Unit: Electric Force, Field & Potential

NGSS Standards/MA Curriculum Frameworks (2016): HS-PS2-4

AP® Physics 2 Learning Objectives/Essential Knowledge (2024): 10.1.A, 10.1.A.2, ,

10.1.A.3, 10.1.A.3.i, 10.1.A.3.ii, 10.1.A.4, 10.1.B, 10.1.B.1, 10.1.B.2, 10.1.B.3 Mastery Objective(s): (Students will be able to...)

- Solve problems using Coulomb's Law
- Quantitatively predict the effects on the electrostatic force when one of the variables (amount of electric charge or distance) in Coulomb's Law is changed.

#### Success Criteria:

Details

**Big Ideas** 

- Variables are correctly identified and substituted correctly into the correct part of the correct equation.
- Algebra is correct and rounding to appropriate number of significant figures is reasonable.

#### Language Objectives:

• Explain how force and distance both affect the amount of force between two charged objects.

Tier 2 Vocabulary: charge

#### Labs, Activities & Demonstrations:

- Charged balloon or Styrofoam sticking to wall.
- Charged balloon pushing meter stick.
- Van de Graaff generator with negative electrode attached to inertia balance pan.

#### Notes:

Electric charge is measured in Coulombs (abbreviation "C"). One Coulomb is the amount of electric charge transferred by a current of 1 ampere for a duration of 1 second.

+1 C is the charge of  $6.2415 \times 10^{18}$  protons.

-1 C is the charge of  $6.2415 \times 10^{18}$  electrons.

A single proton or electron therefore has a charge of  $\pm 1.6022 \times 10^{-19}$  C. This amount of charge is called the <u>elementary charge</u>, because it is the charge of one elementary particle.

An object can only have an integer multiple of this amount of charge, because it is impossible<sup>\*</sup> to have a charge that is a fraction of a proton or electron.

Because charged particles attract or repel each other, that attraction or repulsion must be a force, which can be measured and quantified. The force is directly proportional to the strengths of the charges, and inversely proportional to the square of the distance. The formula is:

$$F_e = \frac{1}{4\pi\varepsilon_o} \cdot \frac{q_1 q_2}{r^2} = k \frac{q_1 q_2}{r^2}$$

where:

Details

**Big Ideas** 

- $F_e$  = electrostatic force of repulsion between electric charges. A positive value of  $F_e$  denotes that the charges are repelling (pushing away from) each other; a negative value of  $F_e$  denotes that the charges are attracting (pulling towards) each other.<sup>†</sup>
- $\varepsilon_{o}$  = electric permittivity of free space  $\approx 8.85 \times 10^{-12} \frac{F}{m}$ .

$$k = \text{electrostatic constant} = = \frac{1}{4\pi\varepsilon_o} \approx 9.0 \times 10^9 \frac{\text{N} \cdot \text{m}^2}{\text{C}^2}.$$

 $q_1$ ,  $q_2$  = the charges on objects #1 and #2 respectively

This formula is Coulomb's Law, named for its discoverer, the French physicist Charles-Augustin de Coulomb.

Coulomb's Law has several parallels with Newton's Law of Universal Gravitation:

$$F_g = G \frac{m_1 m_2}{r^2} \qquad \qquad F_e = k \frac{q_1 q_2}{r^2}$$

gravitational force

electrostatic force

The situations are similar in that there are two objects, each exerting a force on the other separated by some distance, r. With the gravitational force, masses can only attract, which means  $F_g$  is always attractive. However,  $F_e$  can be either attractive or repulsive, because charges attract or repel, depending on whether they have opposite or like signs. If the charges have the same sign (repulsive), the value of  $F_e$  will be positive; if the charges have opposite signs (attractive), the value of  $F_e$  will be negative.

<sup>\*</sup> This is true for macroscopic objects. Certain quarks, which are the particles that protons and neutrons are made of, have charges of  $\frac{1}{3}$  or  $\frac{2}{3}$  of an elementary charge.

<sup>&</sup>lt;sup>+</sup> It is unfortunate that a positive value for force denotes attraction in the gravitational force equation, but repulsion in the electrostatic force equation.

Big Ideas	Details	Unit: Electric Force, Field & Potential
	Sample problems:	
	Q: Find the force of electrostatic attraction between the proton and electron in a hydrogen atom if the radius of the atom is 37.1 pm	
	<ul> <li>A: The charge of a single proto is −1.60 × 10<sup>-19</sup> C.</li> </ul>	n is 1.60 $ imes$ 10 <sup>-19</sup> C, and the charge of a single electron
	$37.1 \text{ pm} = 3.71 \times 10^{-11} \text{ m}$	
	$F_e = \frac{kq_1q_2}{r^2} = \frac{(8.99 \times 10^9)(1.6)}{(3.8)}$	$\frac{0 \times 10^{-19})(-1.60 \times 10^{-19})}{71 \times 10^{-11})^2} = -1.67 \times 10^{-7} \mathrm{N}$
	However, rather than memory attraction or repulsion, it's e	ative, which signifies that the force is attractive. rize whether a positive or negative indicates asier to reason that the charges are opposite, so the prize what you can understand!
	separated by distance d. If t	with charge $+q$ (which means $q_1 = q_2 = q$ ) are he amount of charge on one of the particles is halved what will be the effect on the force between them?
	A: To solve this problem, we fir	st set up Coulomb's Law:
	$F_e = \frac{kq_1q_2}{r^2}$	
		charges with half of itself—let's say $q_1$ will become e the distance $r$ with (2 $r$ ). This gives:
	$F_e = \frac{k(0.5q_1)q_2}{(2r)^2}$	
	Simplifying and rearranging	his expression gives:
	$F_e = \frac{0.5kq_1q_2}{4r^2} = \frac{0.5}{4} \cdot \frac{kq_1q_2}{r^2} =$	$\frac{1}{8} \cdot \frac{kq_1q_2}{r^2}$
	Therefore, the new $F_e$ will b	$\frac{1}{8}$ of the old $F_e$ .

Details

**Big Ideas** 

An easier way to solve this problem is to do a "before and after" calculation. Set the value of every quantity in the "before" equation to 1:

$$F_e = \frac{kq_1q_2}{r^2} \rightarrow \frac{1\cdot 1\cdot 1}{1^2} = 1$$

For the "after" equation, replace quantities that change with their multipliers:

$$F_e = \frac{kq_1q_2}{r^2} \rightarrow \frac{1 \cdot 1 \cdot 0.5}{2^2} = \frac{0.5}{4} = \frac{1}{8}$$

The "before" value for  $F_e$  was 1, and the "after" value was  $\frac{1}{8}$ , which means the new force will be  $\frac{1}{8}$  of the original force.

This method is sometimes called "Bertha's Rule of Ones," or the "factor of change" method.



