81°	1.414	0.988	0.156	6.314
37°	0.646	0.602	0.799	0.754	82°	1.431	0.990	0.139	7.115
38°	0.663	0.616	0.788	0.781	83°	1.449	0.993	0.122	8.144
39°	0.681	0.629	0.777	0.810	84°	1.466	0.995	0.105	9.514
40°	0.698	0.643	0.766	0.839	85°	1.484	0.996	0.087	11.430
41°	0.716	0.656	0.755	0.869	86°	1.501	0.998	0.070	14.301
42°	0.733	0.669	0.743	0.900	87°	1.518	0.999	0.052	19.081
43°	0.750	0.682	0.731	0.933	88°	1.536	0.999	0.035	28.636
44°	0.768	0.695	0.719	0.966	89°	1.553	1.000	0.017	57.290
45°	0.785	0.707	0.707	1.000	90°	1.571	1.000	0.000	∞

Table JJ.	able JJ. Some Exact and Approximate Conversions						
Length	1 cm	≈	width of a small paper	r clip)		
	1 inch (in.)	Ξ	2.54 cm				
	length of a US dollar bill	=	6.14 in.	=	15.6 cm		
	12 in.	≡	()		30 cm		
	3 ft.	=	, , ,		1 m 39.37 in.		
	1 m 1 km	≡ ≈		=	39.37 m.		
	5,280 ft.	~ E		≈	1.6 km		
	-)						
Mass /	1 small paper clip	≈	0.5 g				
Weight	US 1¢ coin (1983–present)	=	2.5 g				
	US 5¢ coin	=	- 0				
	1 oz.	≈	30 g				
	one medium-sized apple	≈			3.6 oz.		
	1 pound (lb.)	=		≈	454 g		
	1 pound (lb.) 1 ton	≈ ≡	-	~	0.9 tonne		
	1 tonne	=			1.1 ton		
	I tonne	-	1000 Kg	~	1.1 (011		
Volume	1 pinch	*	¹ / ₁₆ teaspoon (tsp.)				
	1 dash	≈					
	1 mL	≈					
	1 tsp.	≈		≈	60 drops		
	3 tsp.	Ξ	1 tablespoon (Tbsp.)		15 mL		
	2 Tbsp.	≡	1 fluid ounce (fl. oz.)	≈	30 mL		
	8 fl. oz.	≡		≈	250 mL		
	16 fl. oz.	≡	1 U.S. pint (pt.)	*	500 mL		
	20 fl. oz.	≡	1 Imperial pint (UK)	≈	600 mL		
	2 pt. (U.S.)	≡	1 U.S. quart (qt.)	≈	1 L		
	4 qt. (U.S.)	Ξ	1 U.S. gallon (gal.)	≈	3.8 L		
	4 qt. (UK) ≡ 5 qt. (U.S.)	≡	1 Imperial gal. (UK)	≈	4.7 L		
Speed /	1 ^m /s	=	3.6 ^{km} /h	*	2.24 ^{mi.} /h		
Velocity	60 ^{mi.} /h	≈	, 100 ^{km} /h	≈	, 27 ^m /s		
			100 /1		27 73		
Energy	1 cal	≈	4.18 J				
	1 Calorie (food)	≡	1 kcal	≈	4.18 kJ		
	1 BTU	≈	1.06 kJ				
Power	1 hp	≈	746 W				
	1 kW	≈	1.34 hp				
Temper-	0 К	=	–273.15 °C	_	absolute zero		
ature	-						
	0 °R	Ξ	–459.67 °F	=	absolute zero		
	0 °F	≈	-18 °C ≡ 459.67 °R				
	32 °F	=	0°C ≡ 273.15K	=	water freezes		
	70 °F	≈	21 °C	≈	room temperature		
					-		
	212 °F	=	100 °C	=	water boils		
Speed of light	300 000 000 ^m /s	~	186 000 ^{mi.} /s	*	1 ^{ft.} /ns		

Table	КΚ.	Greek
Alphal		
А	α	alpha
В	β	beta
Г	γ	gamma
Δ	δ	delta
E	ε	epsilon
Z	ζ	zeta
н	η	eta
Θ	θ	theta
1	ι	iota
К	к	kappa
Λ	λ	lambda
М	μ	mu
Ν	ν	nu
Ξ	ξ	xi
0	0	omicron
П	π	pi
Р	ρ	rho
Σ	σ	sigma
Т	τ	tau
Y	υ	upsilon
Φ	φ	phi
х	χ	chi
Ψ	ψ	psi
Ω	ω	omega

Table LL. D	ecimal
Equivalents	
$\frac{1}{2} = 0.5$	$\frac{1}{5} = 0.2$
$\frac{1}{3} = 0.33\overline{3}$	$\frac{2}{5} = 0.4$
$\frac{2}{3} = 0.66\overline{6}$	$\frac{3}{5} = 0.6$
$\frac{1}{4} = 0.25$	4/ ₅ = 0.8
$\frac{3}{4} = 0.75$	$\frac{1}{8} = 0.125$
$\frac{1}{6} = 0.166\overline{6}$	$\frac{3}{8} = 0.375$
$\frac{5}{6} = 0.833\overline{3}$	$\frac{5}{8} = 0.625$
$\frac{1}{7} = 0.\overline{142857}$	$\frac{7}{8} = 0.875$
$\frac{2}{7} = 0.\overline{285714}$	$\frac{1}{9} = 0.11\overline{1}$
$\frac{3}{7} = 0.\overline{428571}$	⅔=0.22 2
⁴ / ₇ = 0.571428	$\frac{4}{9} = 0.44\overline{4}$
⁵ ⁄ ₇ = 0.714285	% = 0.555
⁶ / ₇ = 0.857142	% = 0.777
$\frac{1}{11} = 0.0909$	⁸ / ₉ = 0.888
$\frac{2}{11} = 0.18\overline{18}$	$\frac{1}{16} = 0.0625$
$\frac{3}{11} = 0.27\overline{27}$	$\frac{3}{16} = 0.1875$
$\frac{4}{11} = 0.36\overline{36}$	$\frac{5}{16} = 0.3125$
⁵ ∕ ₁₁ = 0.4545	$\frac{7}{16} = 0.4375$
$\frac{6}{11} = 0.54\overline{54}$	$\frac{9}{16} = 0.5625$
⅔=0.6363	$\frac{11}{16} = 0.6875$
$\frac{8}{11} = 0.72\overline{72}$	$\frac{13}{16} = 0.8125$
⁹ / ₁₁ =0.81 81	$\frac{15}{16} = 0.9375$
¹⁰ / ₁₁ = 0.9090	

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